

Probing exotic superconductors  
by high sensitivity microcalorimetry

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CEA-Grenoble, IRIG-LATEQS



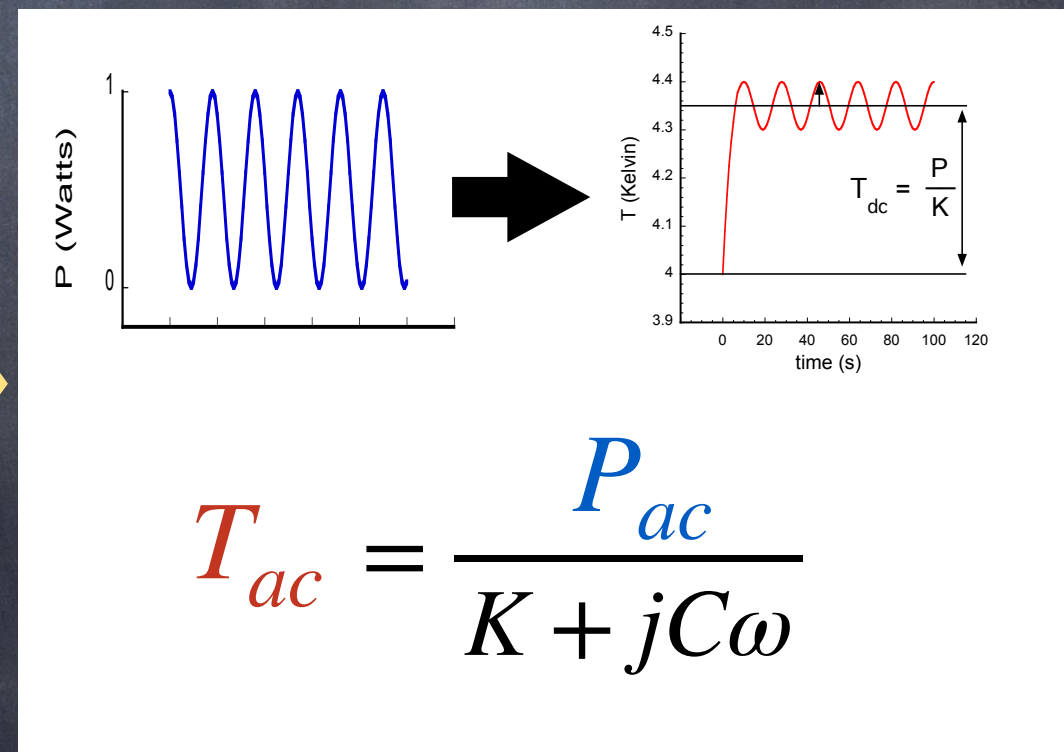
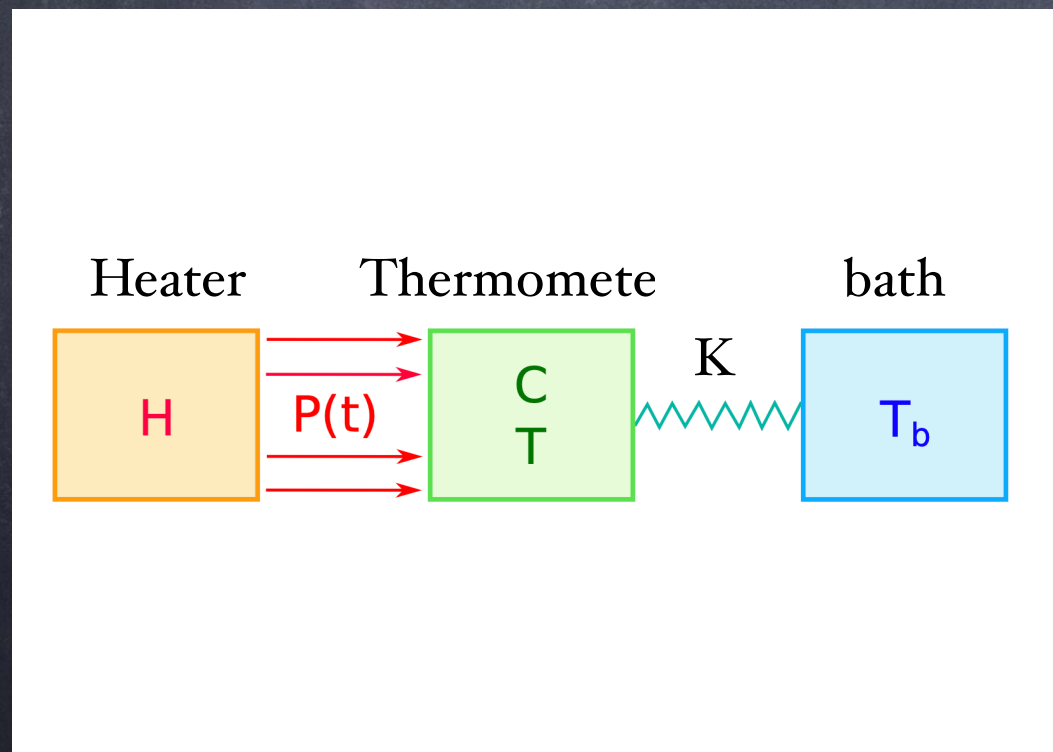
# Alternative calorimetry

applying an alternative **heating** power  $P_{ac}$  (at  $\omega$ )

to a sample of heat capacity **C**

linked to the thermal bath through **K**

and recording corresponding **temperature oscillations**  $T_{ac}$





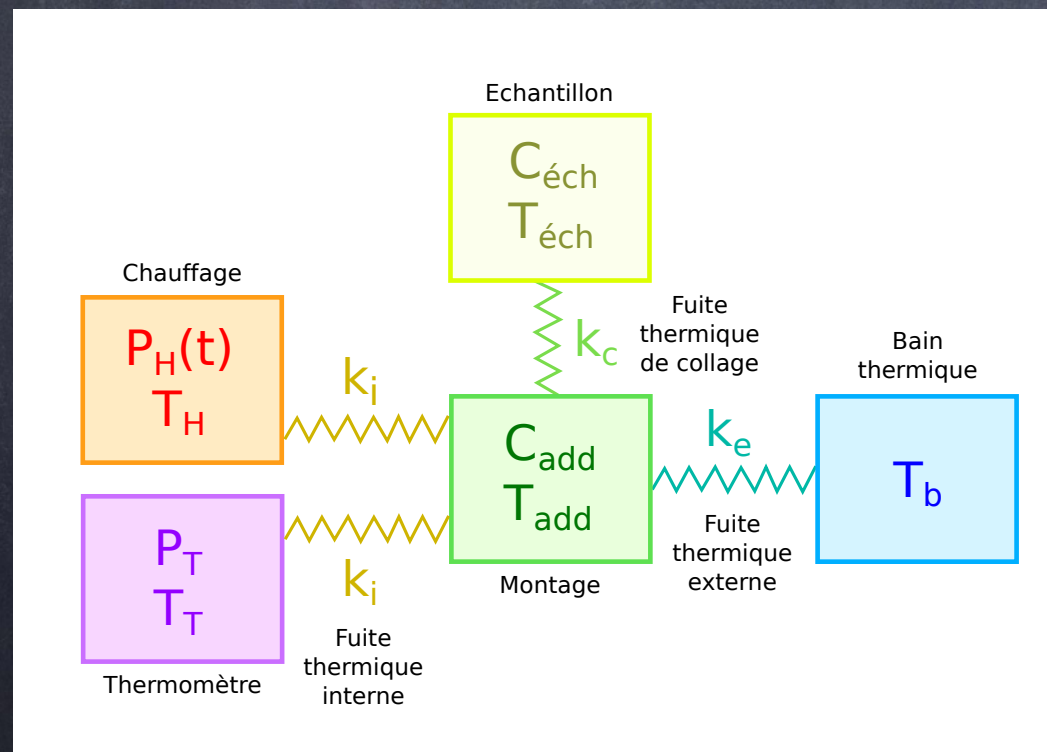
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Unfortunately life is a little bit more complicated (internal couplings)

$$T_{ac} = \frac{P_{ac}}{K_{eff} + jC_{eff}\omega}$$

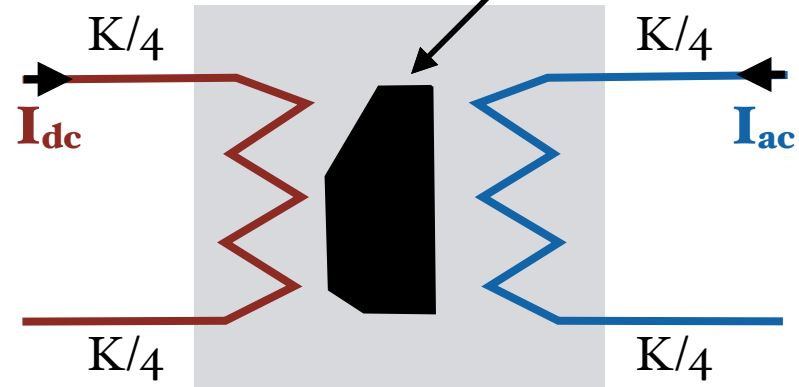
but  $C_{eff} \rightarrow C$  in the *good* conditions...



Thermometer

Heater

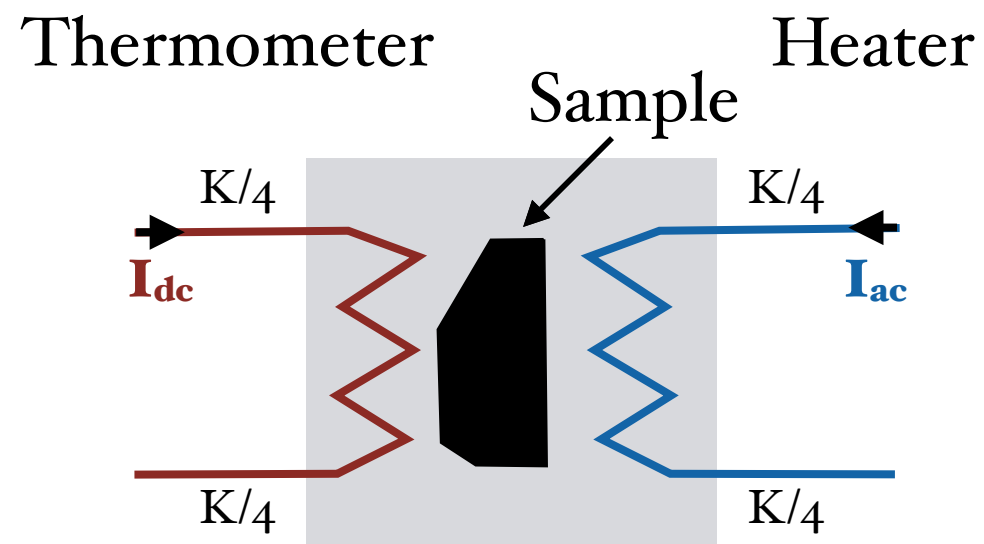
Sample



**HEATER** : resistance  $R_H$  (or optical fiber,...)

**THERMOMETER** :  $R_T$  (or thermocouple,...)





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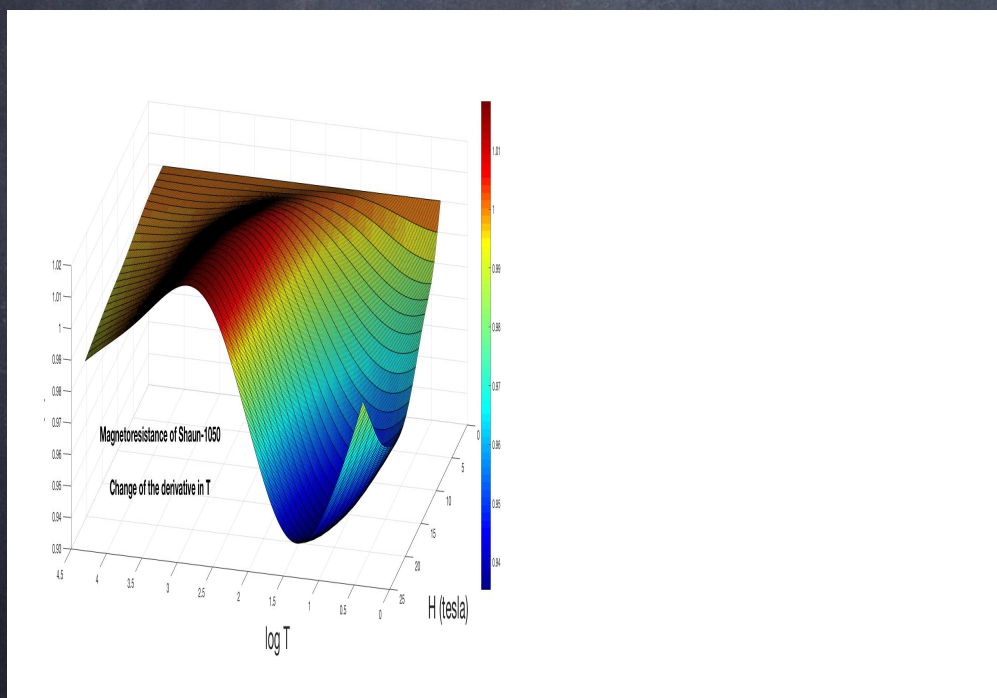
**THERMOMETER** :  $R_T$  (or thermocouple,...)

and this technique then requires

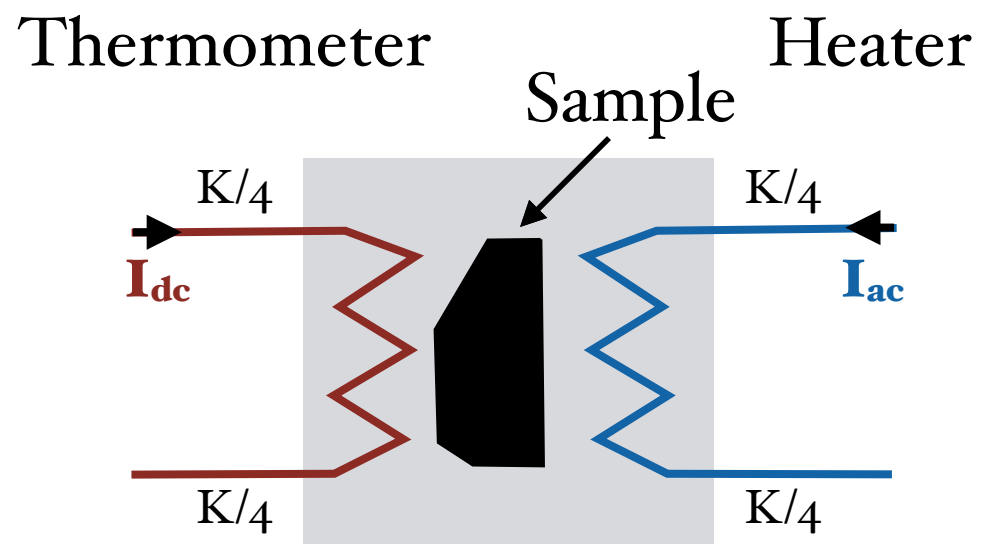
**very demanding calibrations**

for  $R(T, H)$

$$V_{dc} = R_T(T, H) I_{dc} \rightarrow T$$







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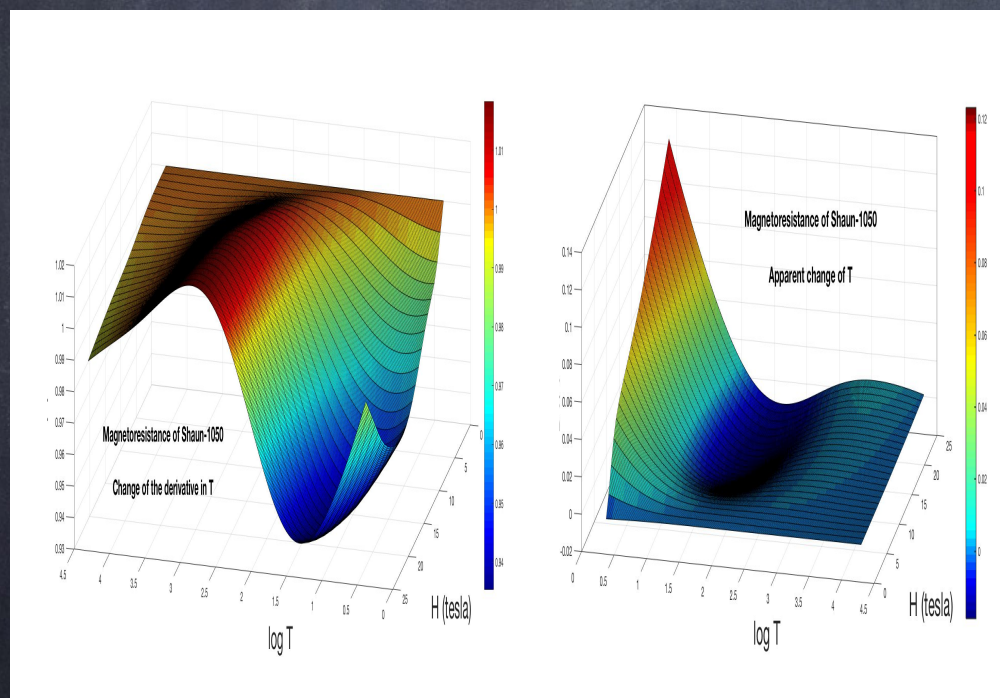
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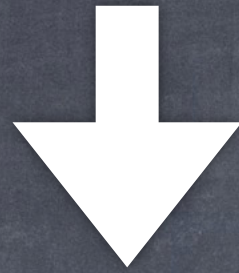
$$V_{dc} = R_T(T, H) I_{dc} \rightarrow T$$

**AND  $dR/dT$**

$$V_{ac} = \frac{dR_T}{dT}(T, H) T_{ac} I_{dc} \rightarrow C$$

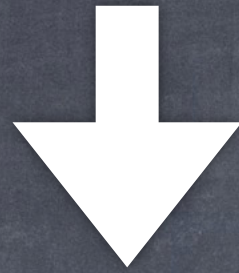






- **Small samples**  
a few milligrams down to ~ 10 micrograms (or less)
- **Continuous H and/or T sweeps**  
in **extreme conditions** : 36T-0.1K (even under pressure)
- **Good absolute accuracy (> 95%)**  
as deduced from measurements in ultra pure Cu (1mg)

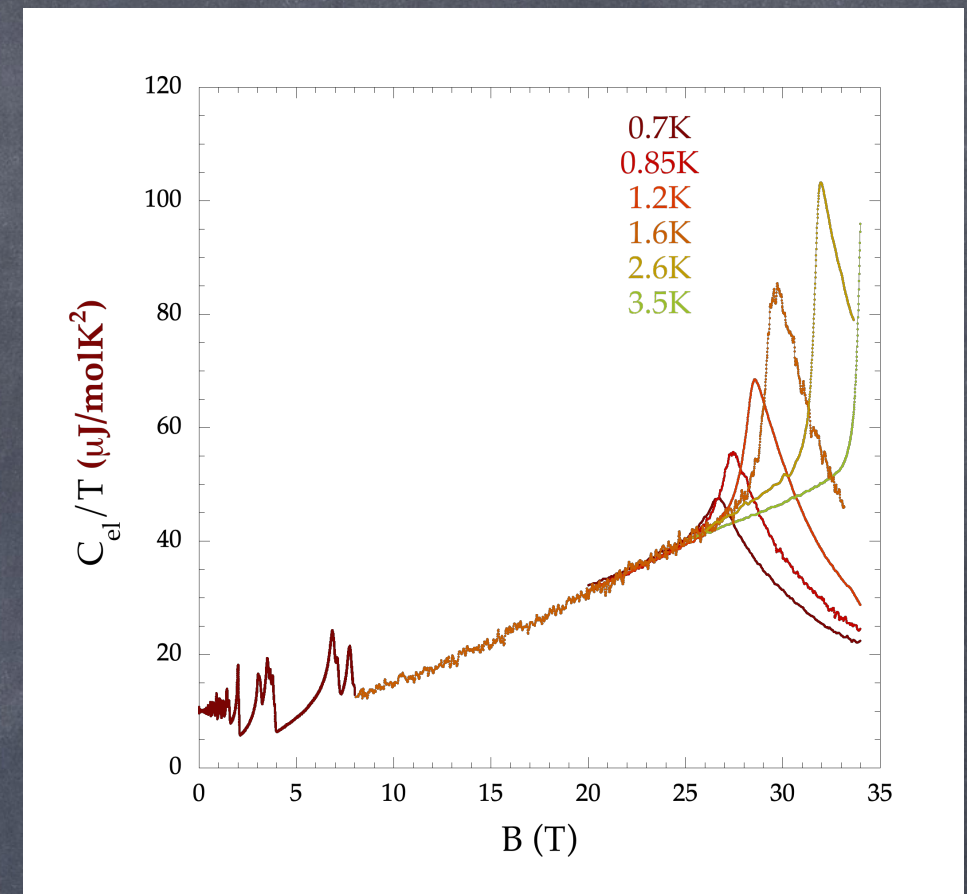




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- **excellent resolution (down to a few  $10^{-5}$  of the total signal)**  
Lock-in detection, filters  $\rightarrow \Delta C \sim 10^{-13} \text{ J/K}$

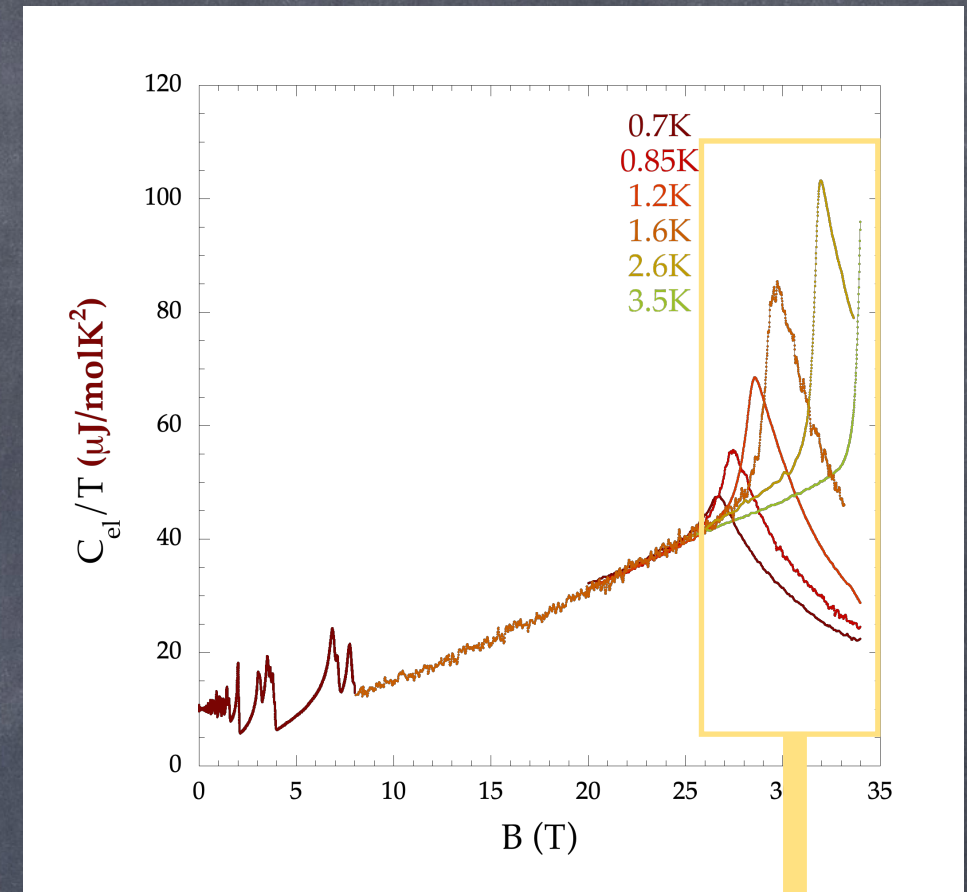


⇒ detection of **small *features*** in  $C/T$   
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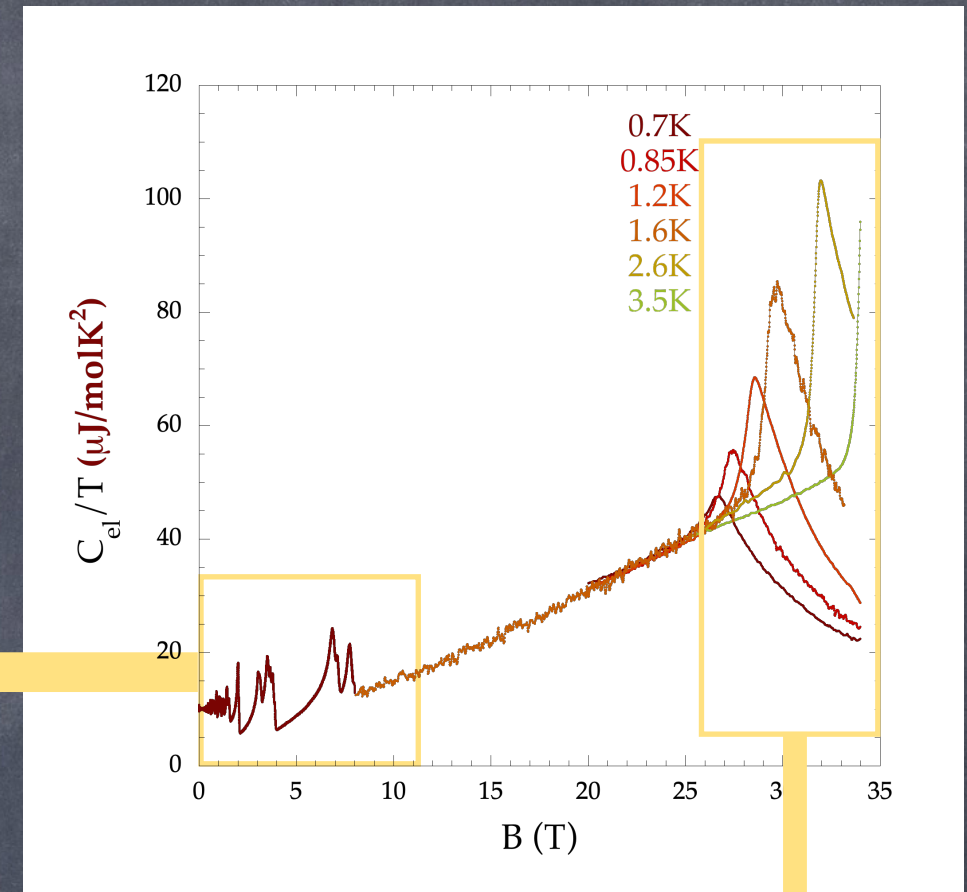
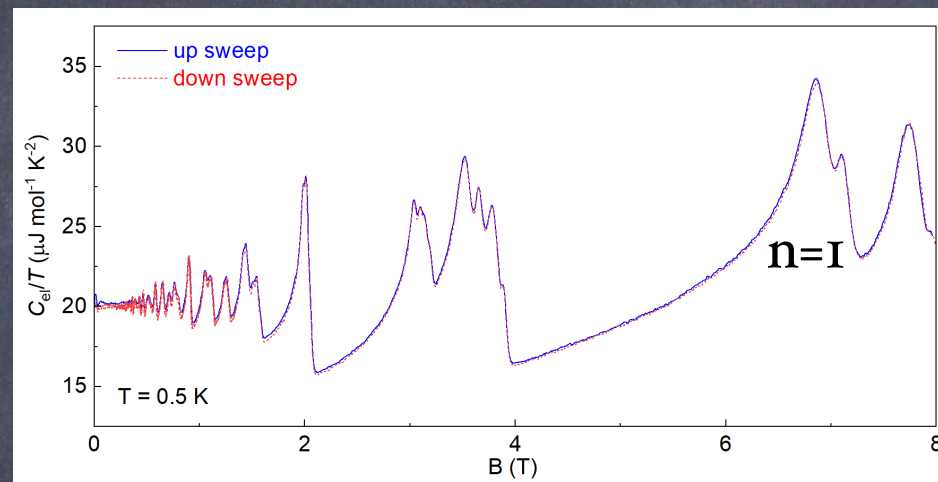


Electronic phase  
transition in the  
quantum limit (1D)  
Marcenat *et al.* PRL 2021



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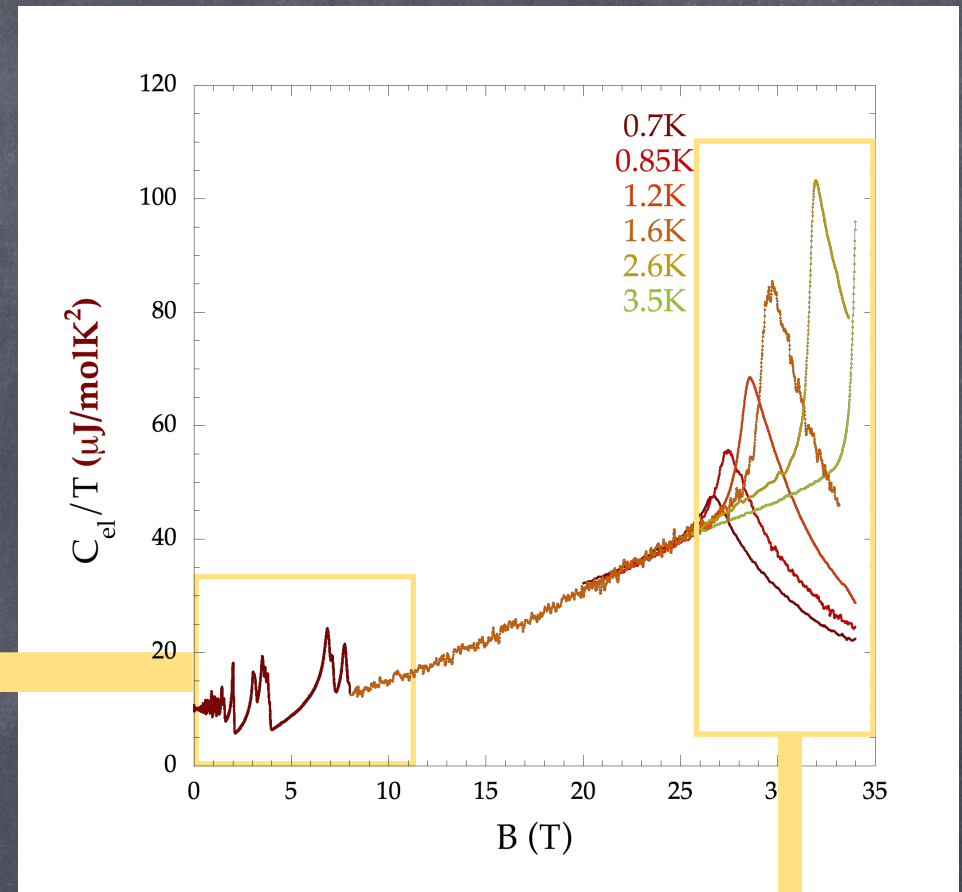
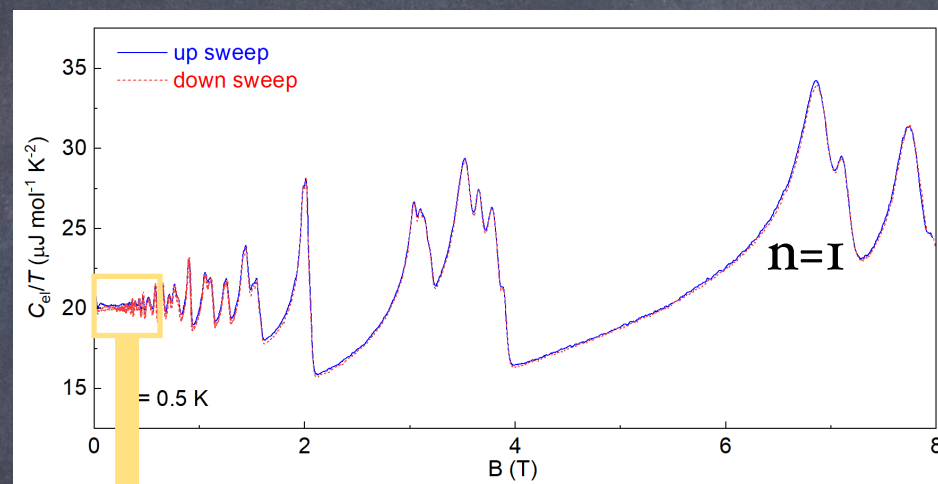


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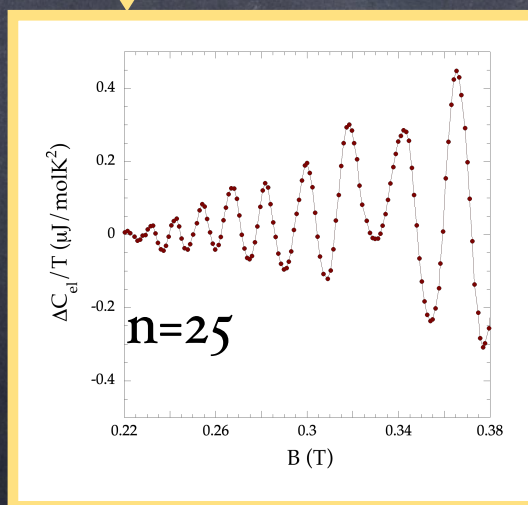


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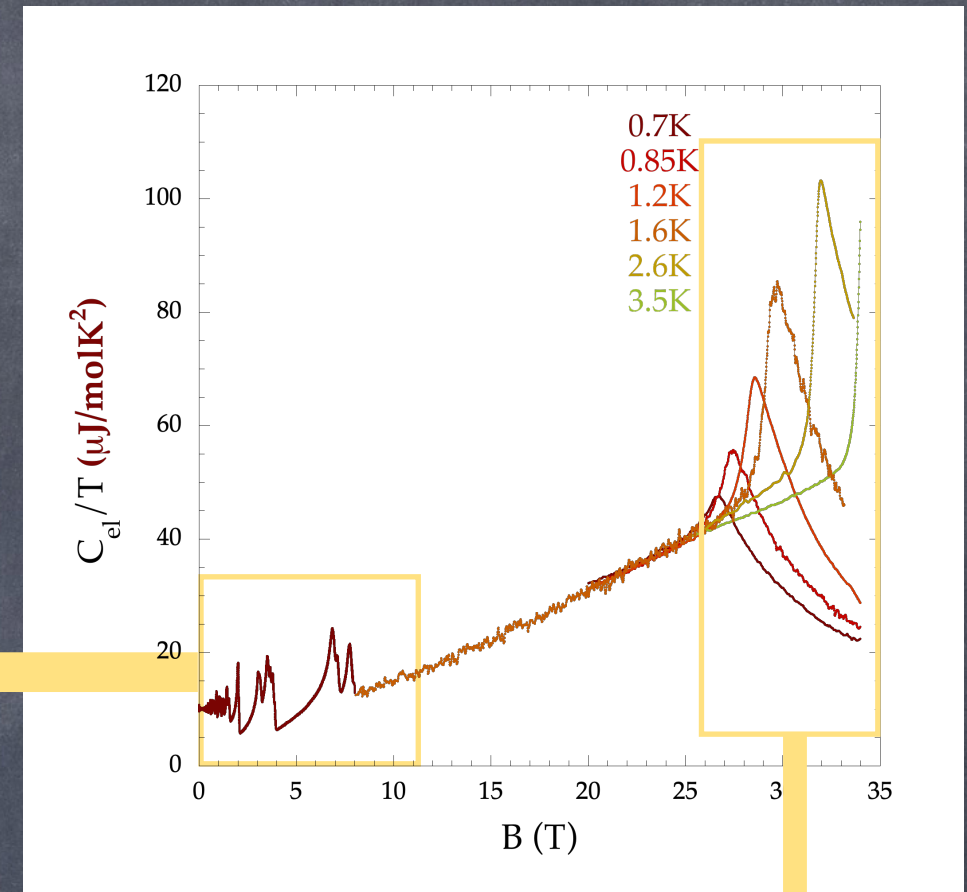
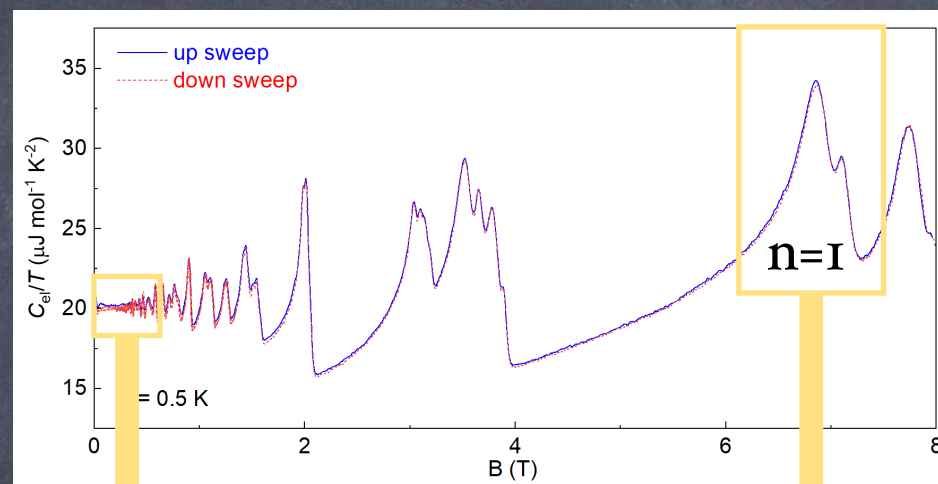


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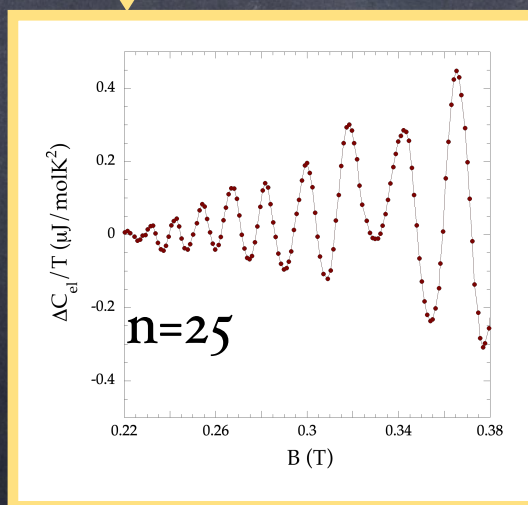


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Note the *splitting* of the peaks  
characteristic of  $C/T$   
measurements  
Zhuo *et al.* Nature Com 2023

Electronic phase  
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# Outline

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Things that we do understand and that we do **NOT** understand on :

- ◎ **The FeSe nematic superconductor**

H-T phase diagram and T & H dependence of the gap structure

- ◎ **Thermodynamic properties of the normal state in cuprates**

Quantum criticality at the onset of the pseudo-gap and charge order



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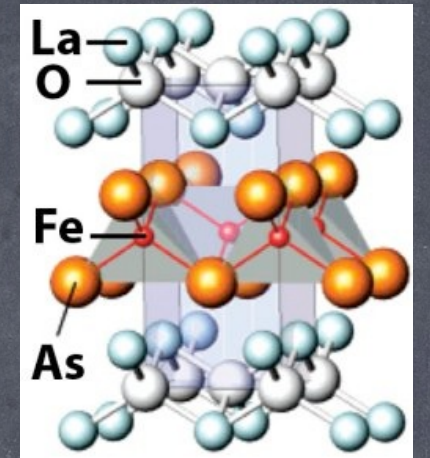
H-T phase diagram and T & H dependence of the gap structure



**FeSe** = **iron based** superconductor

attracted considerable interest due to the interplay between  
superconductivity and magnetism

and  $T_c$  rising up to  $\sim 50\text{K}$  in  $\text{Gd}(\text{O},\text{F})\text{FeAs}$  (so called 1111-phase)

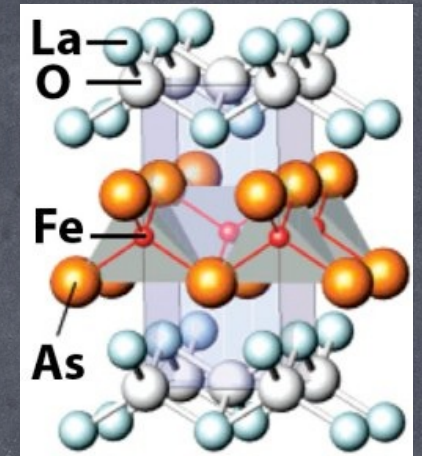




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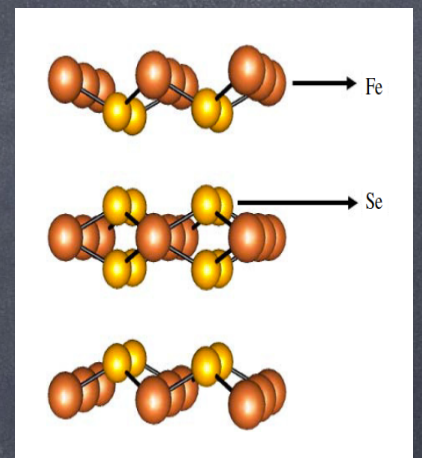


- **FeSe** = c-axis stacking of SC layers **without** any charge reservoir.
- Moderate  $T_c \sim 9\text{K}$ , but **very low carrier concentration**

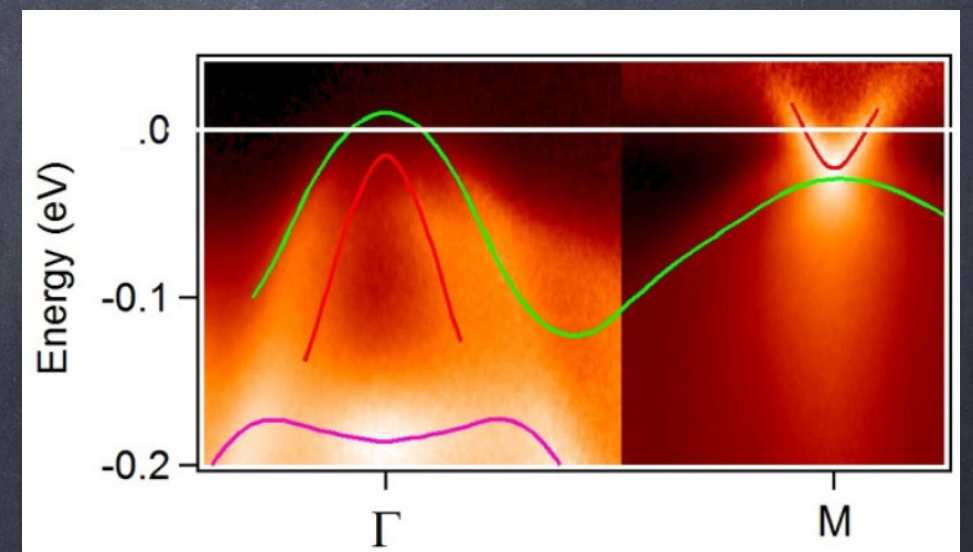
**semi-metal** : small *e+hole pockets*

$E_F \sim \Delta$  : *high*  $T_c$  (two gap-) superconductor

at the verge of a Bose Einstein Condensation



L.Fanfarillo *et al.*, PRB 2016





- interesting **vortex physics**

It all started in the 90s in high  $T_c$  cuprates

⇒ Strong thermal fluctuations

$$G_i = (1/8)(k_B T_c / \epsilon_{\text{cond}})^2 \sim 10^{-2}$$

where  $\epsilon_{\text{cond}} = \epsilon_0 \xi$  with  $\epsilon_0 = \Phi_0^2 / 4\pi\lambda^2$

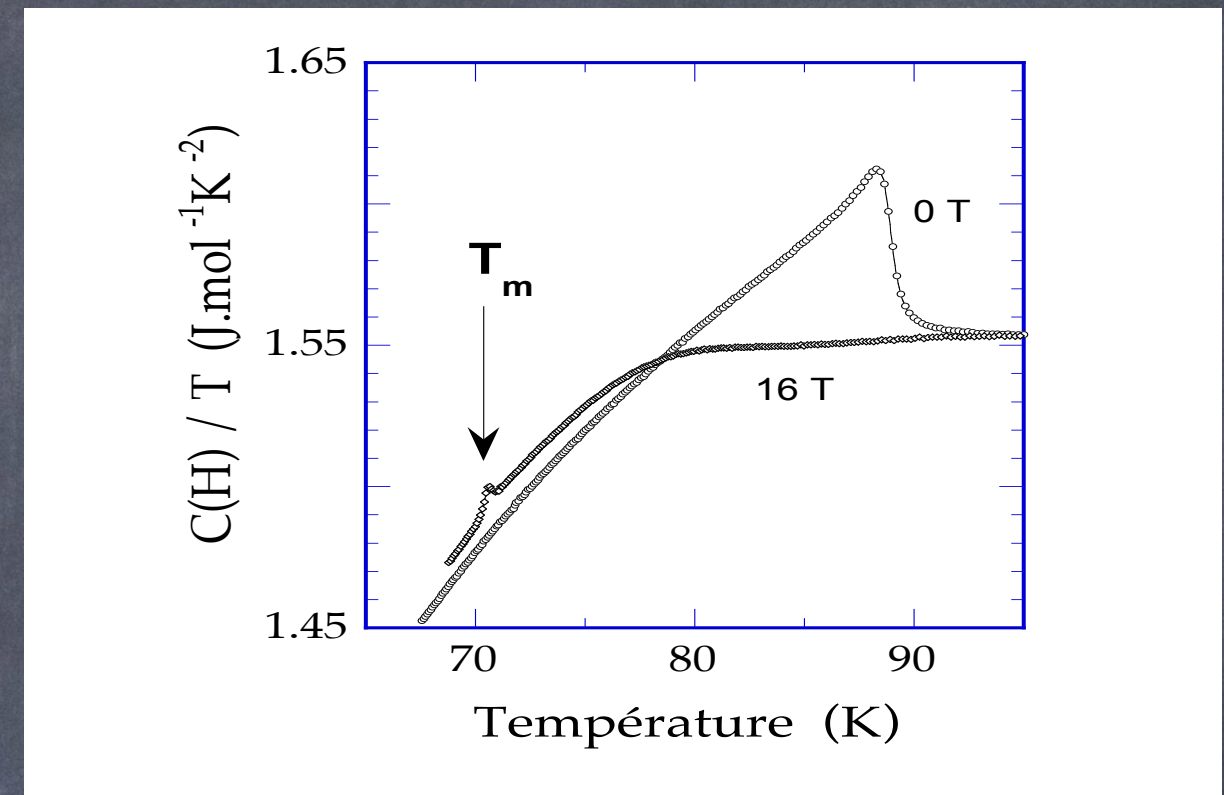
⇒ **melting** of the vortex solid

**Sharp (1<sup>st</sup> order) peak in  $C/T$**

... but observed only in (a few)

high quality optimally doped

YBaCuO single crystals





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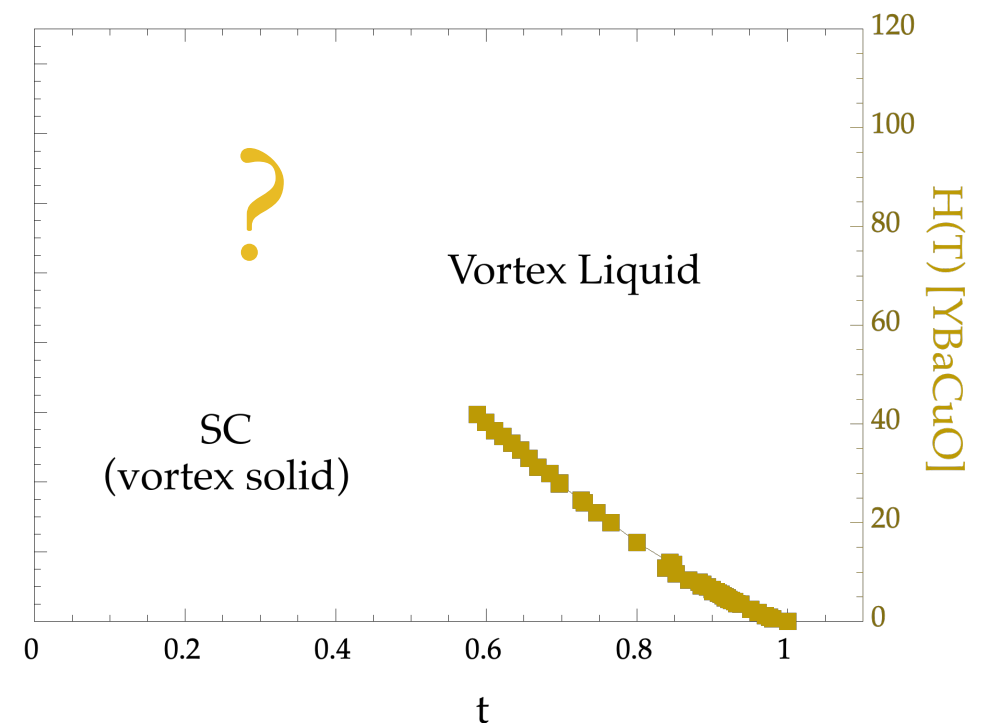
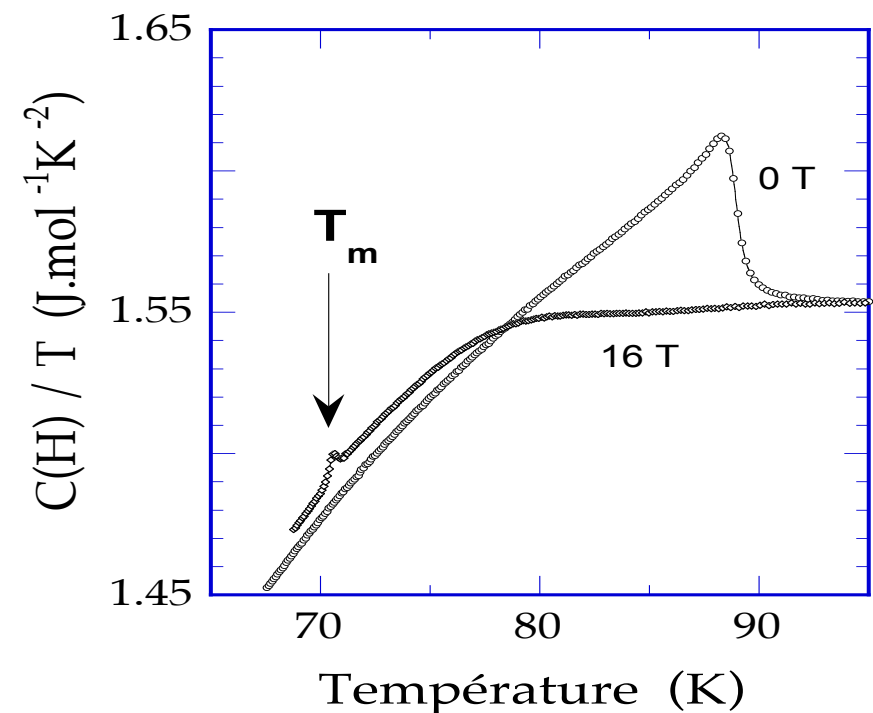
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The melting line can only be  
tracked down to  $\sim T_c/2$





**FeSe** : Small superfluid density

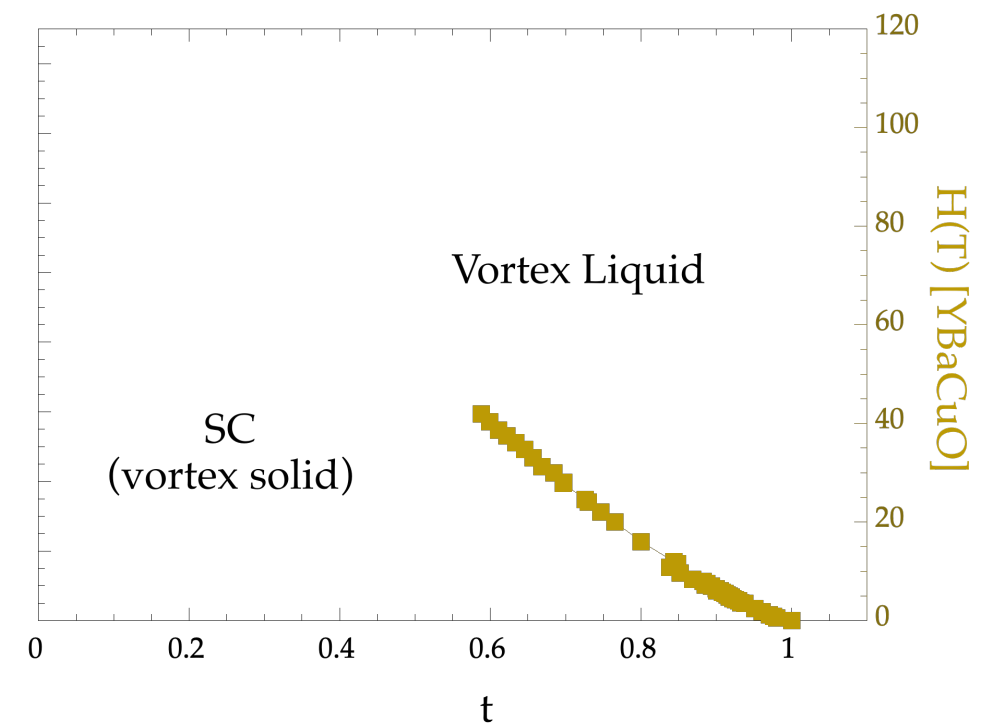
$\Rightarrow$  large  $\lambda$  value

$\Rightarrow$  **Very** small condensation energy

$$\epsilon_{\text{cond}} = \epsilon_0 \xi_c \sim 160 \text{ K}$$

$\Rightarrow$  (still a) **Large Gi value**

	<b>FeSe</b>	Nb	YBaCuO
$T_c$	9	9	92
$\lambda$ (Å)	5000	400	1200
$\epsilon_0$ (K/Å)	8	1200	140
$\xi_c$ (Å)	20	400	4
$\epsilon_{\text{cond}}$ (K)	<b>160 !</b>	$5 \cdot 10^5$	560
Gi	<b><math>10^{-3}</math></b>	$3 \cdot 10^{-9}$	$5 \cdot 10^{-3}$





**FeSe** : Small superfluid density

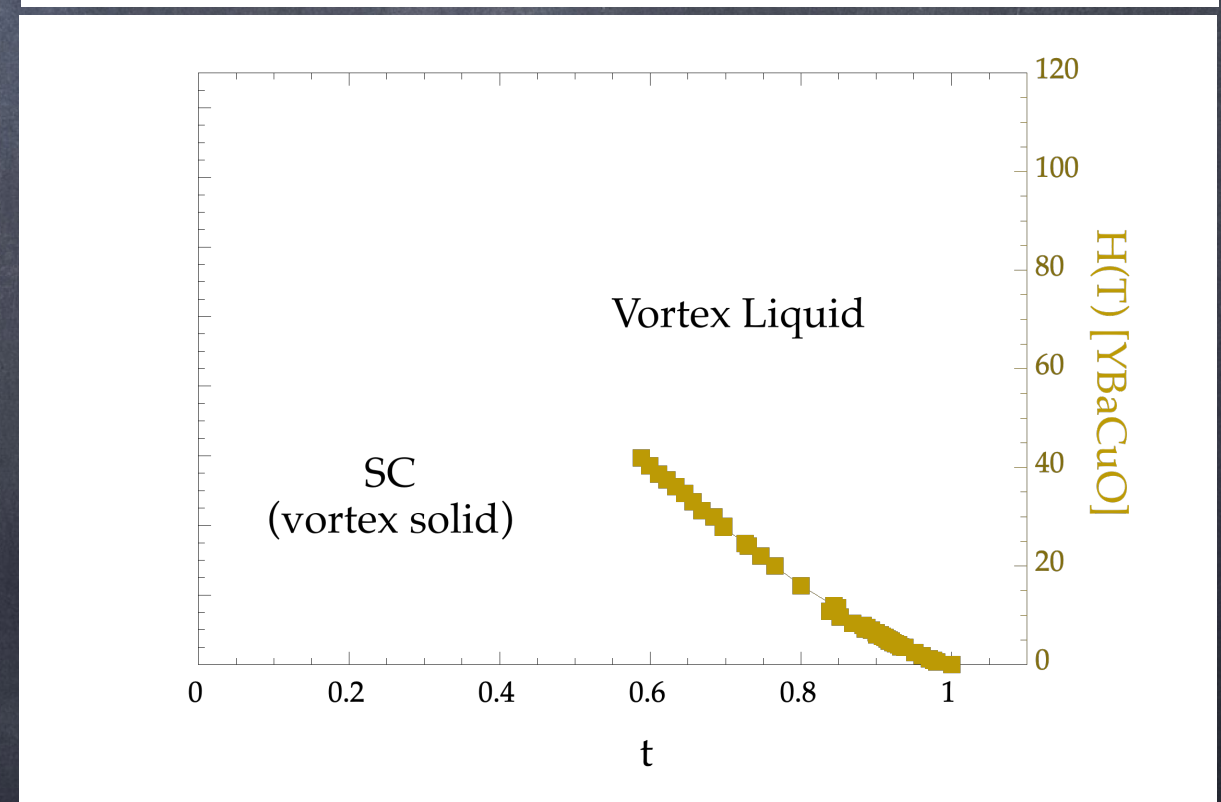
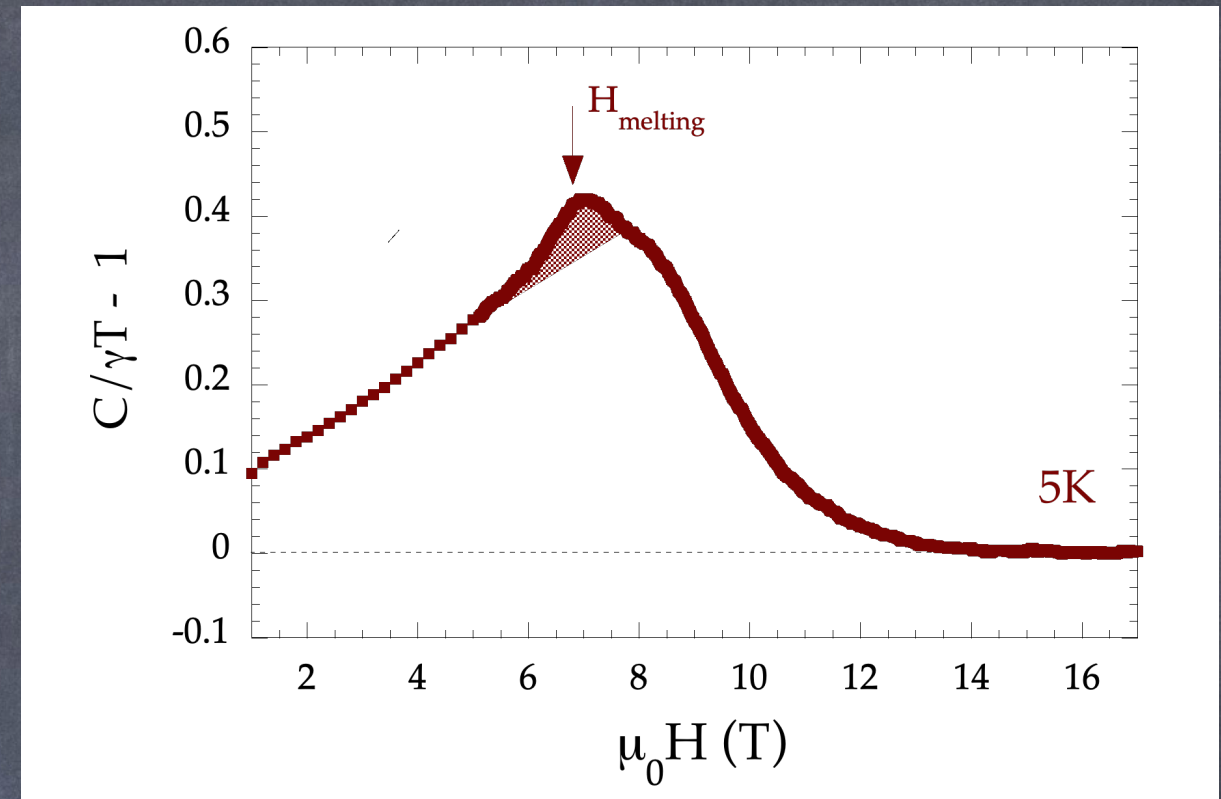
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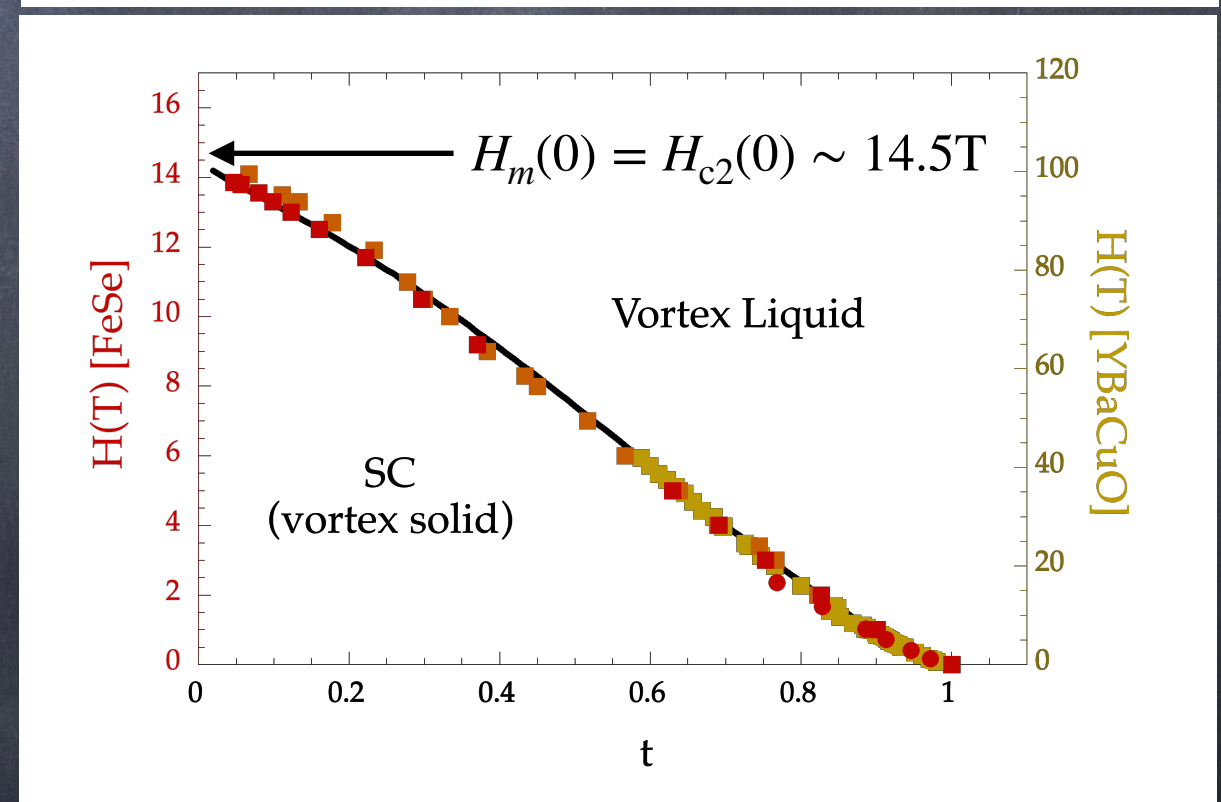
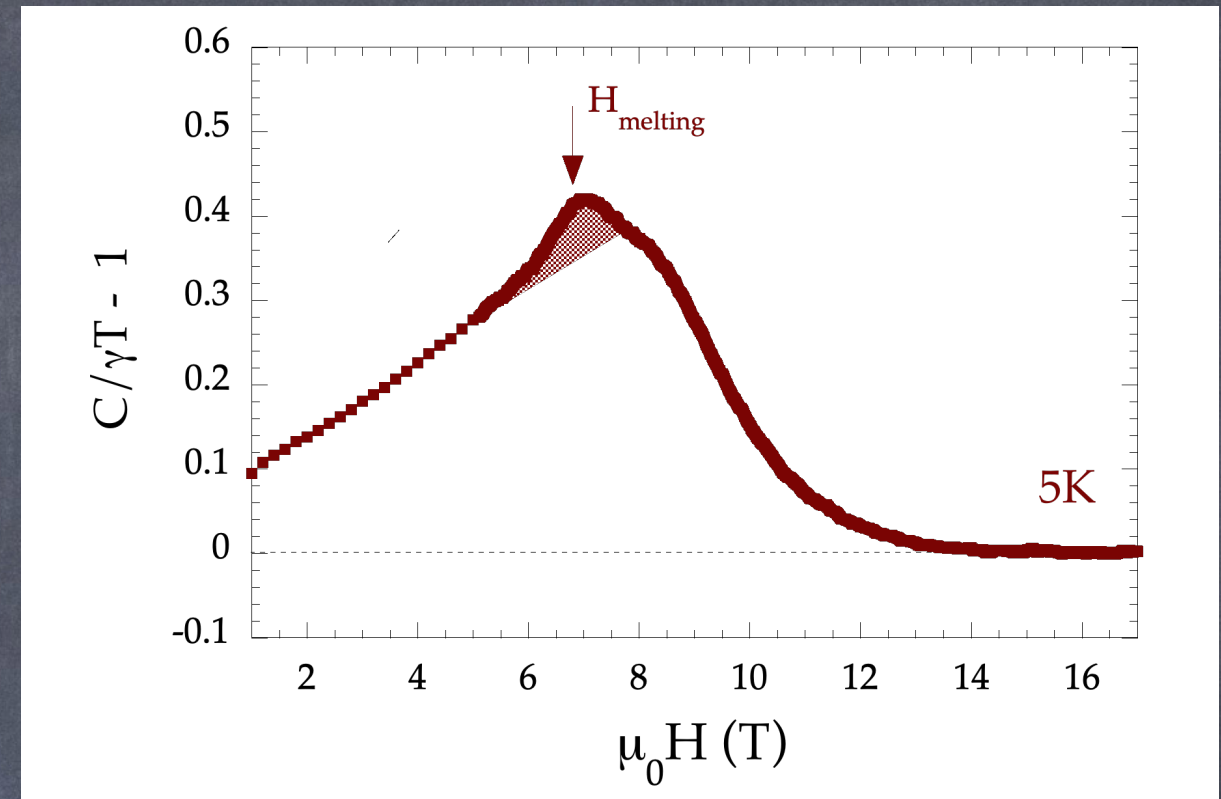
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...which can be studied (and well fitted)

**down to the lowest T**

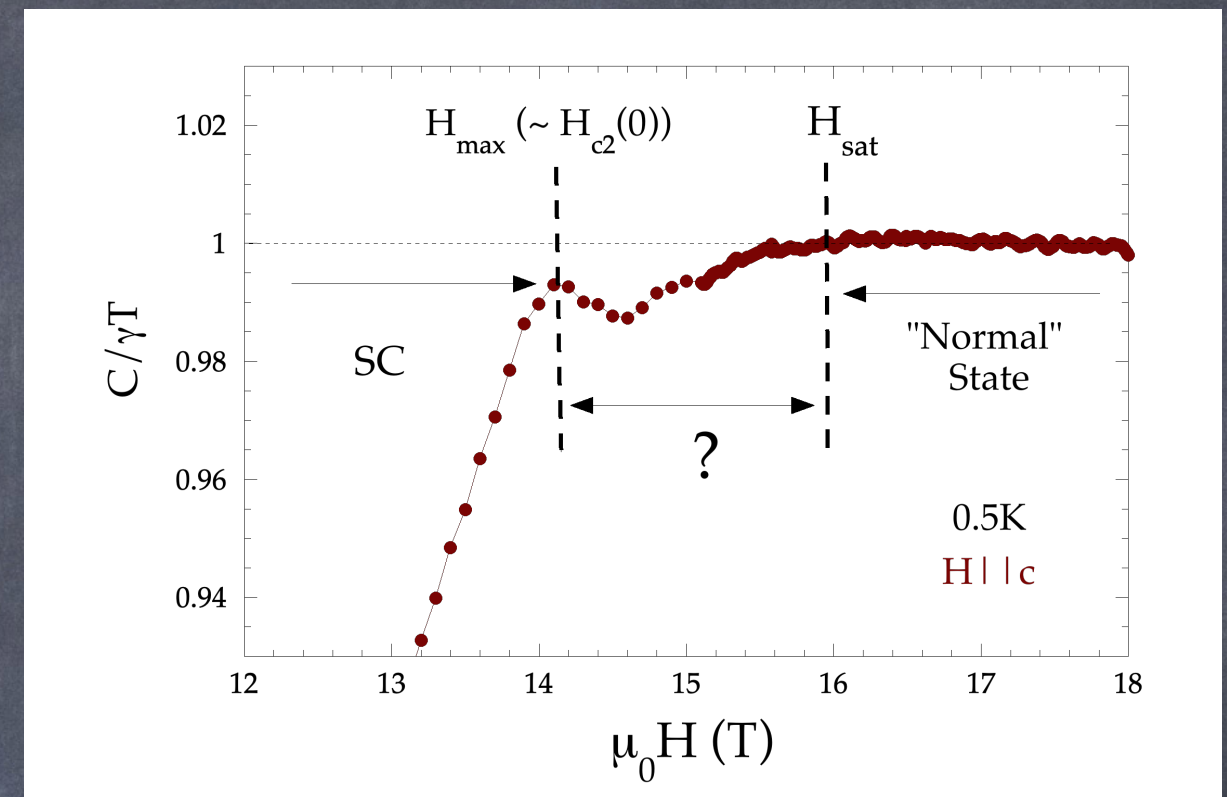
$$(H_{c2}(0) \sim 14.5 \text{ T})$$

(interplay with paramagnetic limit for  $H_{\parallel \text{ab}}$   
see F.Hardy *et al.* PRR 2020)





but  $C/T$  still increases with  $H$   
**well above  $H_{c2}(0)$  ???**  
 and only saturates above  $H_{\text{sat}}$





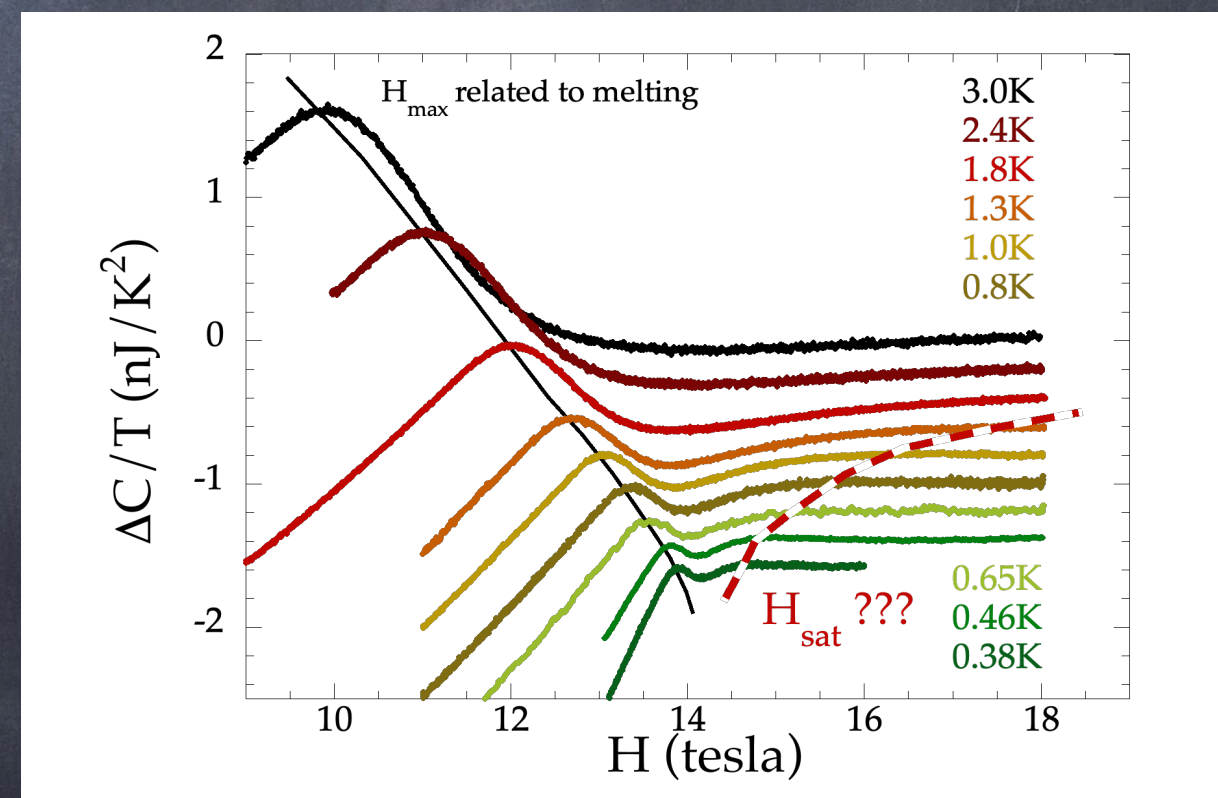
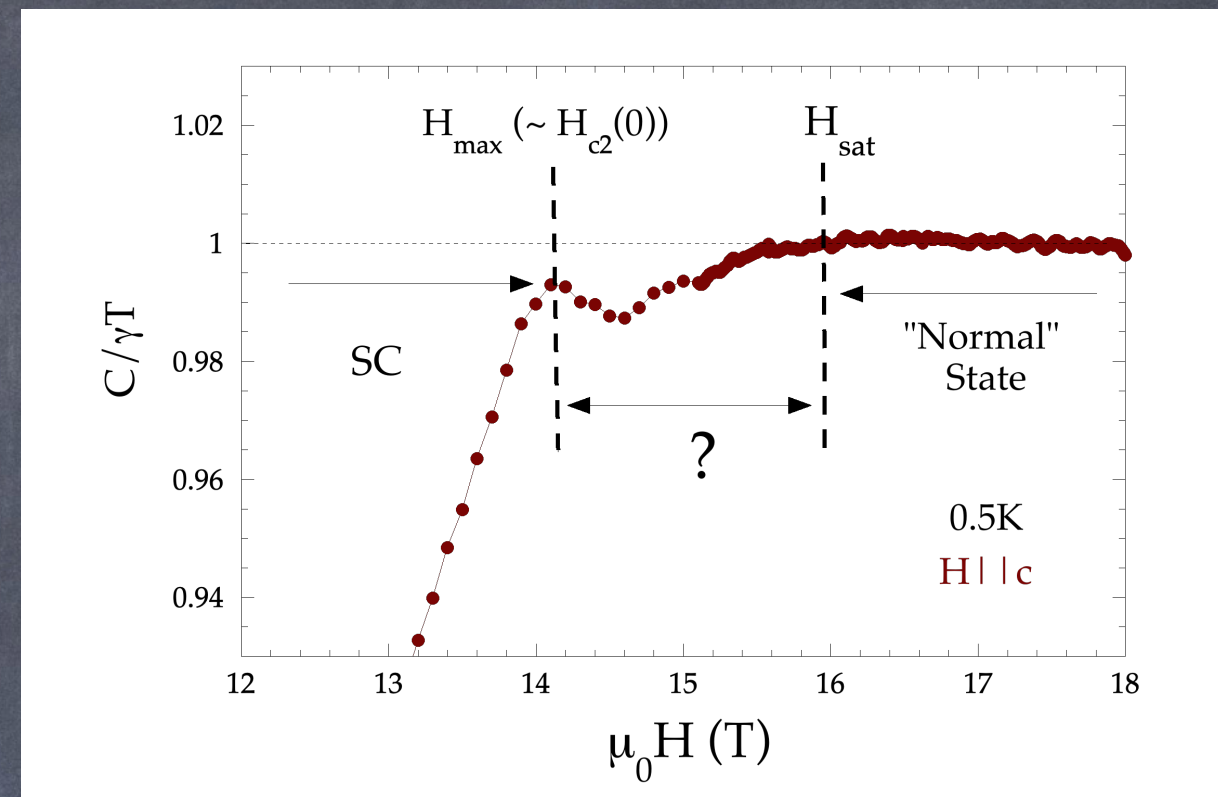
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**Nature of the  $H_{\text{sat}}$  field ?**

increases with  $T$  !

(  $\rightarrow 22 \text{ T} @ 1.8\text{K}$  )

Signature of an electronic transition ?





- No magnetic order (still a structural phase transition)  
but orbitally ordered **nematic state** (breaking of the  $C_4$  symmetry)

Mukherjee *et al.* PRL 2015, Aichhorn *et al.* PRB 2010, Yamakawa *et al.* PRX 2016, Watson *et al.* PRB 2017

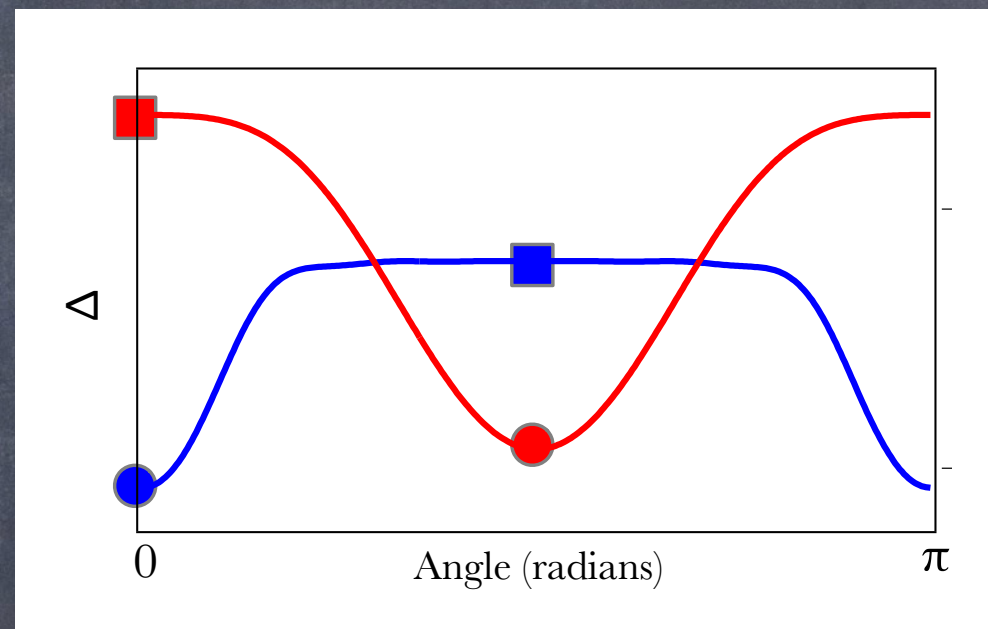
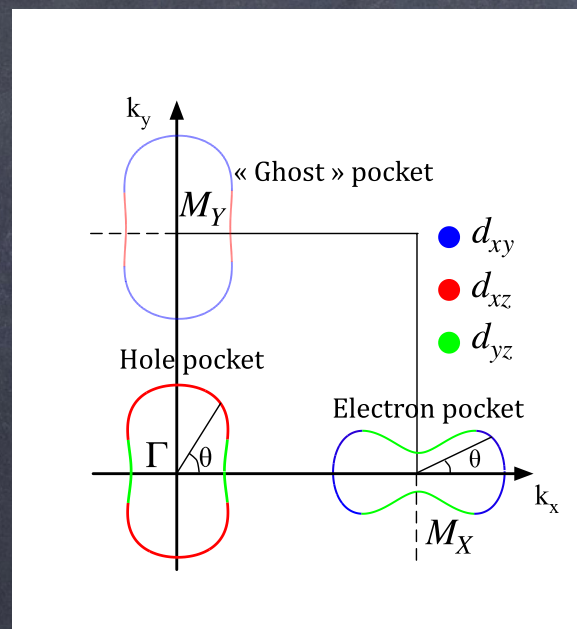


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**C2 anisotropy** of (the spectral weight and) superconducting **gaps**



$$\Delta_{\text{hole}}^{\text{max}} \sim 2 - 3 \text{ meV}$$

$$\Delta_{\text{elec}}^{\text{max}} \sim 1 - 2 \text{ meV}$$

H.Cercellier *et al.*, PRB 2019 and references therein

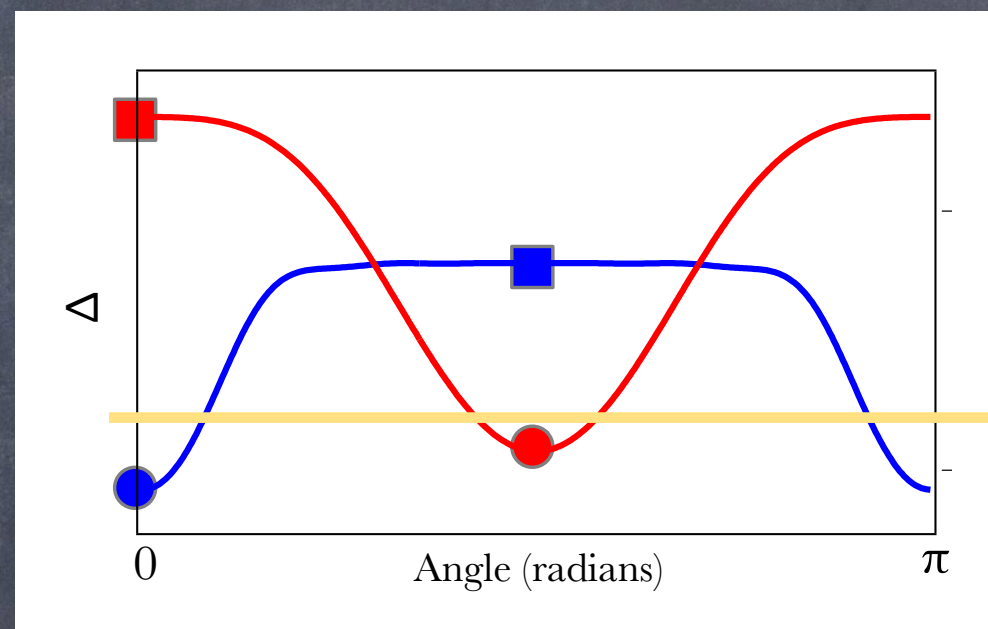
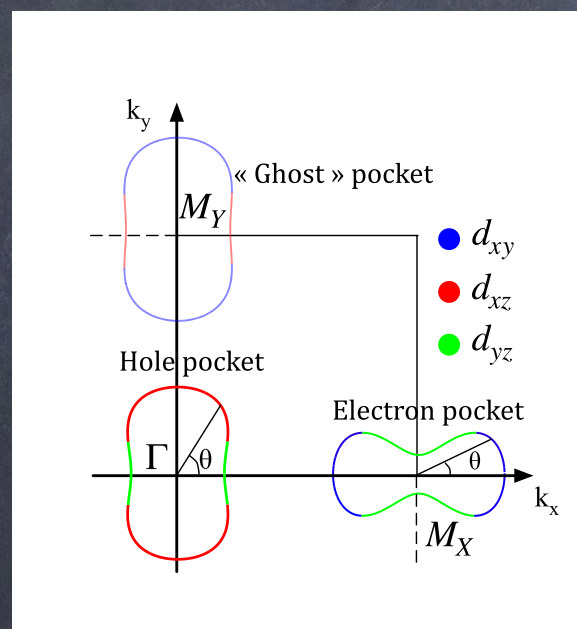


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$$\Delta_{\text{hole}}^{\text{max}} \sim 2 - 3 \text{ meV}$$

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0?

$$\Delta_{\text{hole}}^{\text{min}}, \Delta_{\text{elec}}^{\text{min}} < 0?$$

accidental nodes ?

H.Cercellier *et al.*, PRB 2019 and references therein

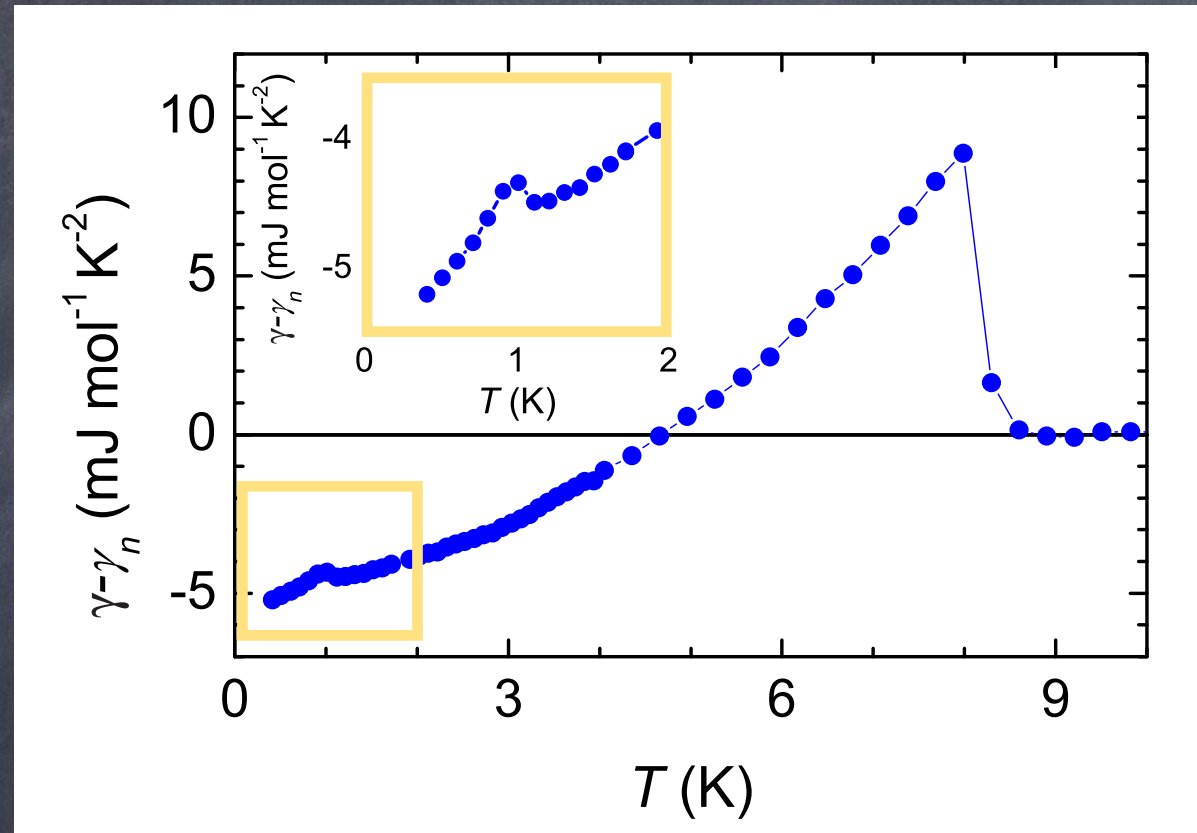
Nematic order couples the s and d wave harmonics of the gap (**s+d symmetry**)

$\Delta_s$  and  $\Delta_d$  sensitive to **nematicity and intra/interband couplings**.

➔ *Accidental* gap nodes can show off if  $\Delta_d > \Delta_s$



Moreover : *anomalous* specific heat anomaly **around 1 K**  
 (but not observed in all samples ?)



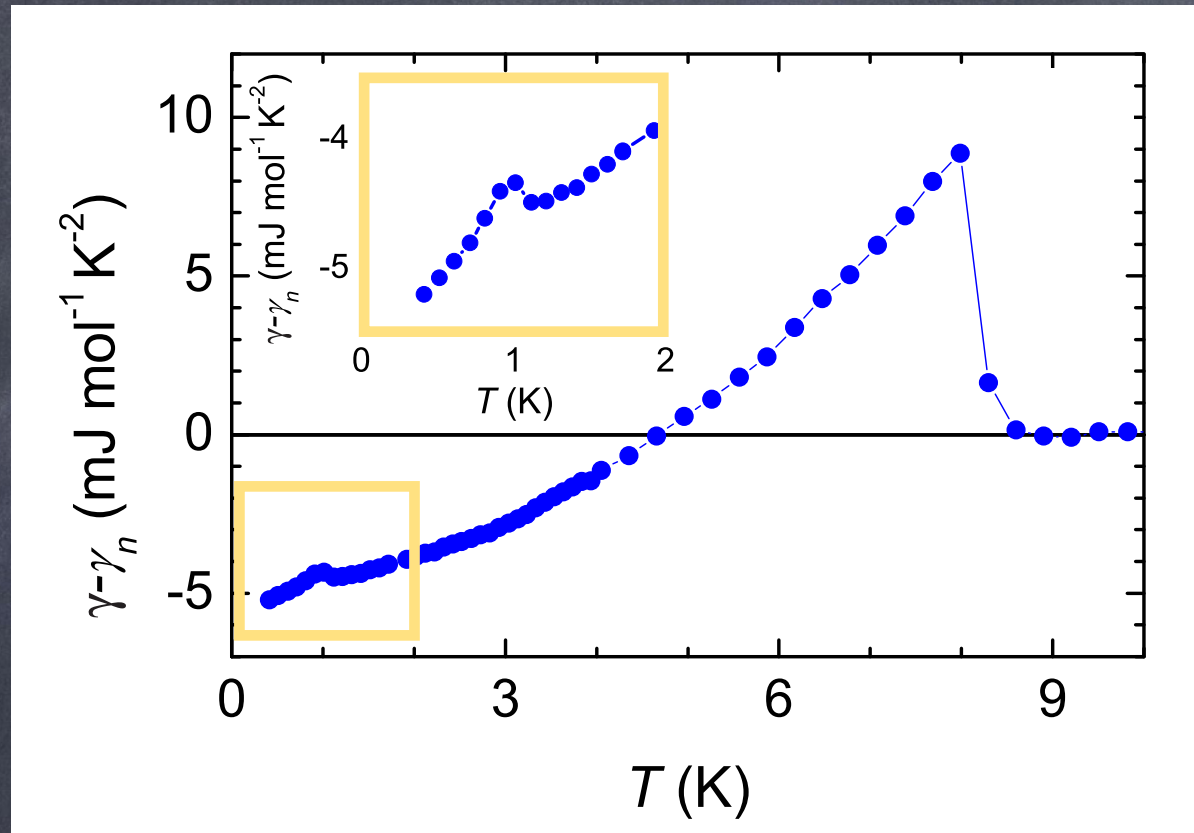
G.Y.Chen *et al.* PRB 2017

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The symmetry of the gap is still an open question  
 which can be probed by specific heat measurement  
 in **rotating** Hllab (Oxy plane)



DOS (=C) maxima when Doppler shift :  $\vec{v}_s \cdot \vec{k}_F \sim \Delta$

velocity of vortex screening  
current = rotating field

(anisotropy of)  
electronic structure

anisotropy of the  
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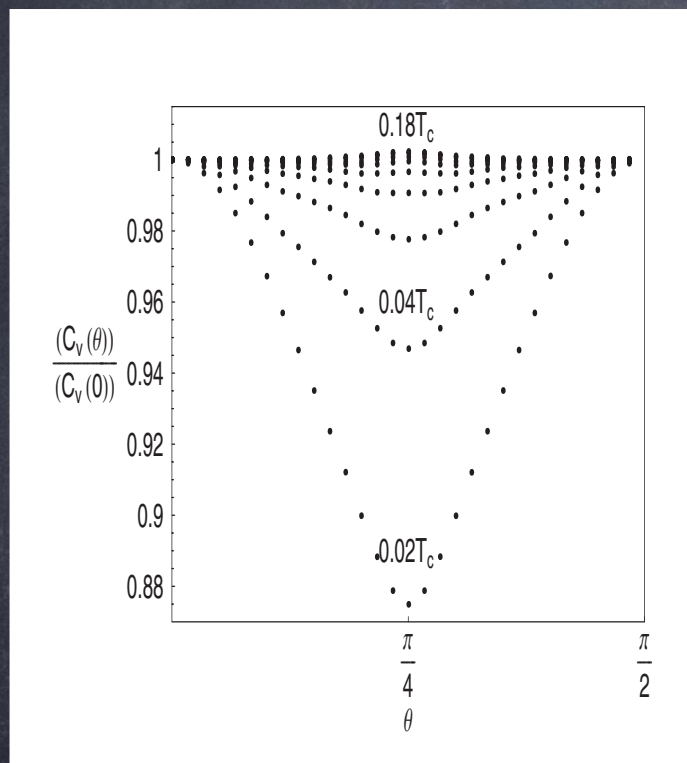


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However  
 $\Delta C/\gamma T < 1\%$   
above  $T_c/10$

and  $\pi/4$ -shift  
(min  $\iff$  max)  
for  $T \sim T_c/10$

**Numerical calculations**

d-wave gap

G.R.Boyd *et al.* PRB 2009

(see also Vorontsov *et al.* PRB 2007)



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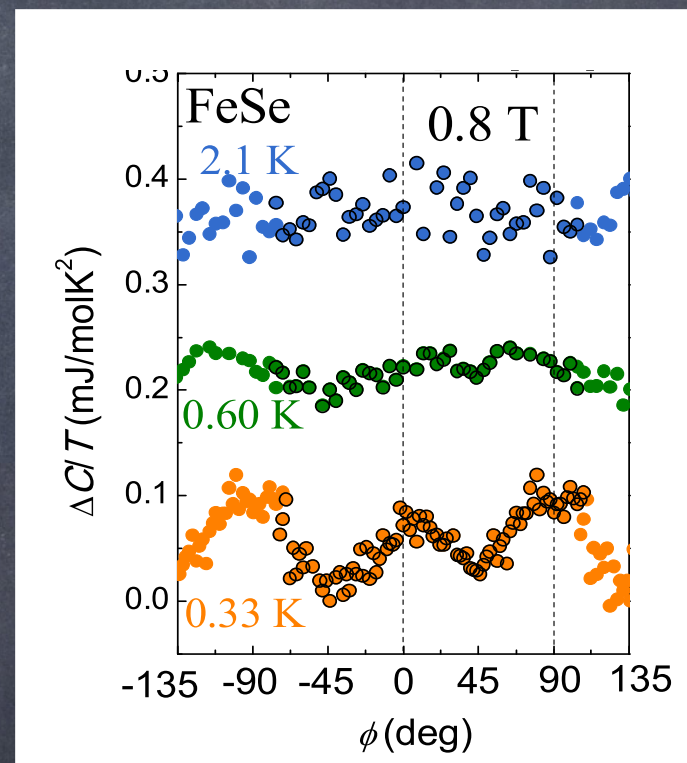
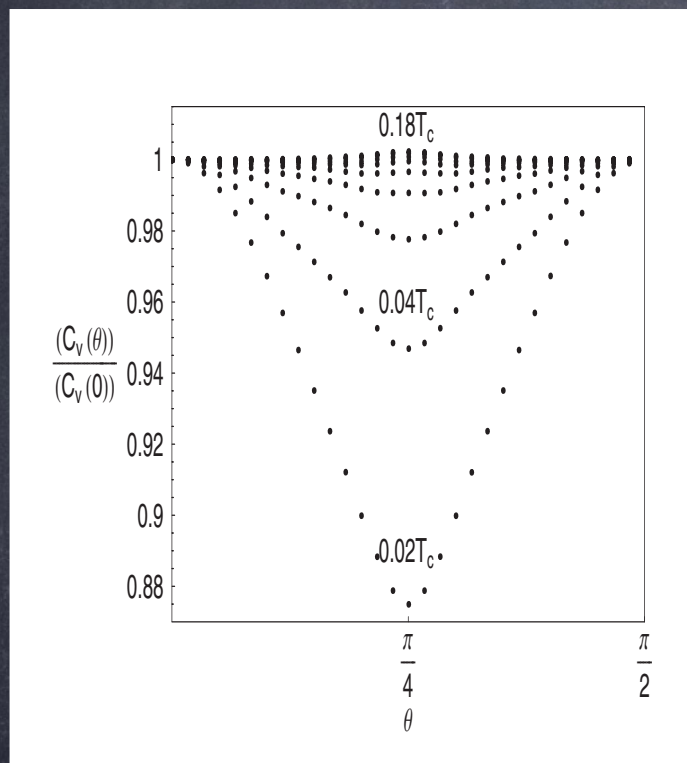
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Observed in FeSe  
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Sun *et al.* PRB 2017

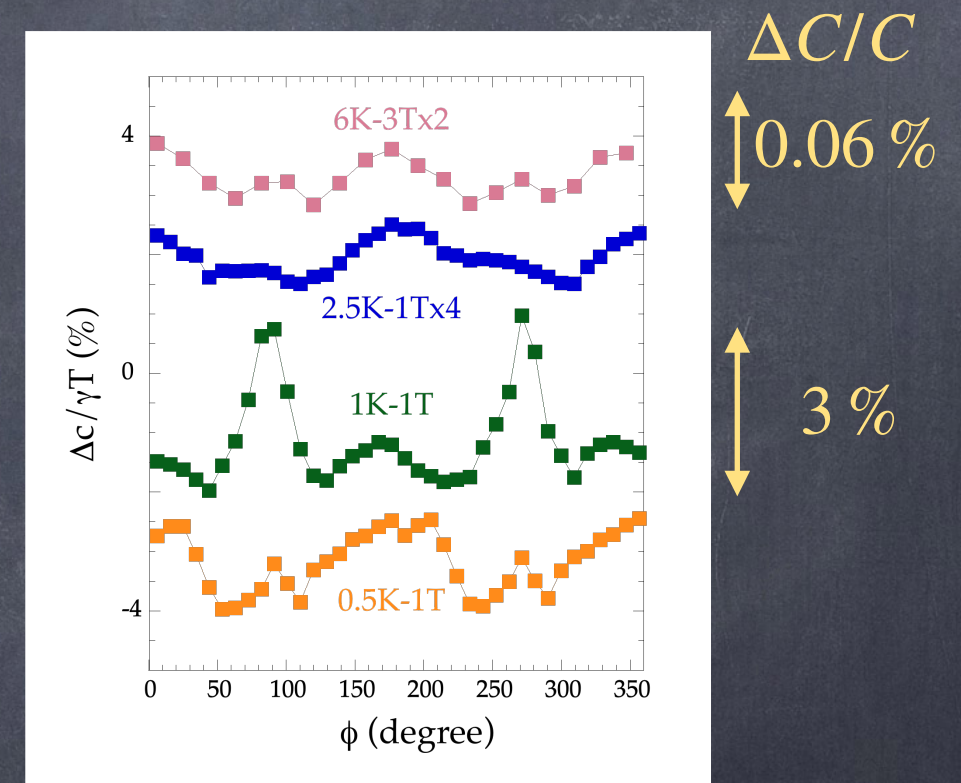
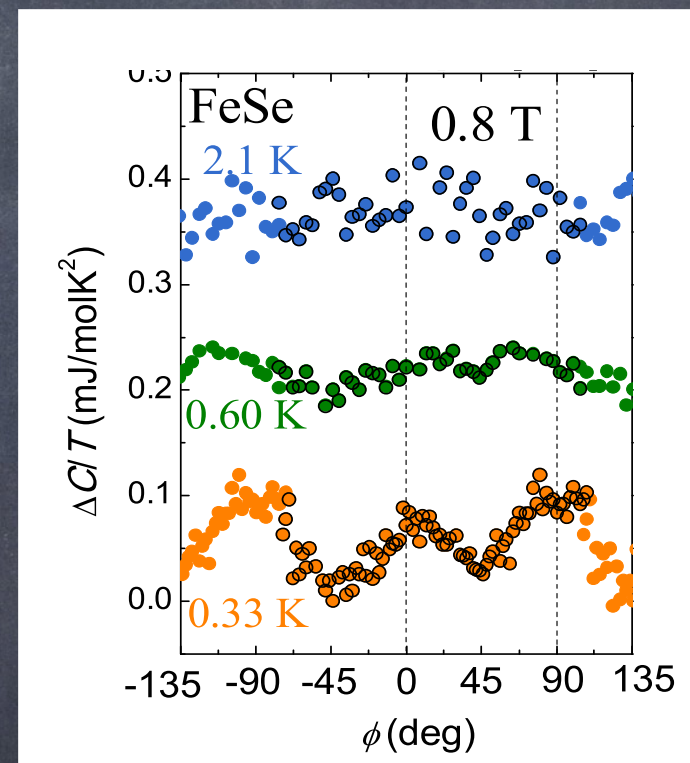
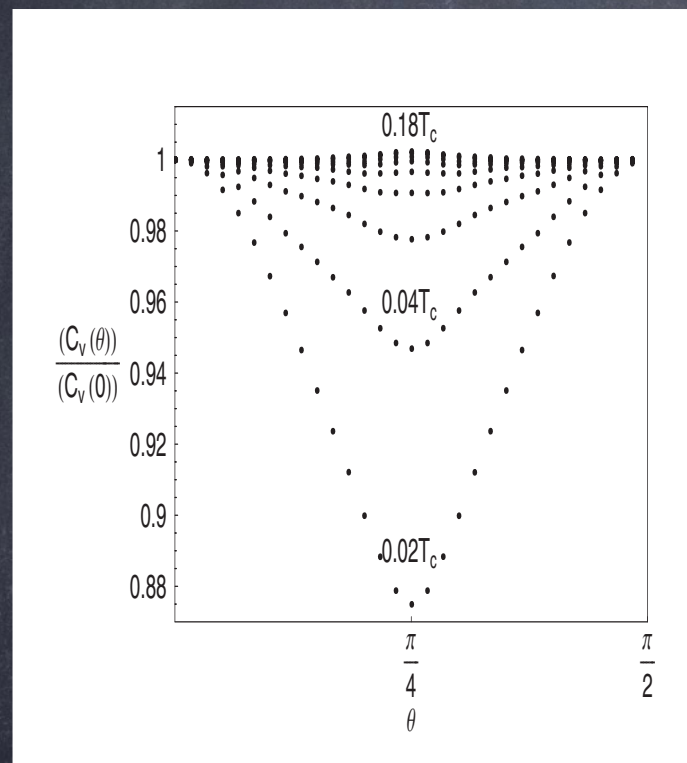


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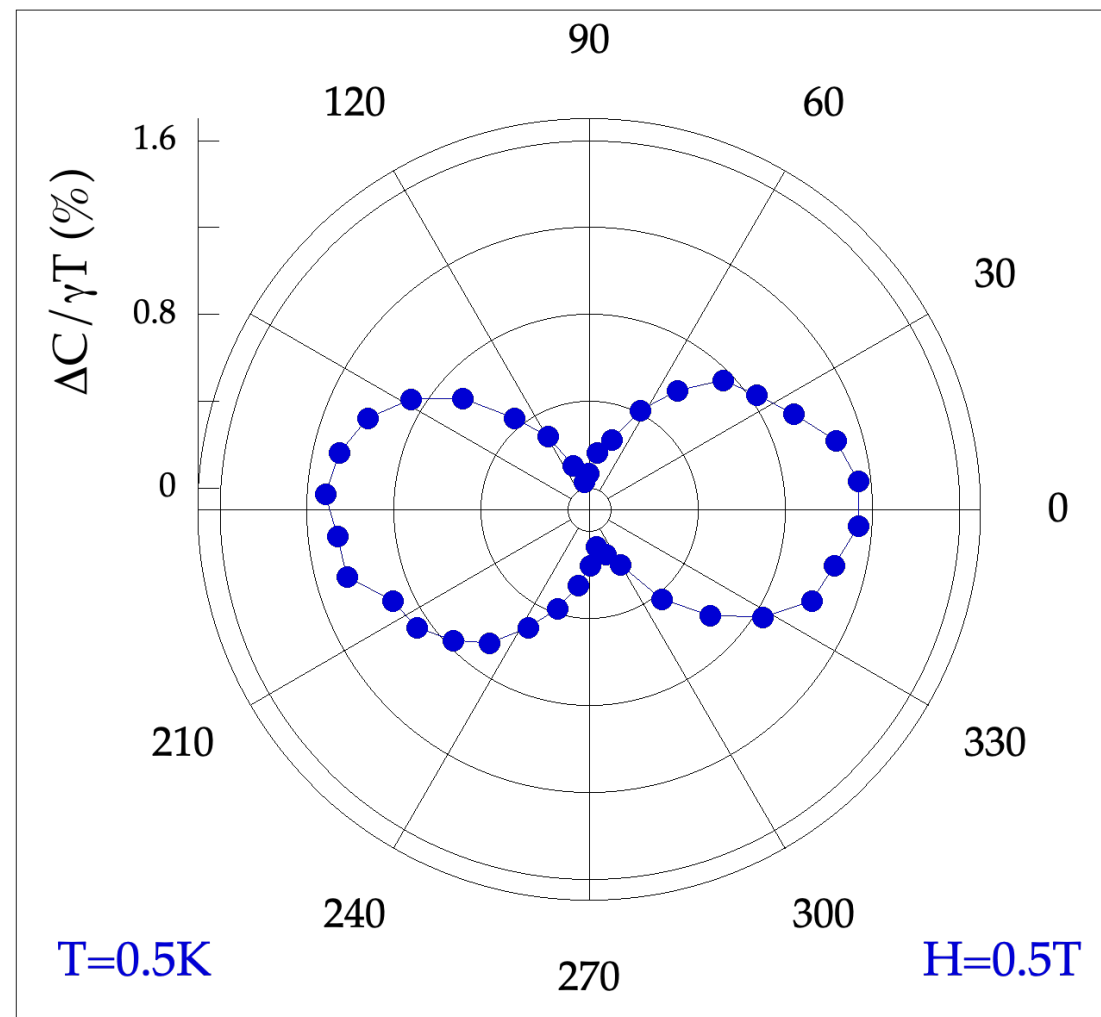
Observed in FeSe  
**up to 6K and/or 6T**  
AC measurements



**twofold (C<sub>2</sub>) symmetry**

at low T/low H

= nematic character of FeSe  
from thermodynamic data





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Good **quantitative** agreement  
with numerical calculations

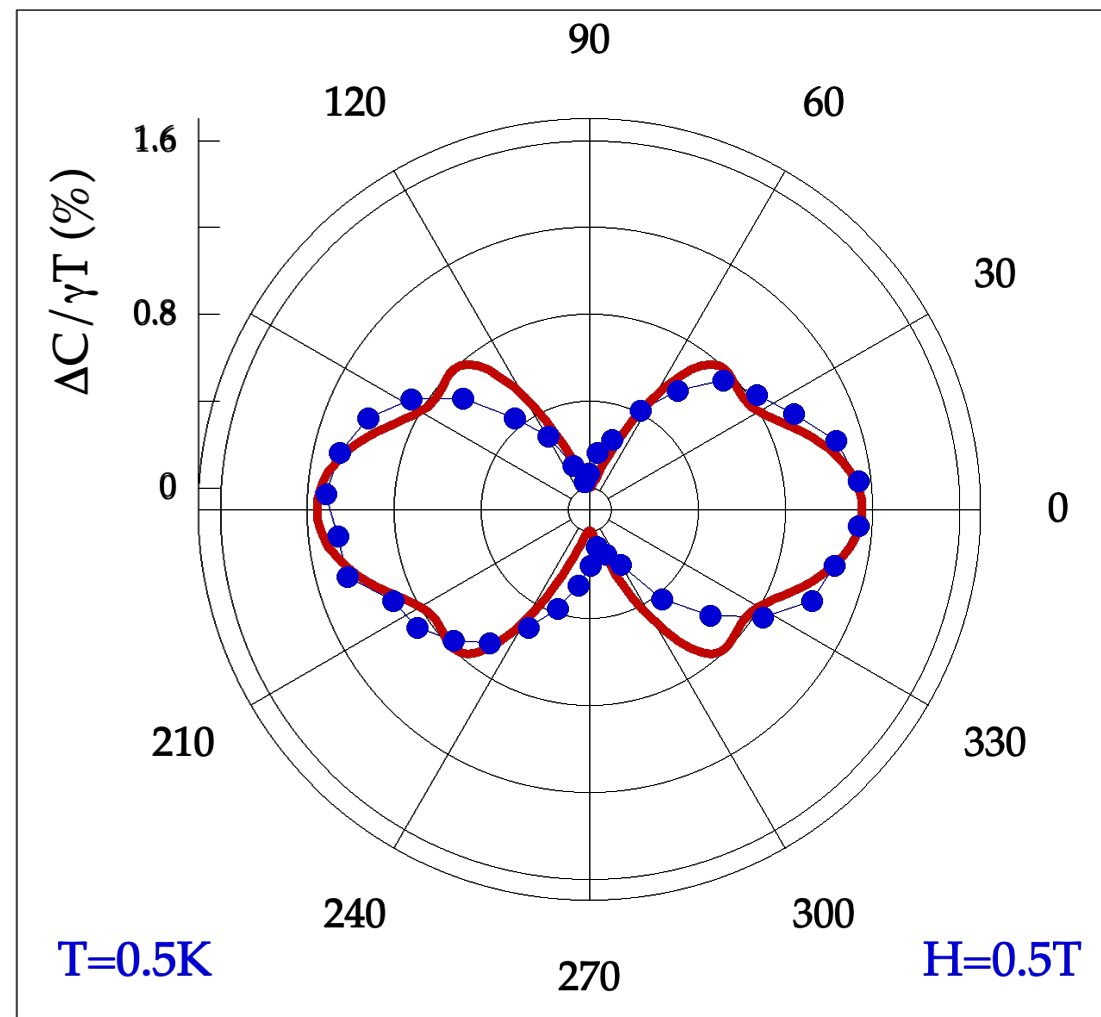
**(H.Cercellier)**

$$\Delta_{\text{hole}}^{\text{max}} \sim 2\text{meV}$$

$$\Delta_{\text{elec}}^{\text{max}} \sim 1\text{meV}$$

in very reasonable agreement with other measurements

H.Cercellier *et al.*, PRB 2019





**twofold (C<sub>2</sub>) symmetry**

at low T/low H

= nematic character of FeSe  
from thermodynamic data

Good **quantitative** agreement  
with numerical calculations

**(H.Cercellier)**

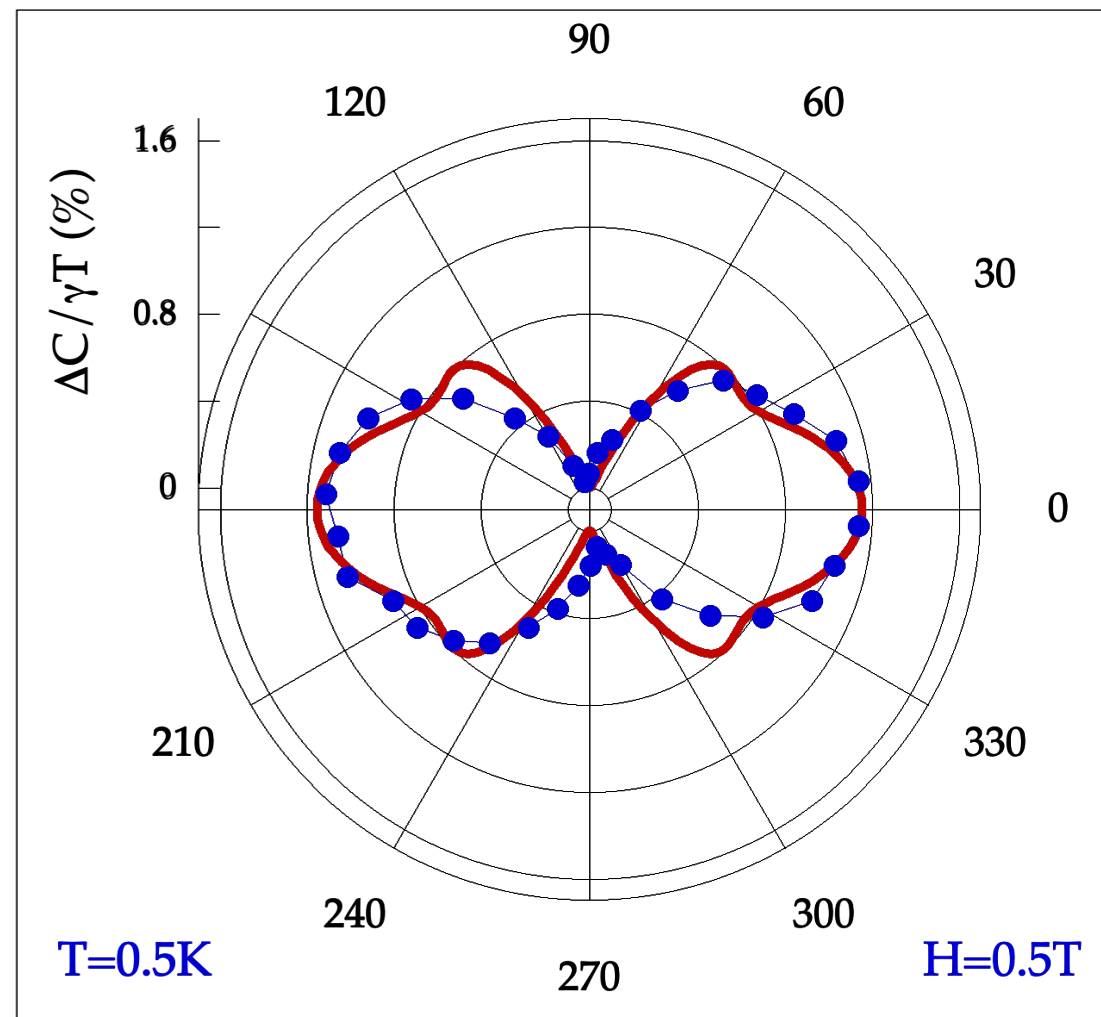
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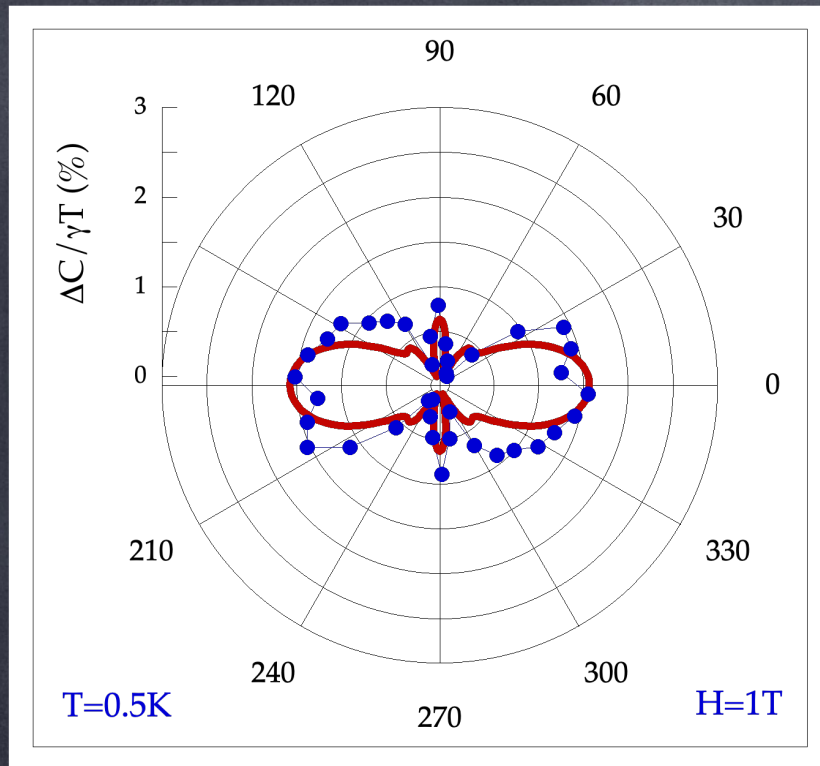
H.Cercellier *et al.*, PRB 2019

but *exotic* temperature and field dependence of  
the gap structure !...





increasing temperature

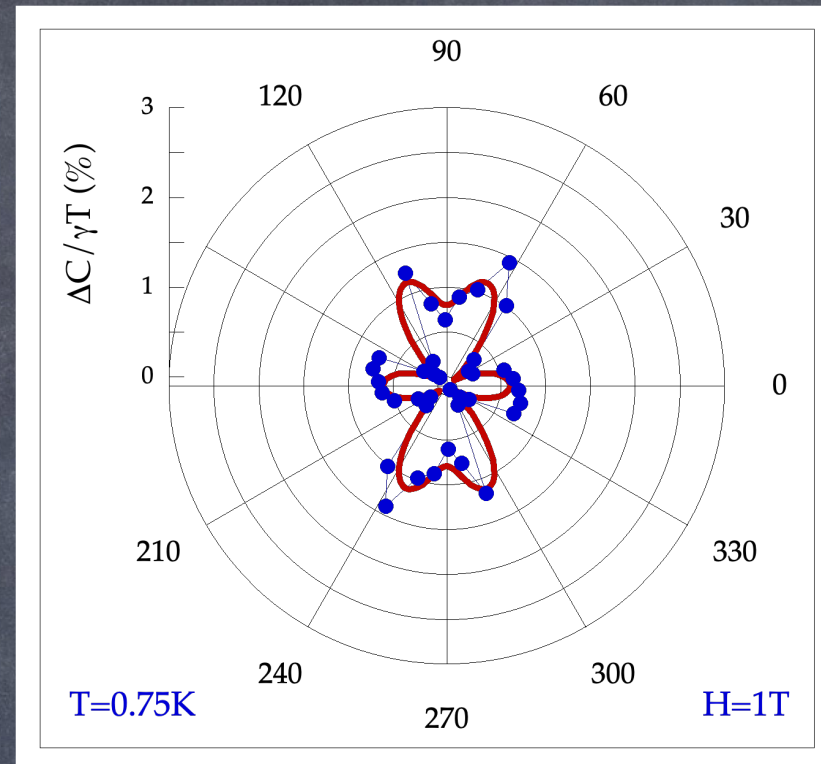
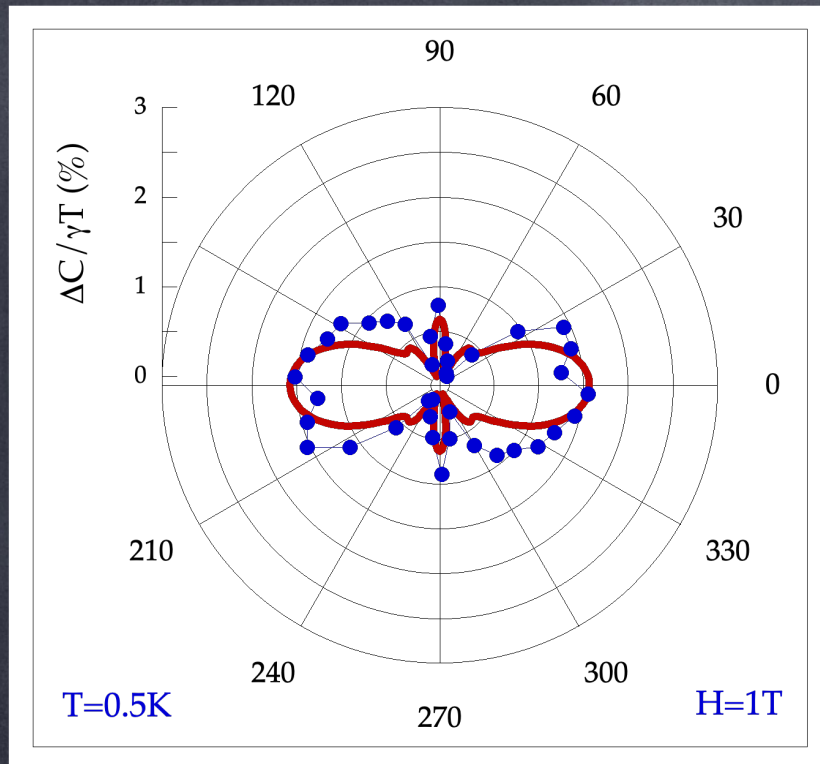


$$\Delta_{\text{hole}}^{\text{max}} \sim 2\text{meV}$$

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increasing temperature



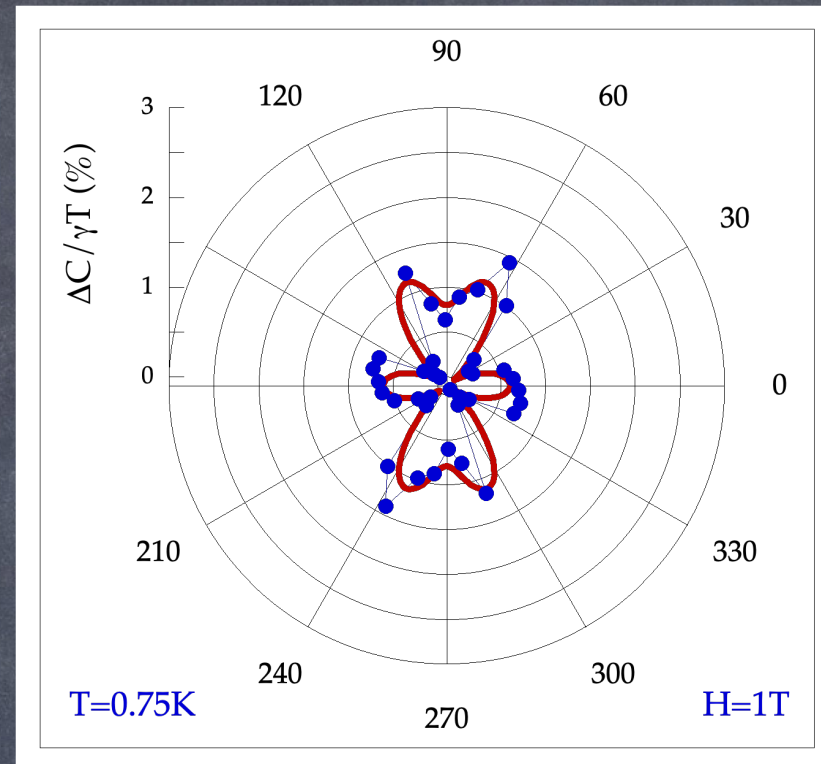
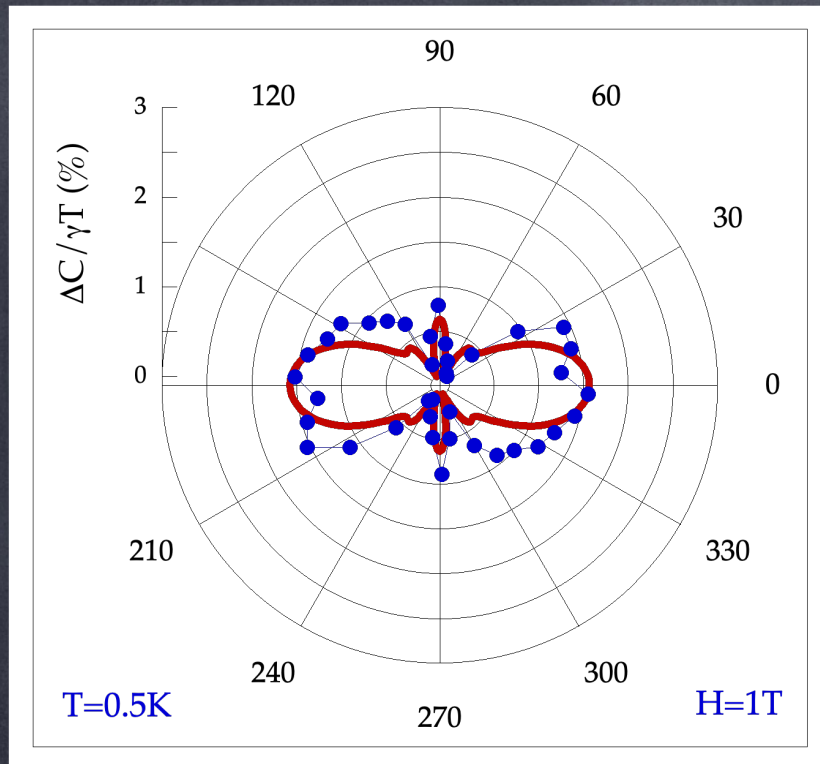
intriguing «butterfly»  
structure

$$\Delta_{\text{hole}}^{\text{max}} \sim 2\text{meV}$$

$$\Delta_{\text{elec}}^{\text{max}} \sim 1\text{meV}$$



increasing temperature →



$$\Delta_{\text{hole}}^{\text{max}} \sim 2\text{meV}$$

$$\Delta_{\text{elec}}^{\text{max}} \sim 1\text{meV}$$

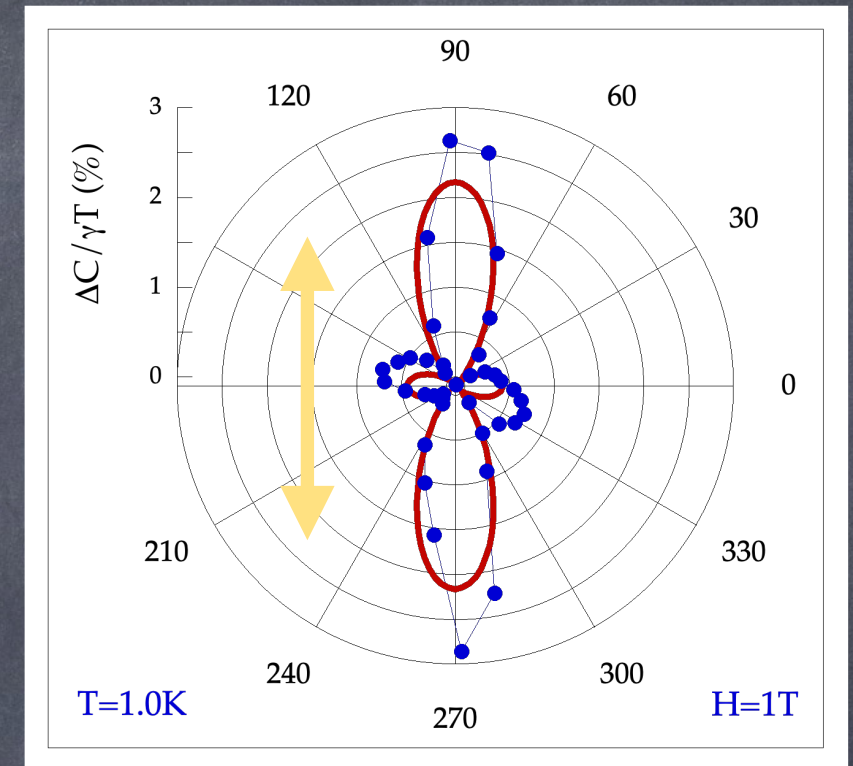
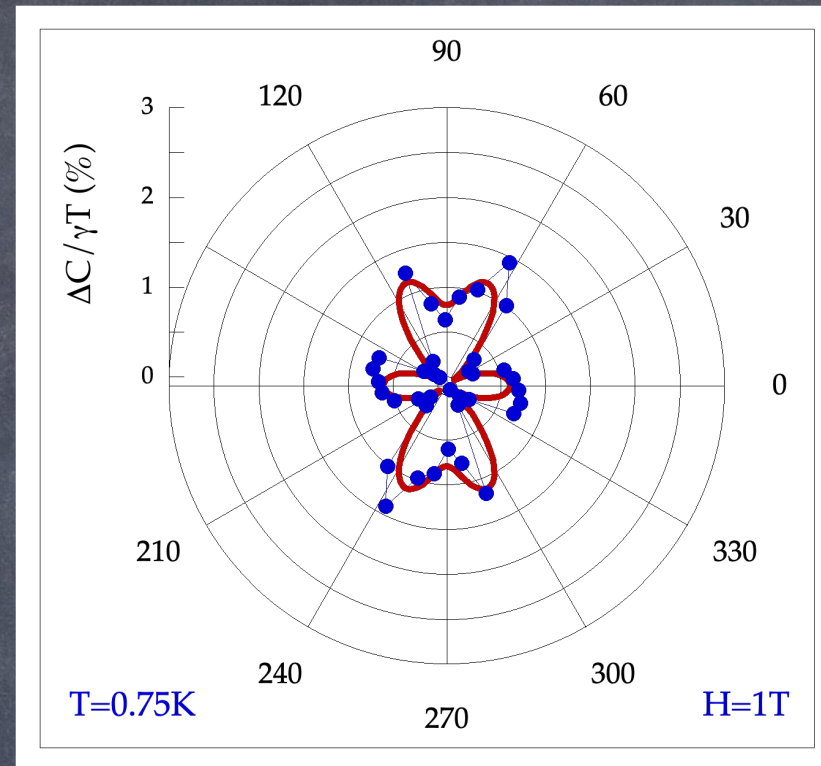
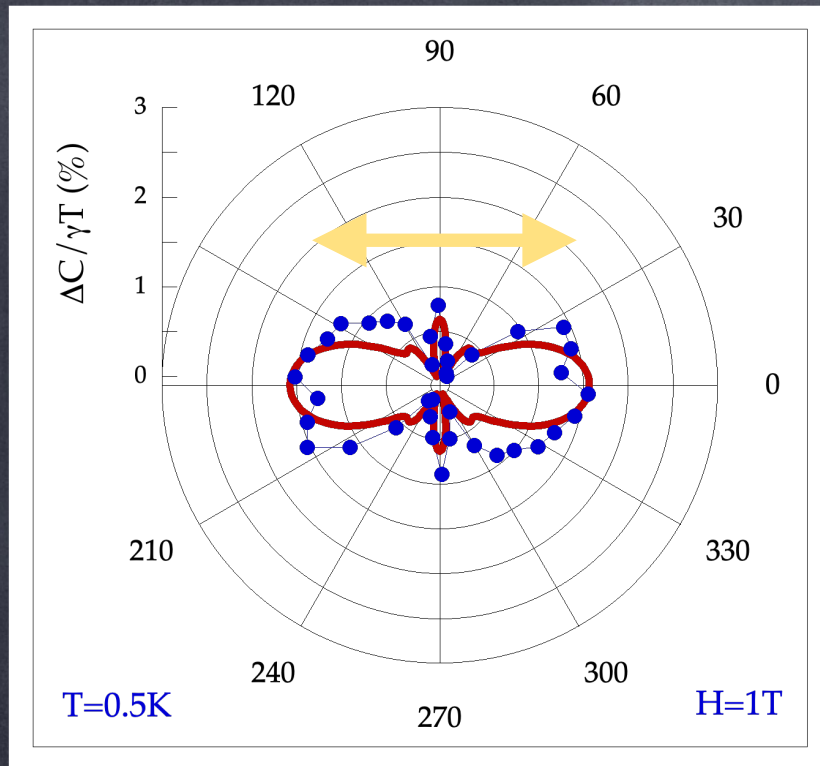
intriguing «butterfly»  
structure

characteristic of  
accidental nodes

$$\Delta_{\text{hole}}^{\text{min}} \sim \Delta_{\text{elec}}^{\text{min}} \sim -0.2\text{meV}$$



increasing temperature



$$\Delta_{\text{hole}}^{\text{max}} \sim 2\text{meV}$$

$$\Delta_{\text{elec}}^{\text{max}} \sim 1\text{meV}$$

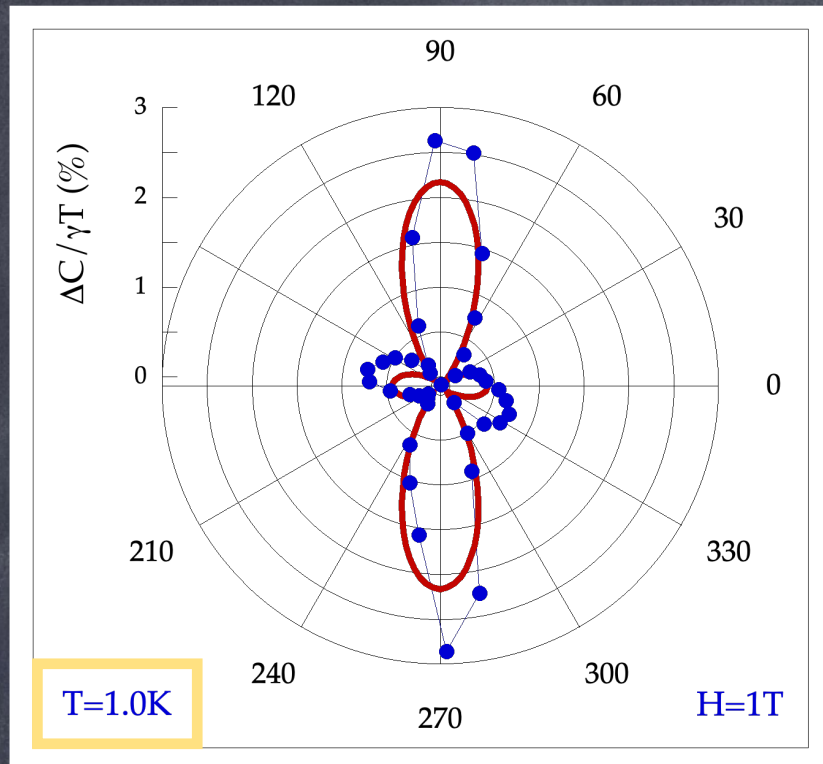
intriguing «butterfly»  
structure  
characteristic of  
**accidental nodes**

$\pi/2$ –shift of the  
symmetry axis  
(for  $T \sim T_c/10$ )  
also well reproduced

$$\Delta_{\text{hole}}^{\text{min}} \sim \Delta_{\text{elec}}^{\text{min}} \sim -0.2\text{meV}$$



increasing temperature



$$\Delta_{\text{hole}}^{\text{max}} \sim 2\text{meV}$$

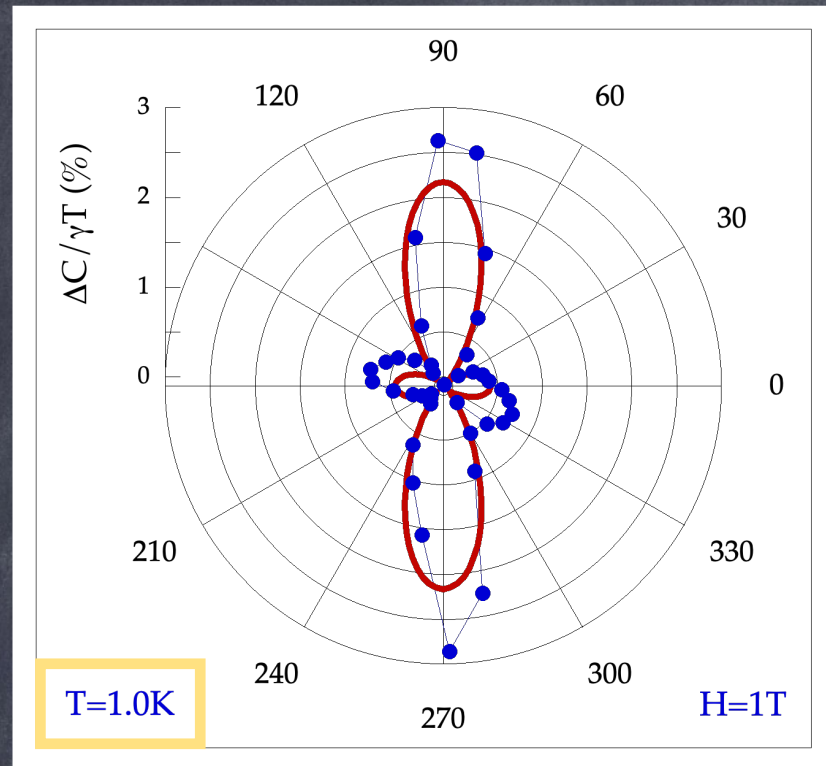
$$\Delta_{\text{hole}}^{\text{min}} \sim -0.2\text{meV}$$

$$\Delta_{\text{elec}}^{\text{max}} \sim 1\text{meV}$$

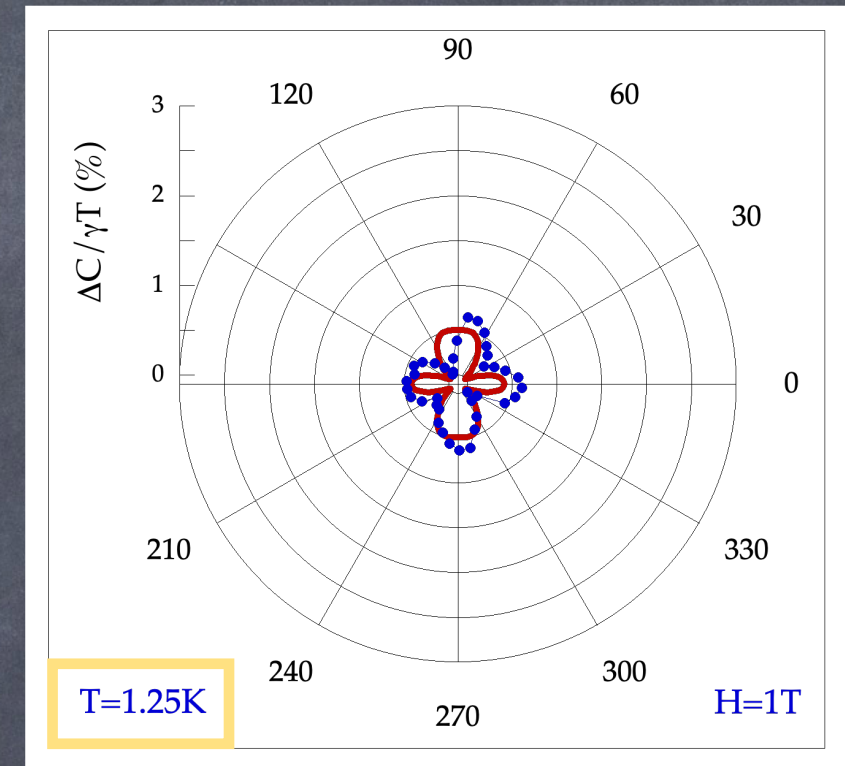
$$\Delta_{\text{elec}}^{\text{min}} \sim -0.2\text{meV}$$



increasing temperature →



but  
drastic drop  
of the  
amplitude  
above 1K ?



$$\Delta_{\text{hole}}^{\text{max}} \sim 2\text{meV}$$

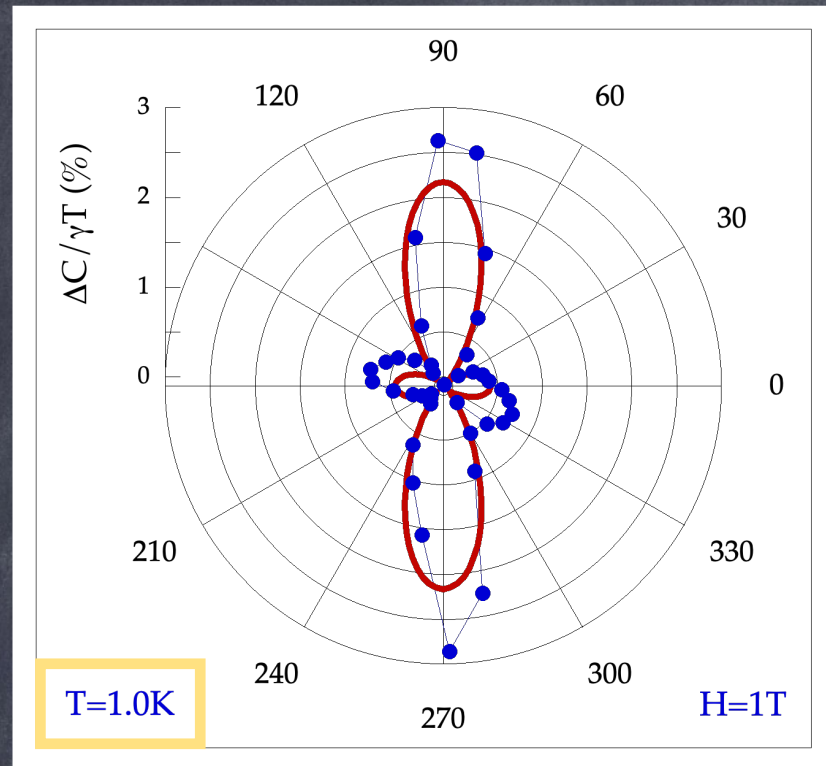
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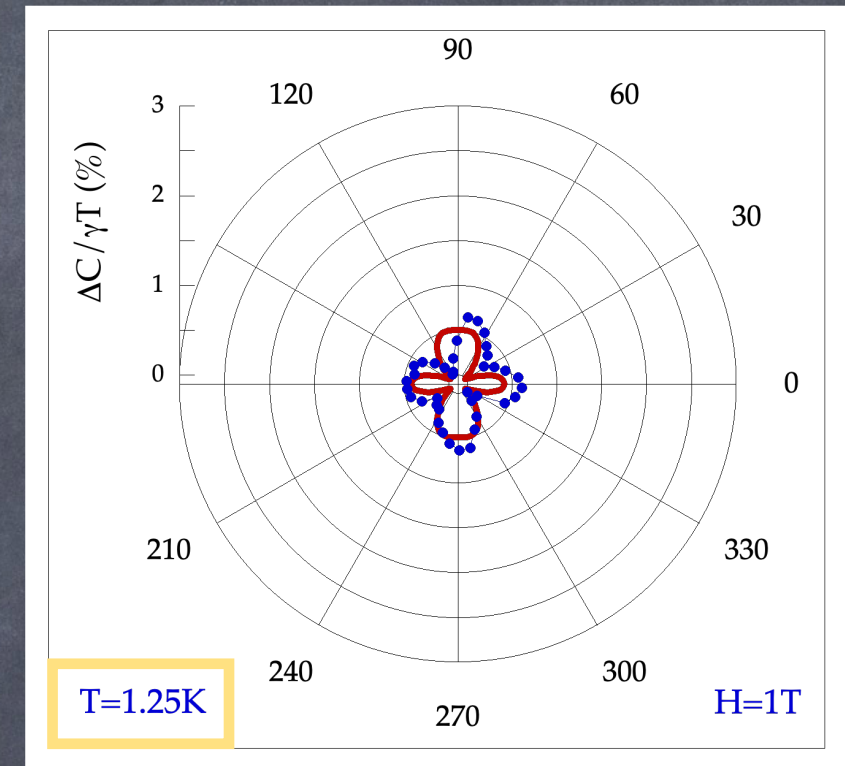
$$\Delta_{\text{elec}}^{\text{min}} \sim -0.2\text{meV}$$



increasing temperature

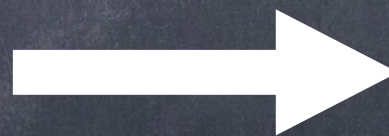


but  
**drastic drop**  
of the  
amplitude  
above 1K ?



**Sudden** change in the gap structure

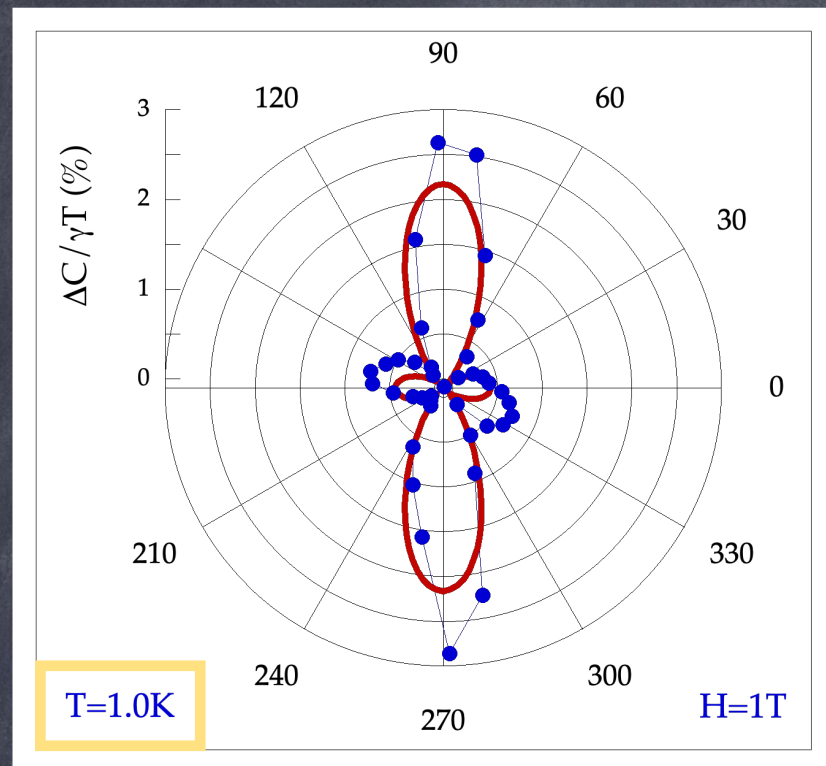
$$\left. \begin{aligned} \Delta_{\text{hole}}^{\text{max}} &\sim 2\text{meV} \\ \Delta_{\text{hole}}^{\text{min}} &\sim -0.2\text{meV} \\ \Delta_{\text{elec}}^{\text{max}} &\sim 1\text{meV} \\ \Delta_{\text{elec}}^{\text{min}} &\sim -0.2\text{meV} \end{aligned} \right\}$$



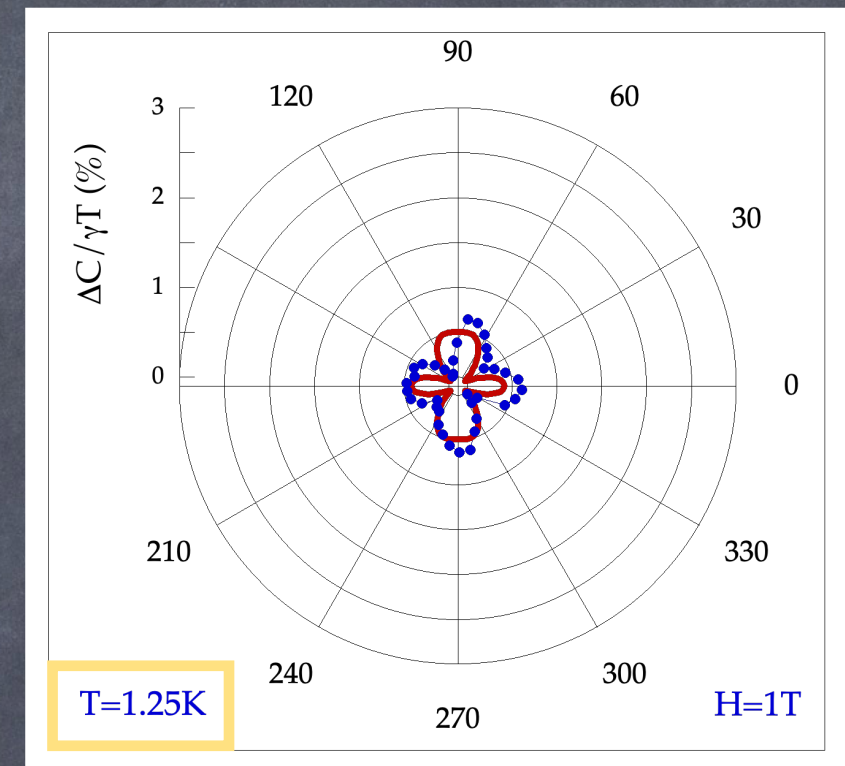
$$\left\{ \begin{aligned} \Delta_{\text{hole}}^{\text{max}} &\sim 2\text{meV} \\ \Delta_{\text{hole}}^{\text{min}} &\sim 0.5\text{meV} \\ \Delta_{\text{elec}}^{\text{max}} &\sim 0.5\text{meV} \\ \Delta_{\text{elec}}^{\text{min}} &\sim -0.2\text{meV} \end{aligned} \right.$$



increasing temperature

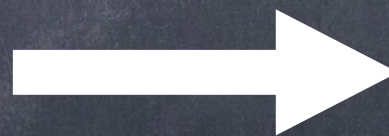


but  
drastic drop  
of the  
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Sudden change in the gap structure

$$\left. \begin{aligned} \Delta_{\text{hole}}^{\text{max}} &\sim 2\text{meV} \\ \Delta_{\text{hole}}^{\text{min}} &\sim -0.2\text{meV} \\ \Delta_{\text{elec}}^{\text{max}} &\sim 1\text{meV} \\ \Delta_{\text{elec}}^{\text{min}} &\sim -0.2\text{meV} \end{aligned} \right\}$$

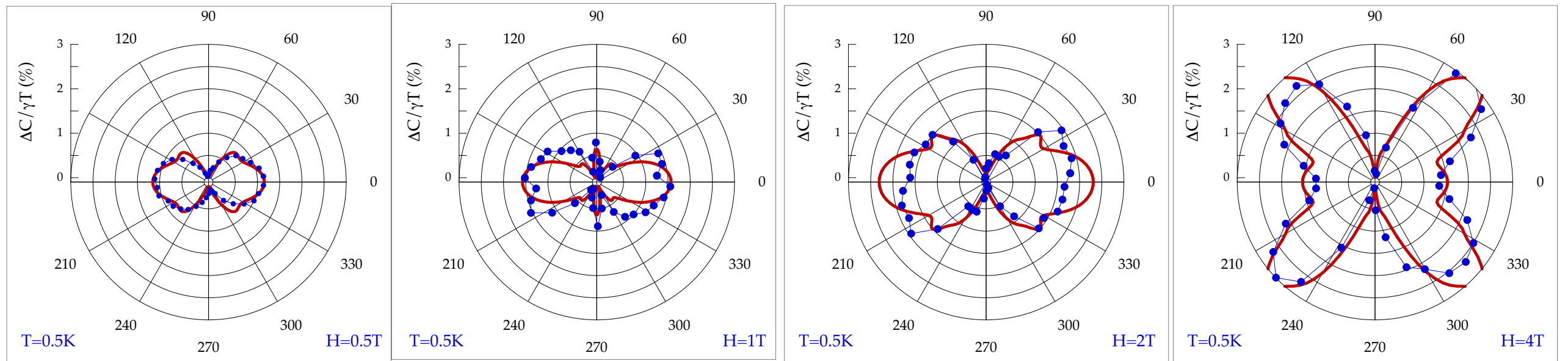
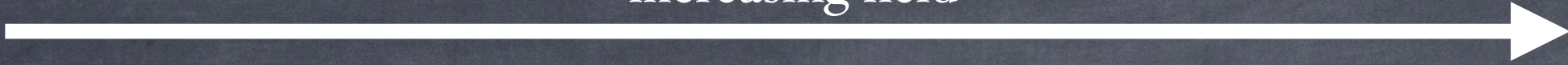


$$\left\{ \begin{aligned} \Delta_{\text{hole}}^{\text{max}} &\sim 2\text{meV} \\ \Delta_{\text{hole}}^{\text{min}} &\sim 0.5\text{meV} \\ \Delta_{\text{elec}}^{\text{max}} &\sim 0.5\text{meV} \\ \Delta_{\text{elec}}^{\text{min}} &\sim -0.2\text{meV} \end{aligned} \right.$$

... leading to the observed specific anomaly around 1K



increasing field



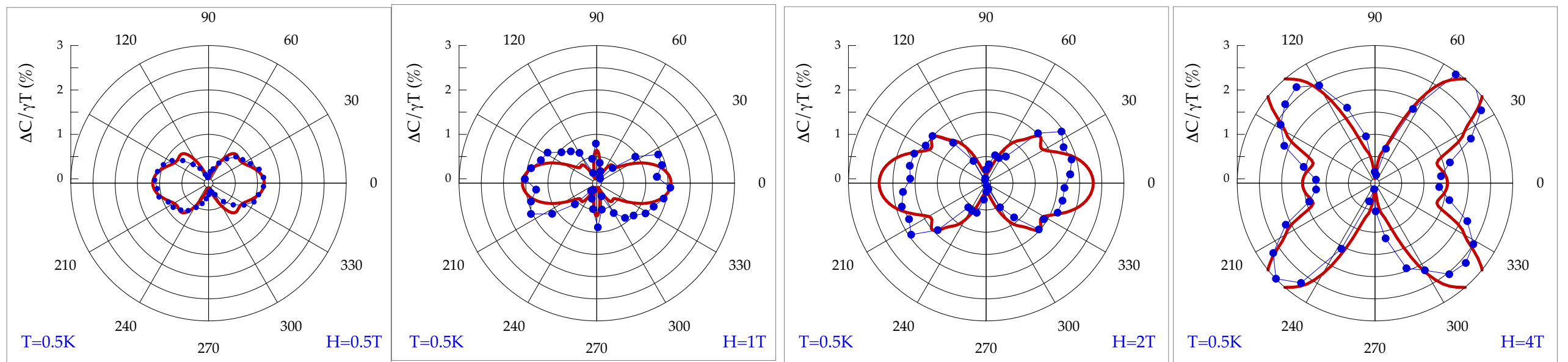
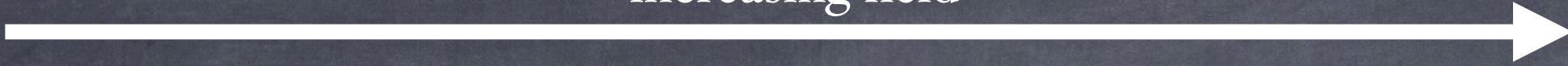
and lobes develop  
around  $45^\circ$   
above  $\sim 4\text{T}$

field dependent gap amplitude

$$\Delta_{\text{hole}}^{\text{max}} \rightarrow \Delta_{\text{elec}}^{\text{max}} \rightarrow 1.5\text{meV}$$



increasing field



and lobes develop  
around  $45^\circ$   
above  $\sim 4\text{T}$

field dependent gap amplitude

$$\Delta_{\text{hole}}^{\text{max}} \rightarrow \Delta_{\text{elec}}^{\text{max}} \rightarrow 1.5\text{meV}$$

This T and H dependence of the gap structure still has to be understood  
(not observed in all samples...)

H.Cercellier *et al.* submitted to PRL (2024)



# Outline

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- ◎ **The FeSe nematic superconductor**

H-T phase diagram and T & H dependence of the gap structure

- ◎ **Thermodynamic properties of the normal state in cuprates**

Quantum criticality at the onset of the pseudo-gap and charge order

part of the PhD work of **B.Michon & C.Girod**



# Outline

---

- ◎ **Thermodynamic properties of the normal state in cuprates**  
Quantum criticality at the onset of the pseudo-gap and charge order

part of the PhD work of **B.Michon & C.Girod**



# Cuprates

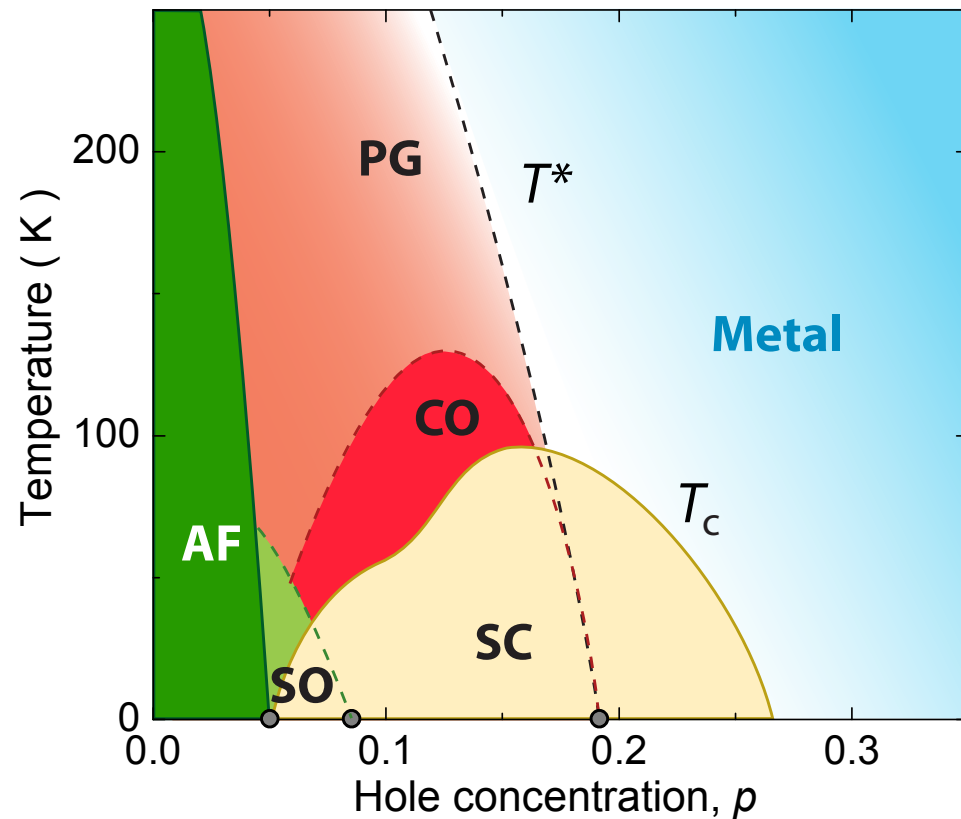
very complexe phase diagram

CO=**charge order**

SO=spin order

PG= *mysterious* **pseudo-gap phase**

SC=superconductor



YBaCuO, Courtesy N.Doiron-Leyraud, Univ. of Sherbrooke



# Cuprates

very complexe phase diagram

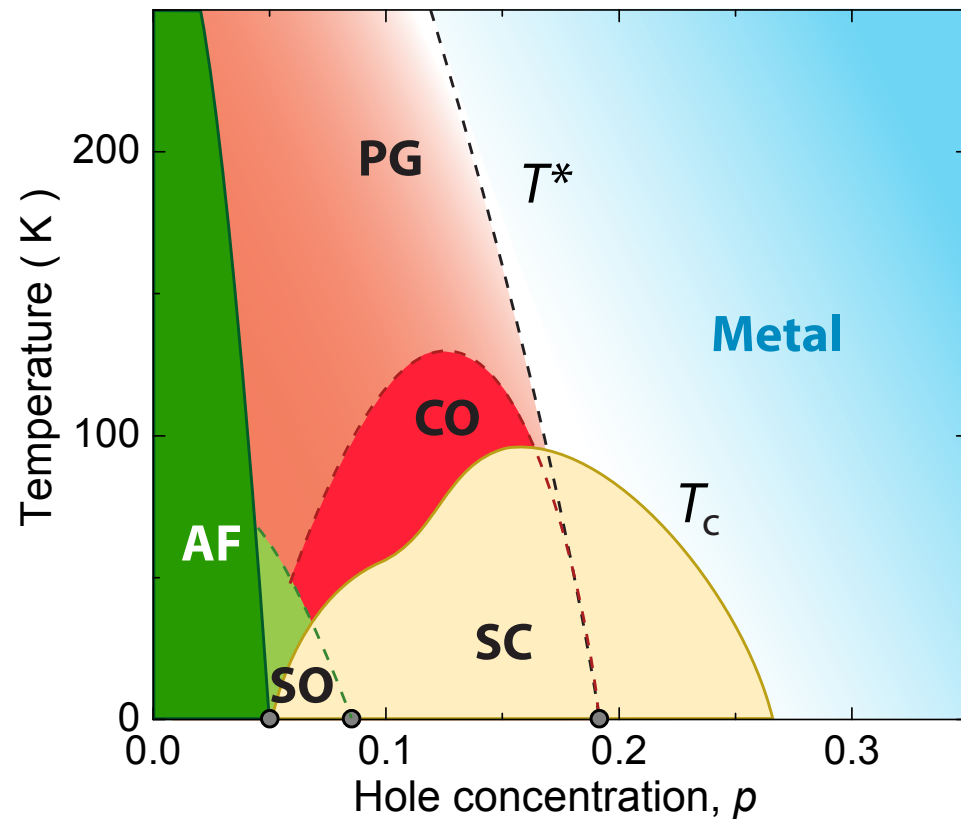
CO=charge order

SO=spin order

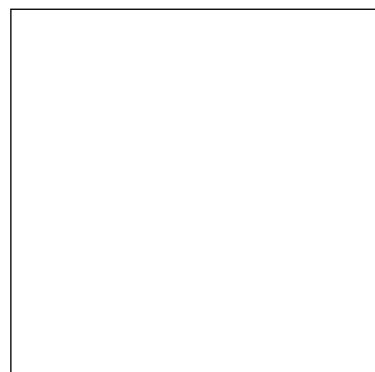
PG= *mysterious* pseudo-gap phase

SC=superconductor

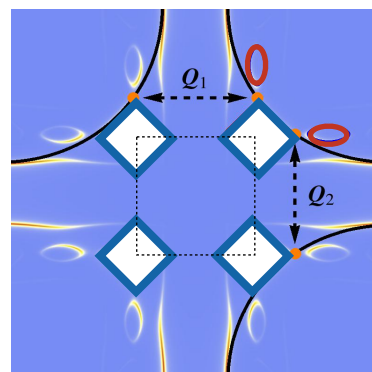
associated with major changes in the topology of the Fermi surface



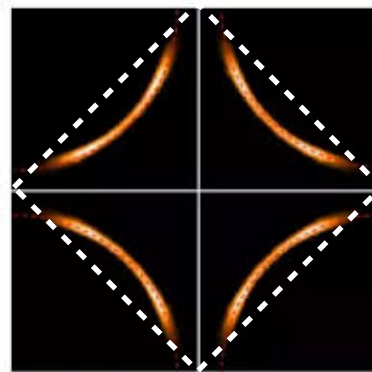
YBaCuO, Courtesy N.Doiron-Leyraud, Univ. of Sherbrooke



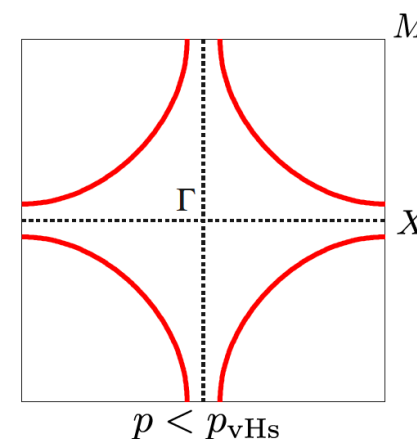
$p = 0$



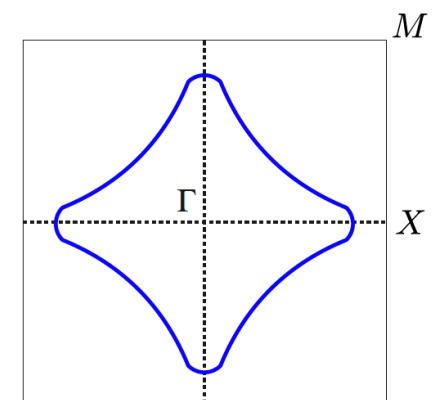
$p = p_{co}$



$p = p_{pg}$



$p < p_{vHs}$



$p_{vHs} < p$

$p = p_{vHs}$



# Let's start with the pseudo-gap phase...

## Linear temperature dependence

of the resistivity : so-called *Planckian* diffusion

C. Collignon et al., PRB 2017, A. Legros et al., Nature 2019

## Drop in the carrier density from $n=1+p$ to $n=p$

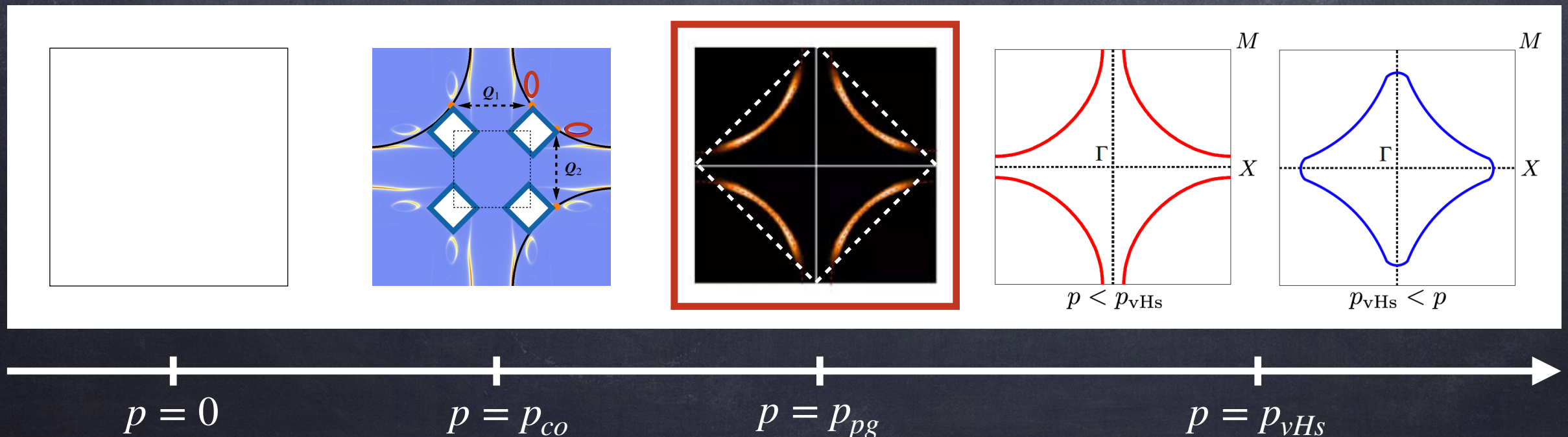
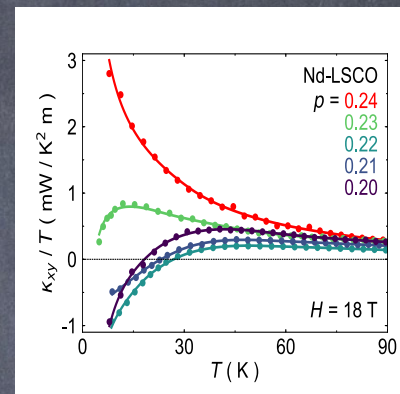
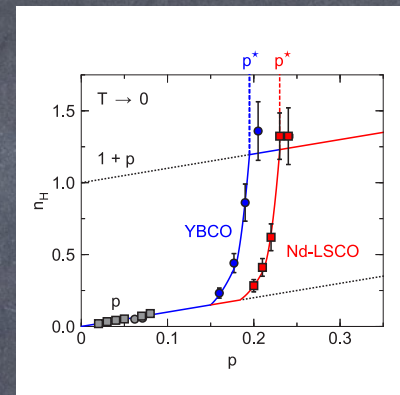
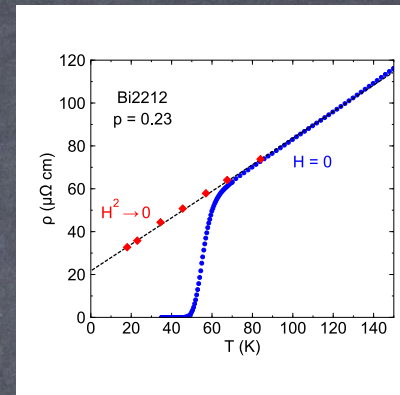
consistent with (AF) reconstruction of the FS

C. Collignon et al., PRB 2017, S. Badoux et al., Nature 2016

## Giant negative thermal Hall effect

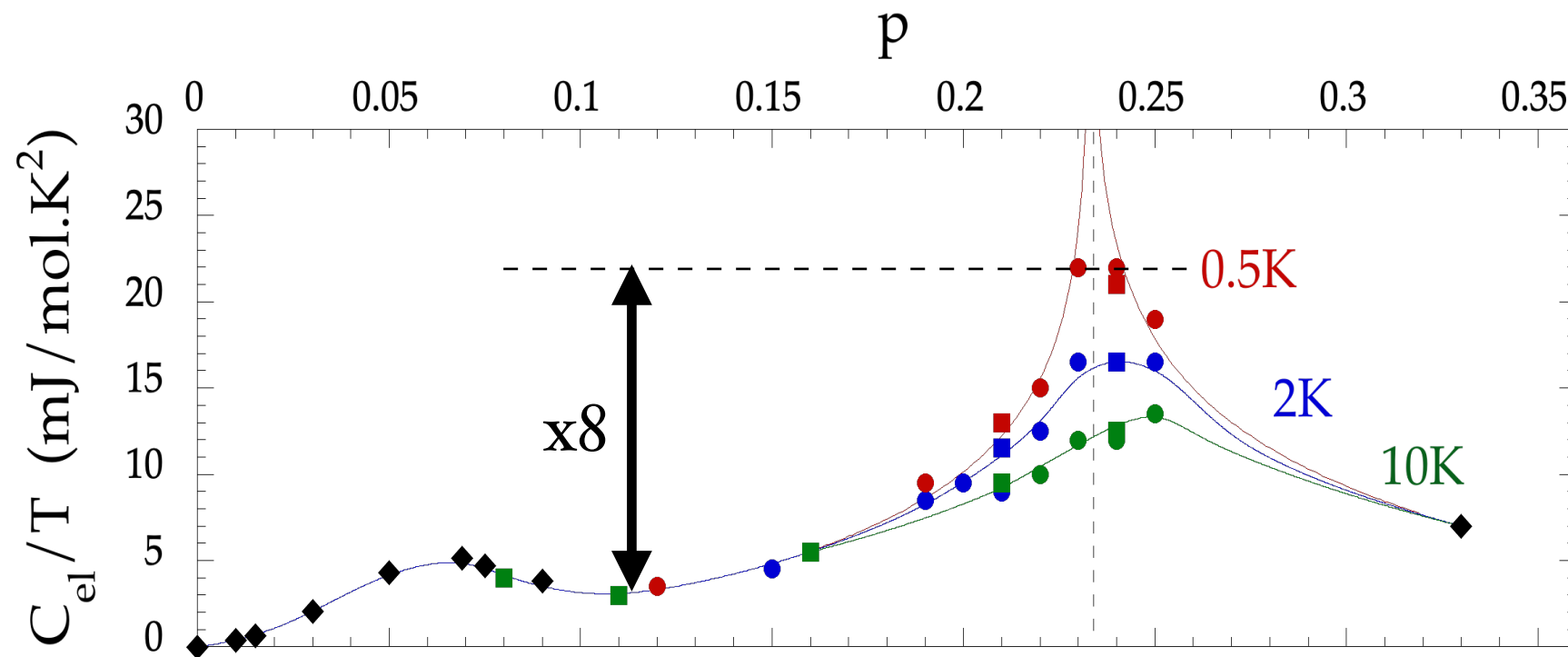
from  $p_{pg}$  down the Mott insulator ( $p=0$ )

G. Grissonanche et al., Nature 2019 & 2020, M-E. Boulanger et al., Nat. Com 2020



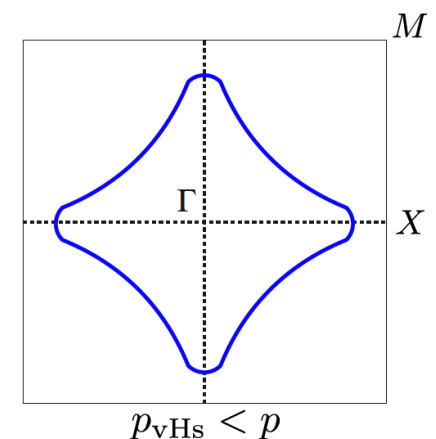
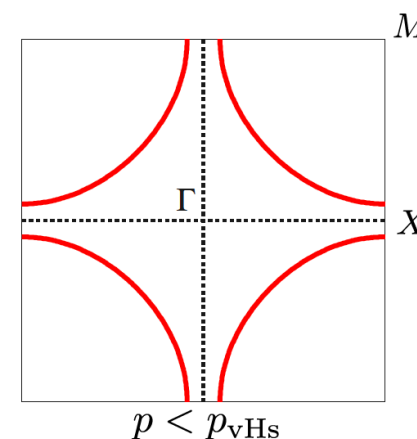
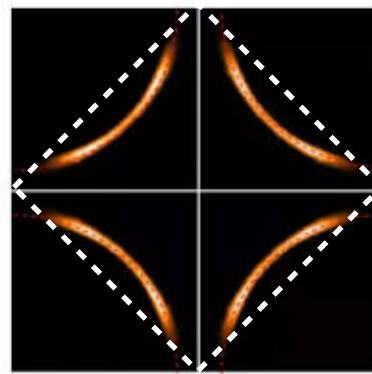
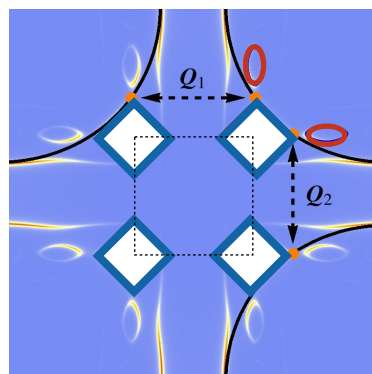
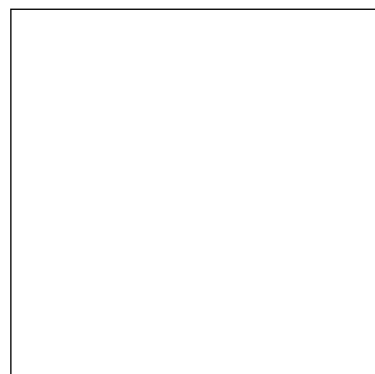


We have shown that the onset of the PG is also associated with  
**pronounced peak** of the Normal state specific heat for  $T \rightarrow 0$   
 (as mentioned yesterday by Chandra Warma)



Nd/Eu-LSCO :  
 $T_c < 15\text{K}$   
 $H_{c2}(0) < 18\text{T}$

B.Michon *et al.*  
 Nature 2019



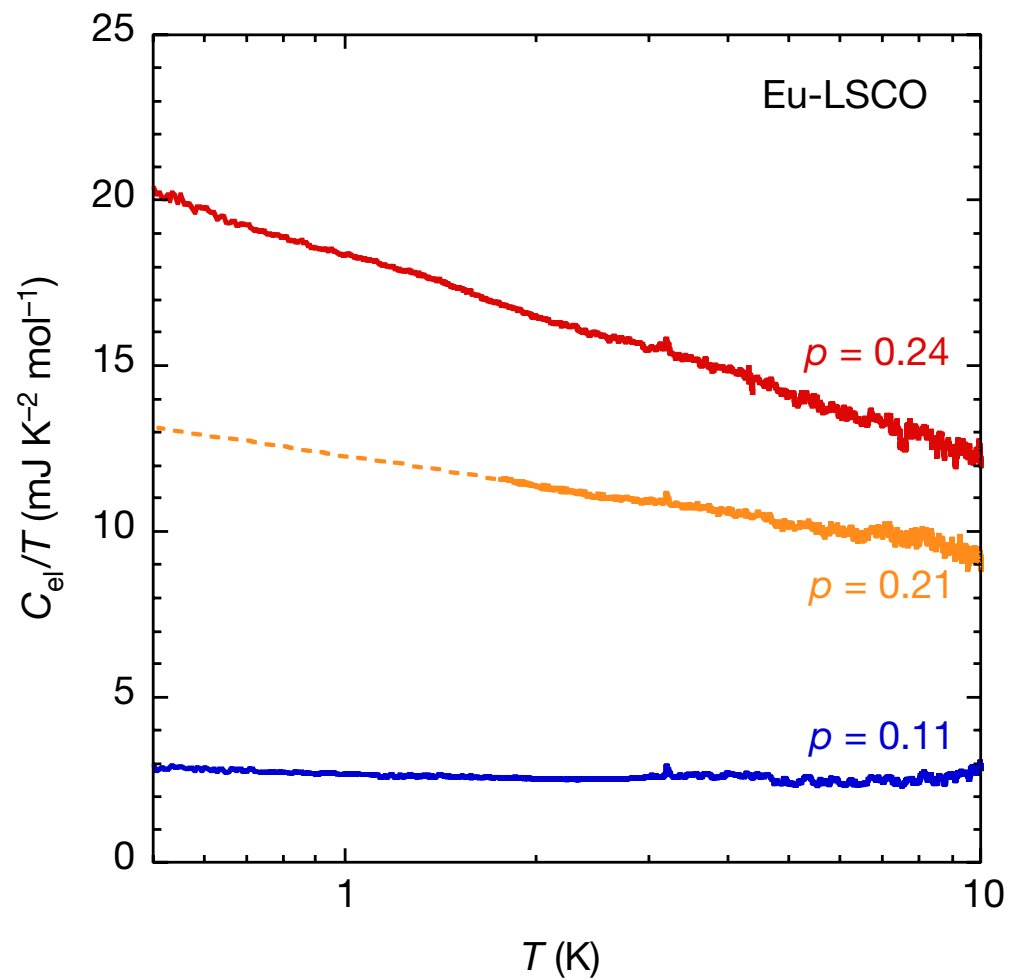
$p = 0$

$p = p_{co}$

$p = p_{pg}$

$p = p_{vHs}$

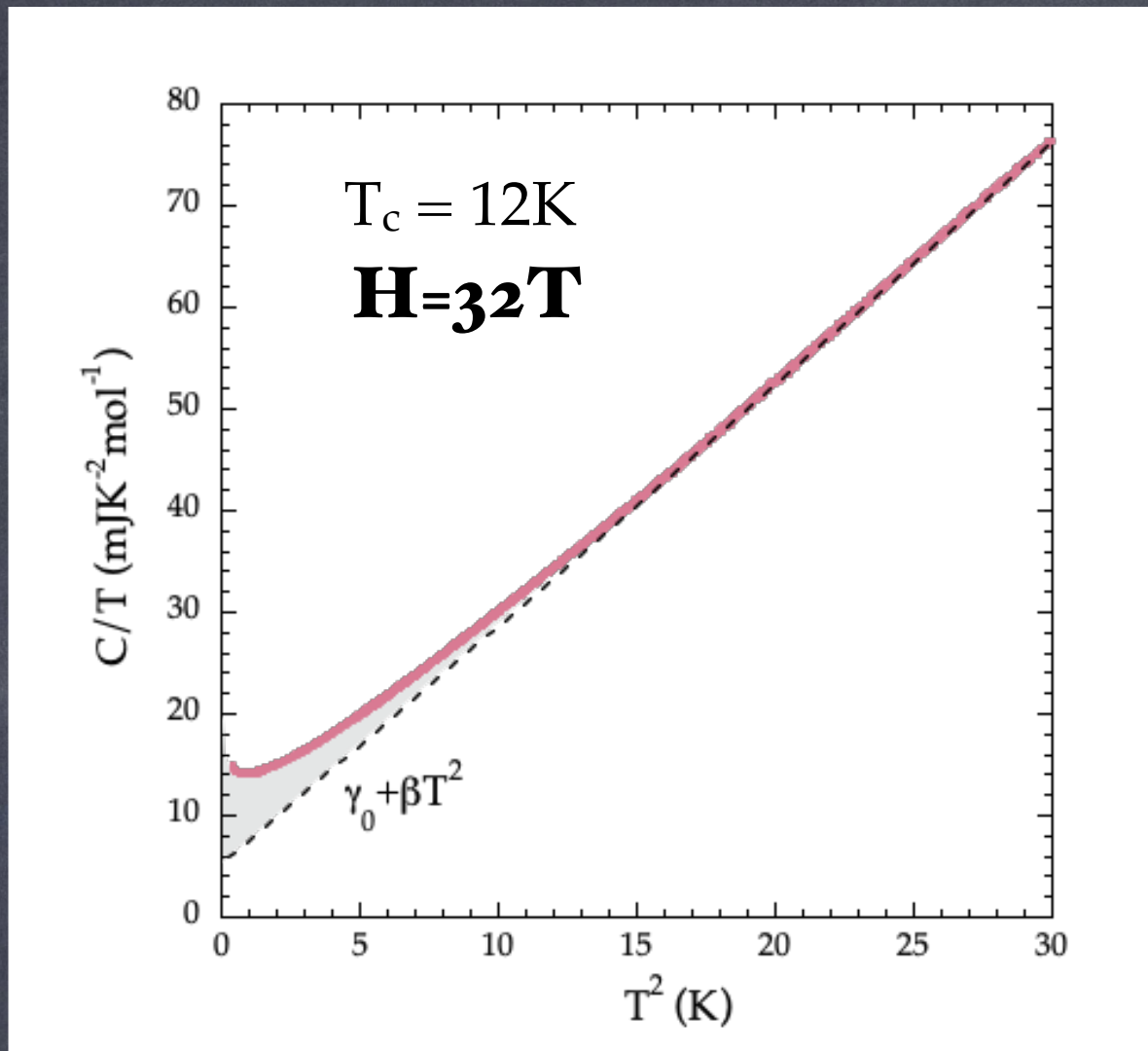




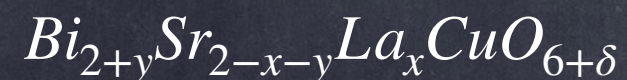
associated with a  $\text{Log}T$   
dependence of  $C_{el}/T$   
for  $p \rightarrow p_{pg} \sim 0.24$   
(here  $C_{el}/T = C/T - \beta T^2$ )

Michon *et al.* Nature 2019



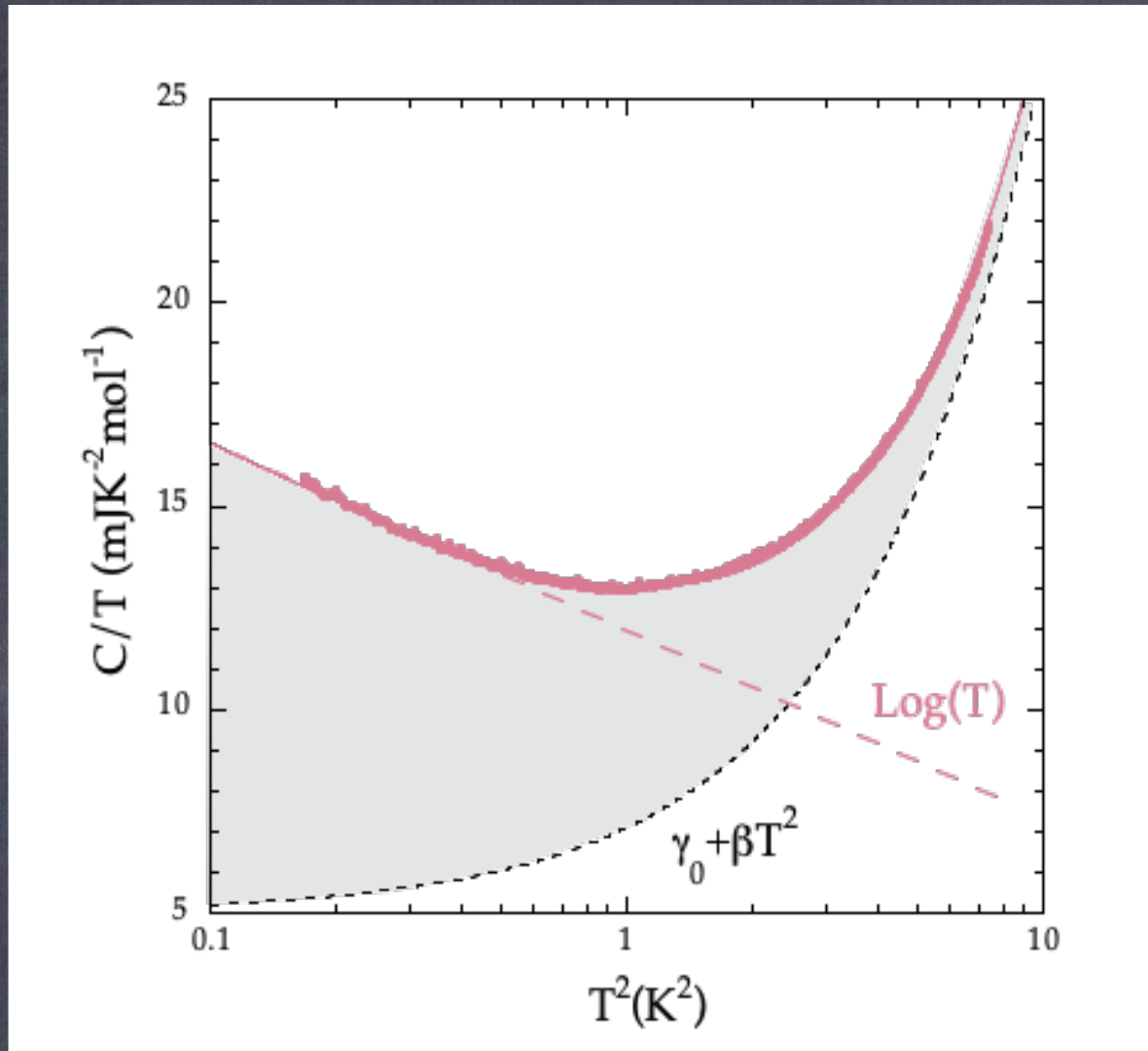


clear deviation from the  
 standard temperature  
 dependence also observed in



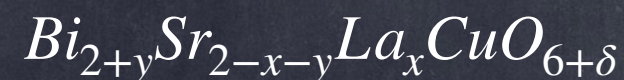
C.Girod *et al.* PRB 2021





(again) very good fit  
to the data with  
 $C/T = \beta T^2 + B \text{Log}(T/T_0)$

**clear deviation from the  
standard temperature  
dependence also observed in**



C.Girod *et al.* PRB 2021



LnT contribution to  
the specific heat pour  $p \sim p_c$

strong C/T peak  
for  $p \rightarrow p_c$  at low T

= *classic* thermodynamic signature of a  $z = d$  **Quantum Critical Point**

**BUT...what is the diverging correlation length ?**



LnT contribution to  
the specific heat pour  $p \sim p_c$

strong C/T peak  
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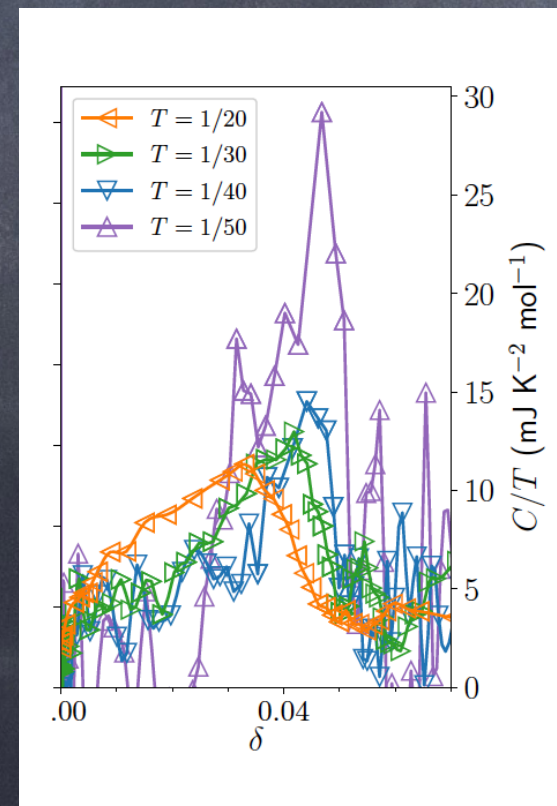
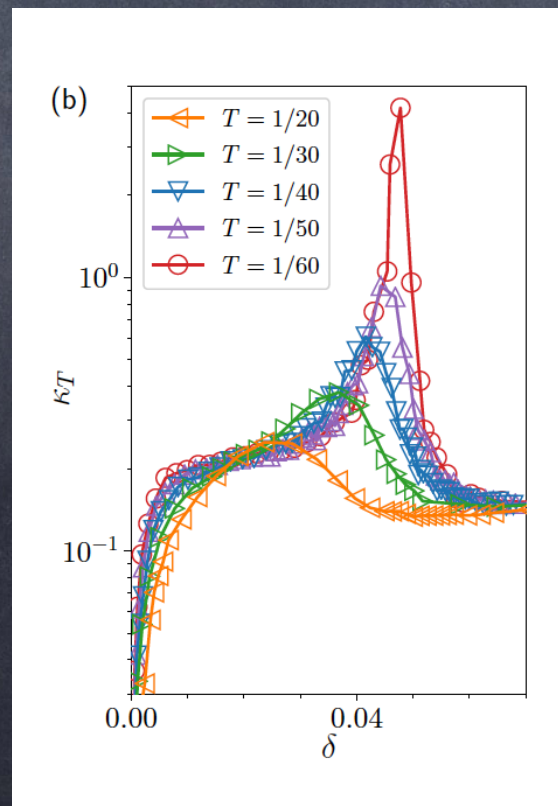
= *classic* thermodynamic signature of a  $z = d$  **Quantum Critical Point**

**BUT...what is the diverging correlation length ?**

cluster-DMFT calculations in the t-U model (correlated systems)

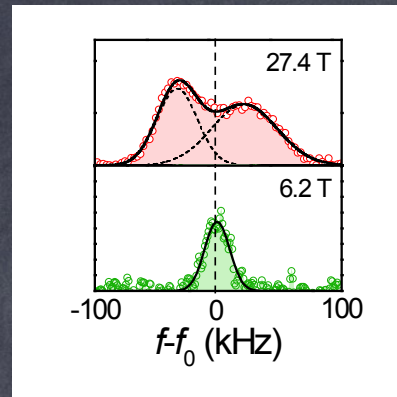
G.Sordi *et al.* Sc. Reports 2012, 2010

T dependent peak in  
the electronic  
compressibility  
 $K_T = 1/n^2(dn/d\mu)_T$   
(diverging at the  
critical point)



**AND in the  
specific heat !  
(as observed)**



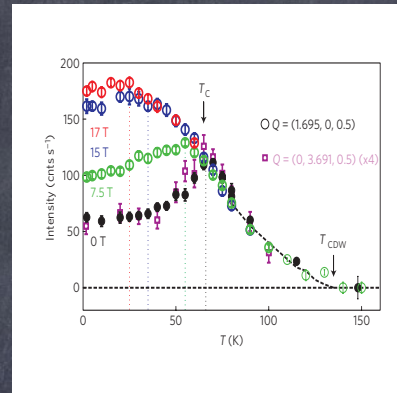


and a few words on the Charge Order...

## Splitting of the NMR lines

modulation of the charge density

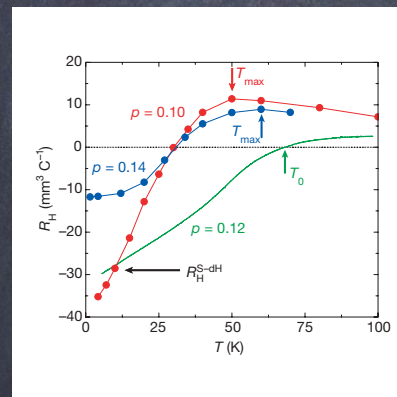
T.Wu et al. Nature 2011



## X-ray diffraction peaks

⇒ Long range CDW at high field/low T

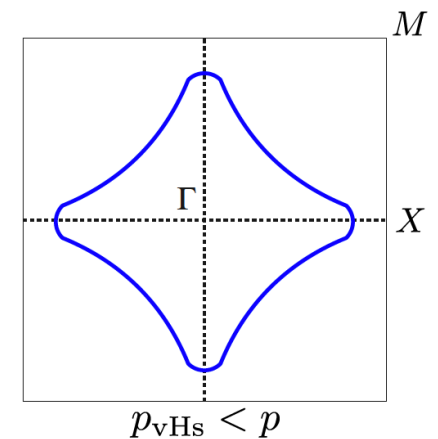
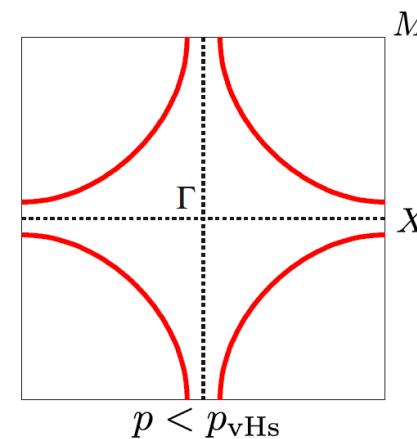
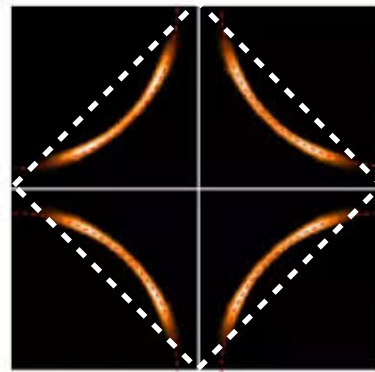
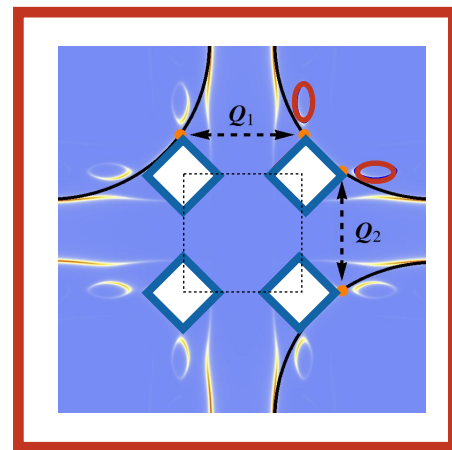
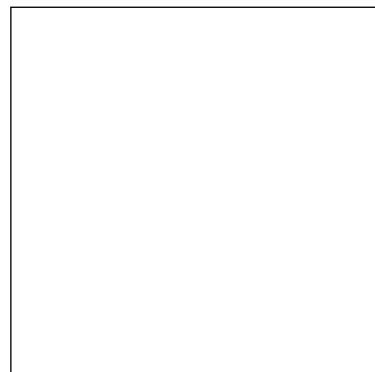
J.Chang et al. Nature Physics 2012, D.Leboeuf et al. Nature Physics 2013 (and more)



## Change of sign of Hall effect

+ low frequency quantum oscillations (FS reconstruction) & reduced  $H_{c2}$

D.Leboeuf et al. Nature 2007, Nicolas Doiron-Leyraud et al. Nature 2007,...



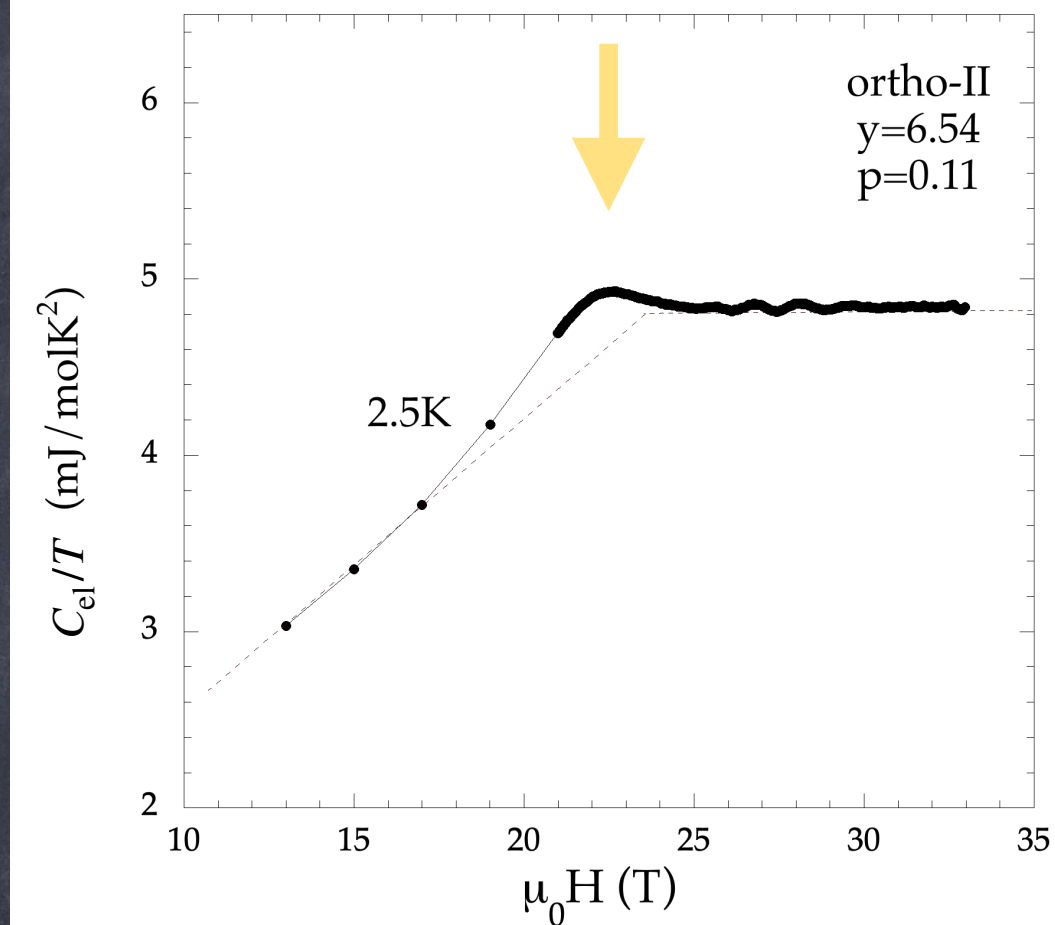
$p = 0$

$p = p_{co}$

$p = p_{pg}$

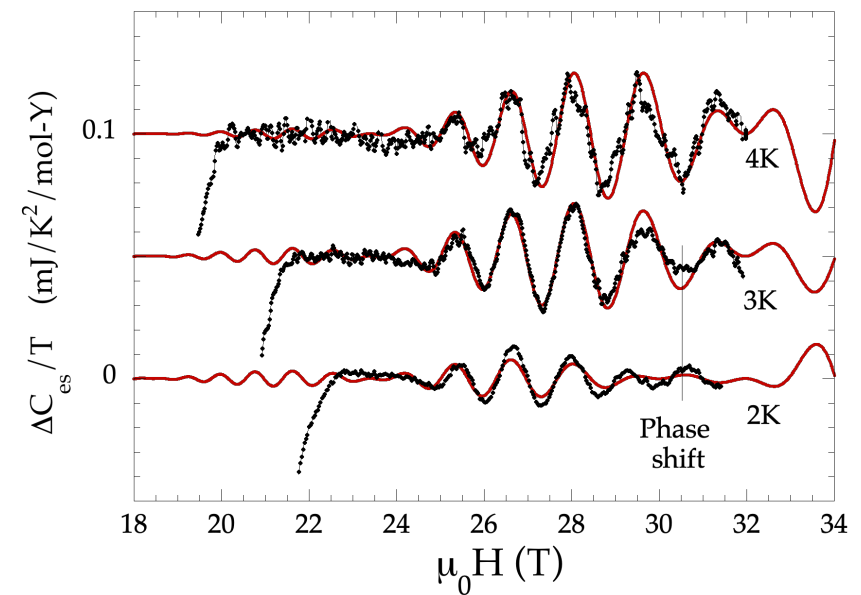
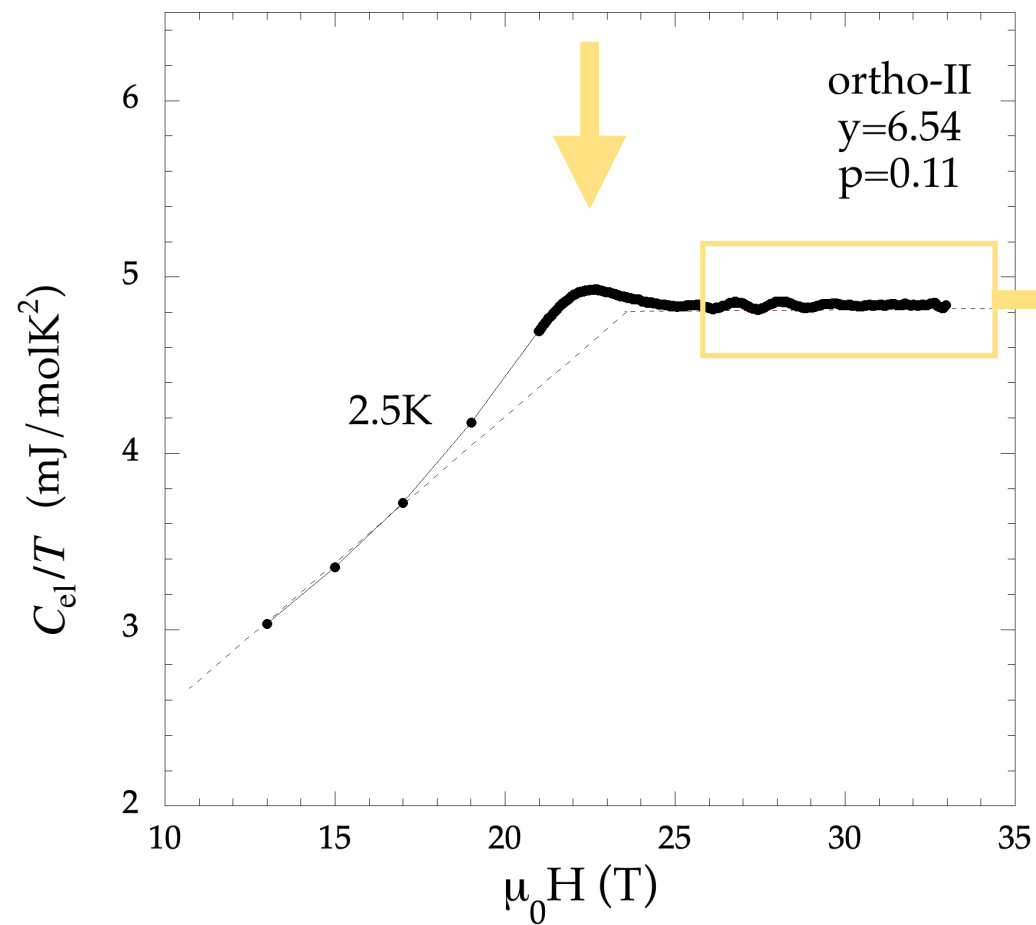
$p = p_{vHs}$





$C/T$  saturates for  $H > H_{\text{DOS}}$   
(not  $H_{c2}$  due to thermal fluctuations)

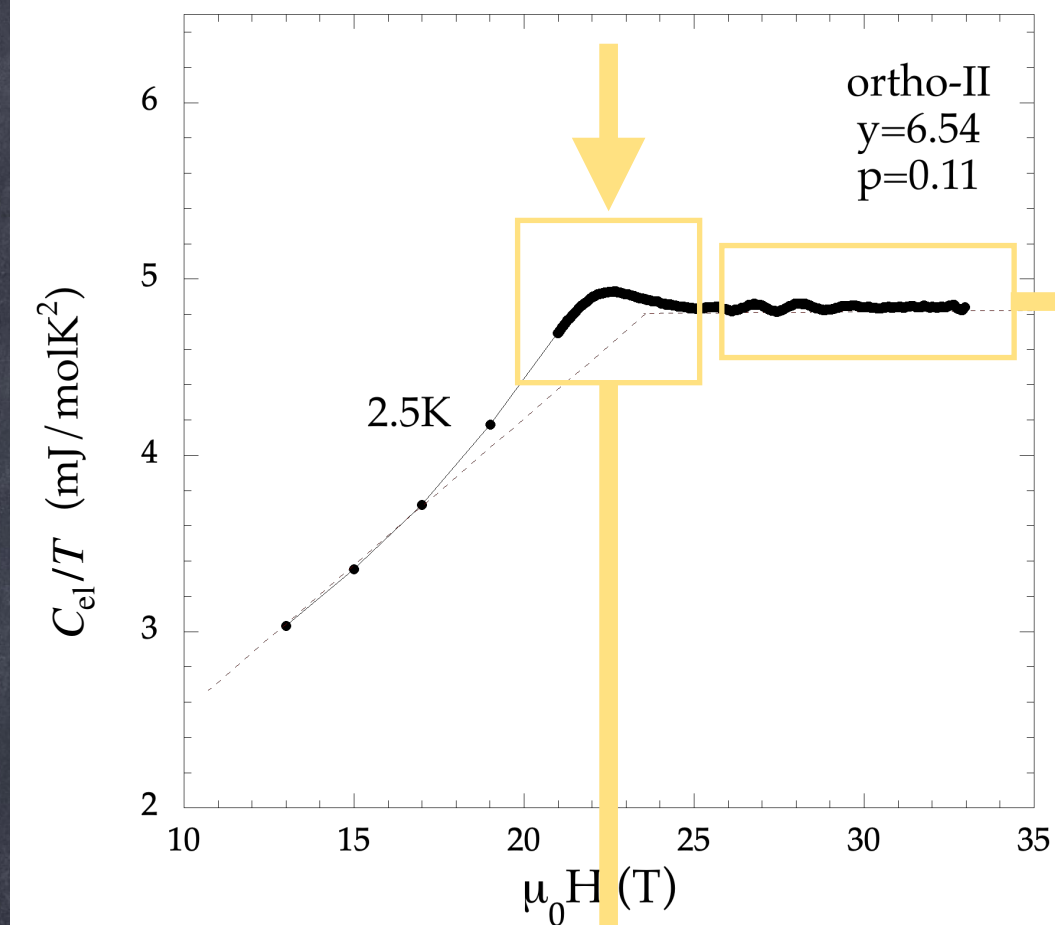




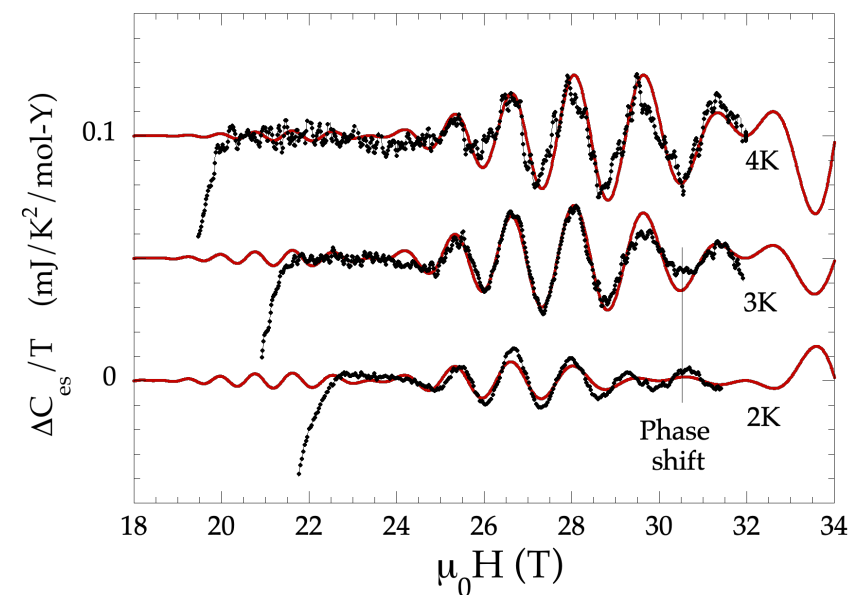
Note the presence of well resolved quantum oscillations in good agreement with **small electron pockets**

$C/T$  saturates for  $H > H_{DOS}$   
(not  $H_{c2}$  due to thermal fluctuations)





note also the small  
**Overshoot at 22T?**



Note the presence of well  
resolved quantum oscillations  
in good agreement with **small  
electron pockets**

$C/T$  saturates for  $H > H_{DOS}$   
(not  $H_{c2}$  due to thermal fluctuations)



which **increases**

for decreasing temperature !

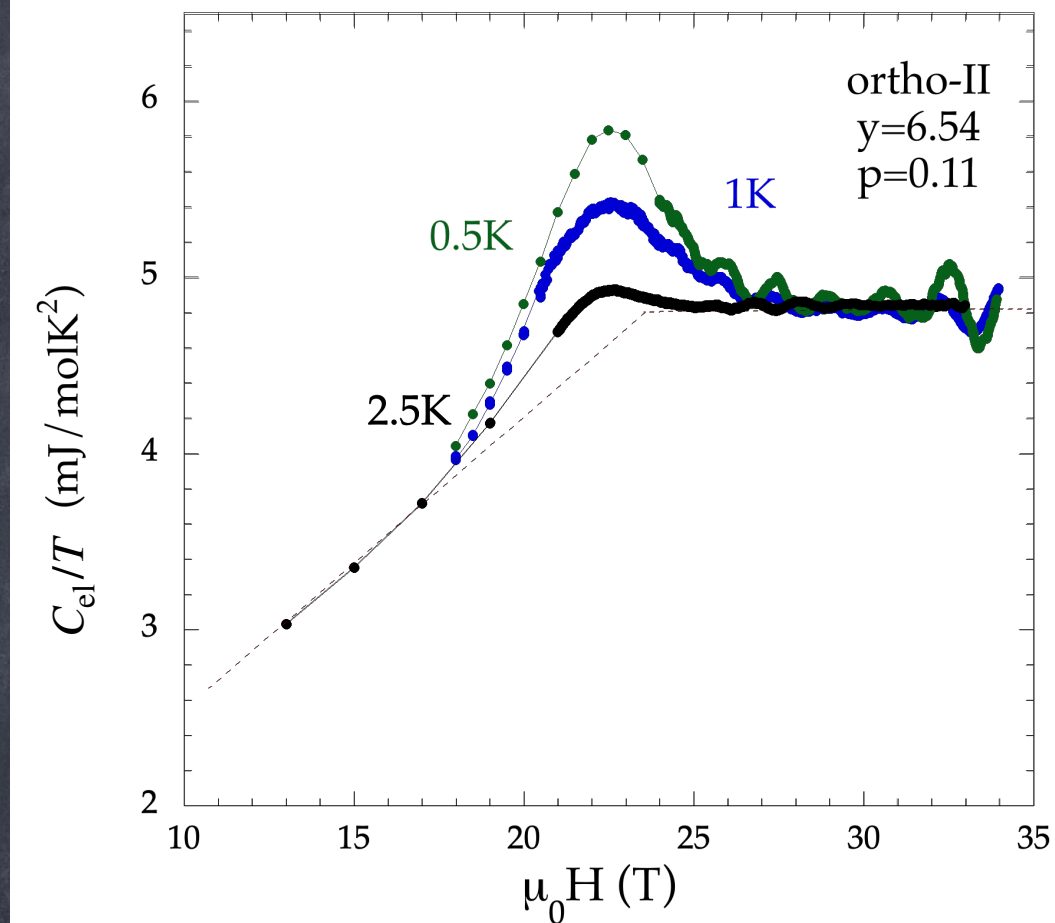
(unpublished)

Can **not** be the standard overshoot  
observed at the SC transition

Its origin still has to be clarified...

(another field induced)

quantum critical point ???





which **increases**

for decreasing temperature !

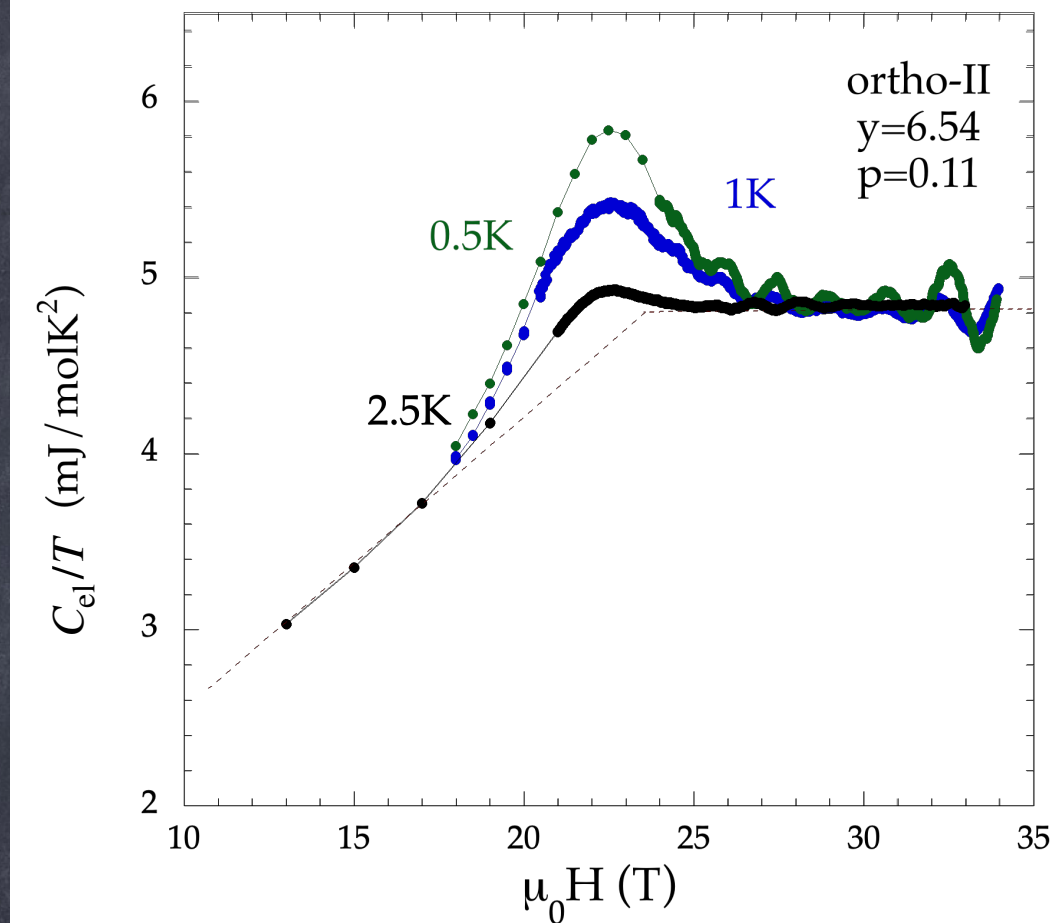
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observed at the SC transition

Its origin still has to be clarified...

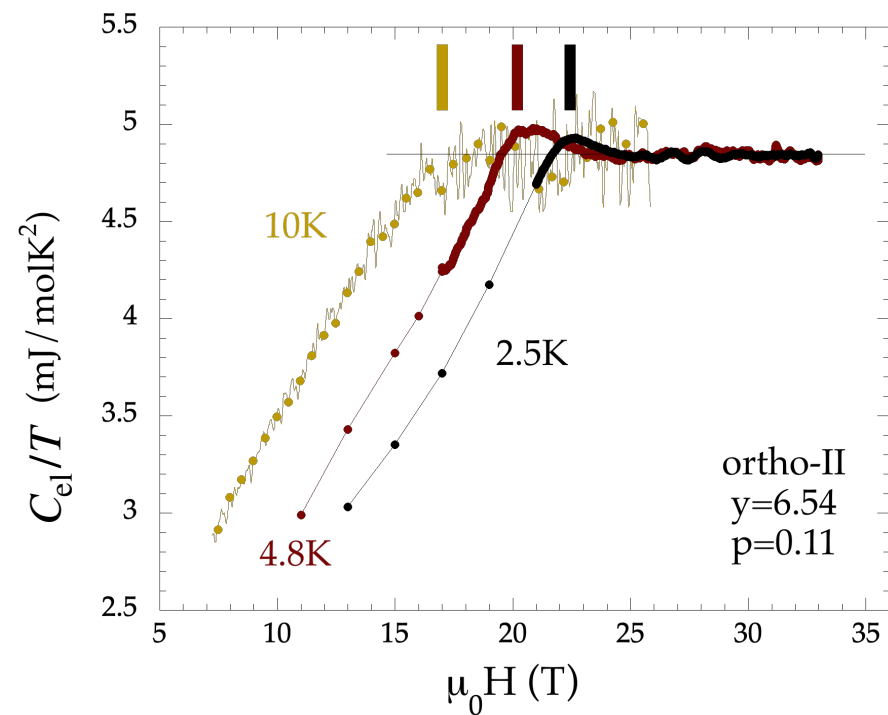
(another field induced)

quantum critical point ???



but let's follow the temperature dependence of  $H_{\text{DOS}}$





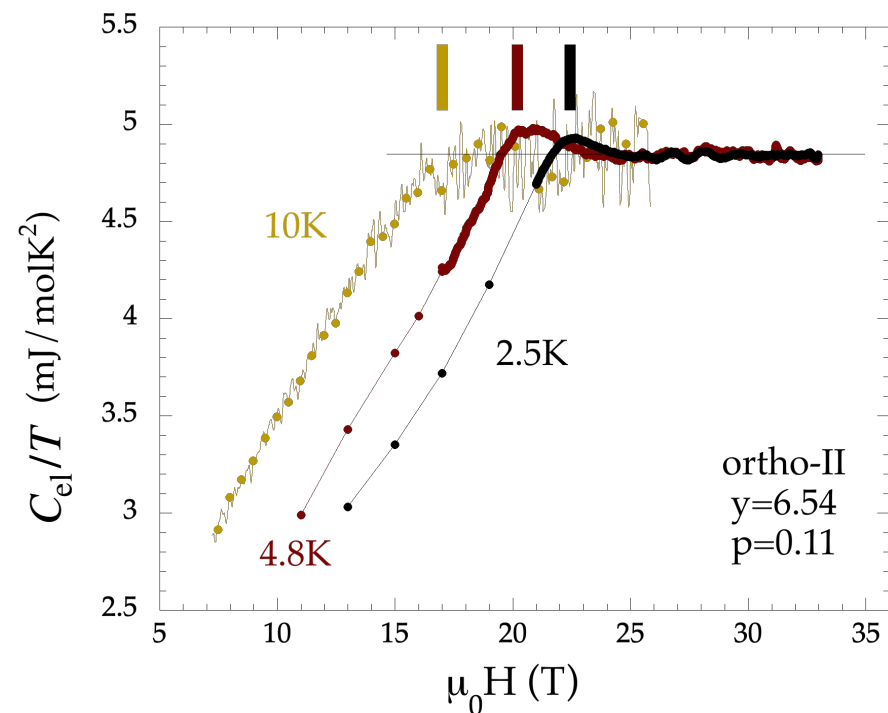
As expected  $H_{DOS}$  decreases with T

but...  $\frac{C_{el}}{T} = \frac{C}{T} - \beta T^2$

and the phonons contribution  
rapidly increases

$\Rightarrow$  increasing signal/noise ratio





As expected  $H_{\text{DOS}}$  decreases with  $T$

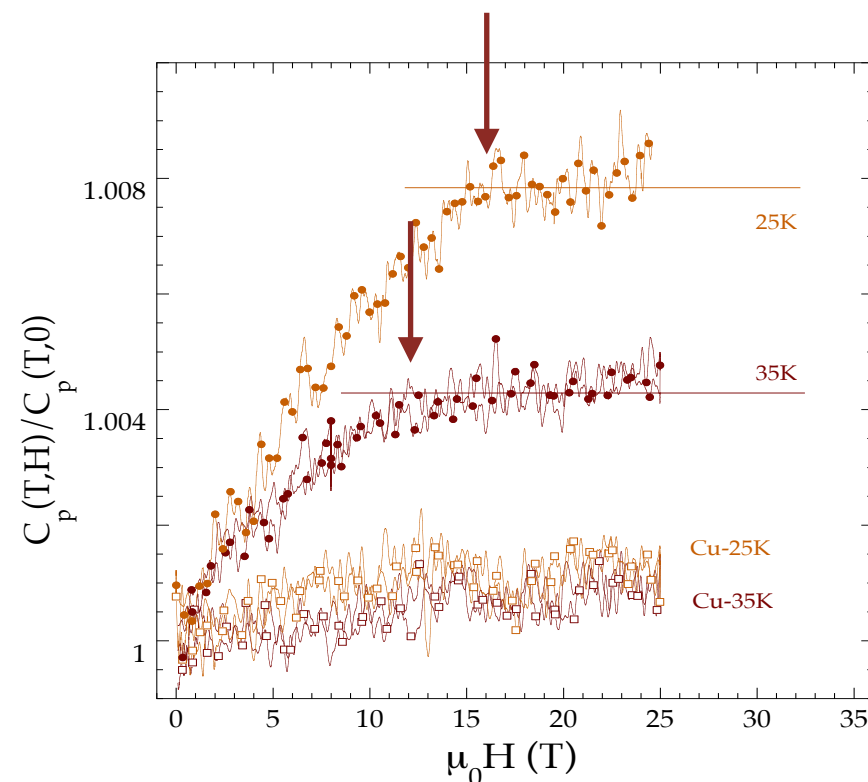
$$\text{but... } \frac{C_{\text{el}}}{T} = \frac{C}{T} - \underline{\beta T^2}$$

and the phonons contribution  
rapidly increases

⇒ increasing signal/noise ratio

⇒ **the variation in  $C_{\text{el}}/T$  becomes smaller than 1% above 20K !**

but can still be determined



**Confirmed by NMR**

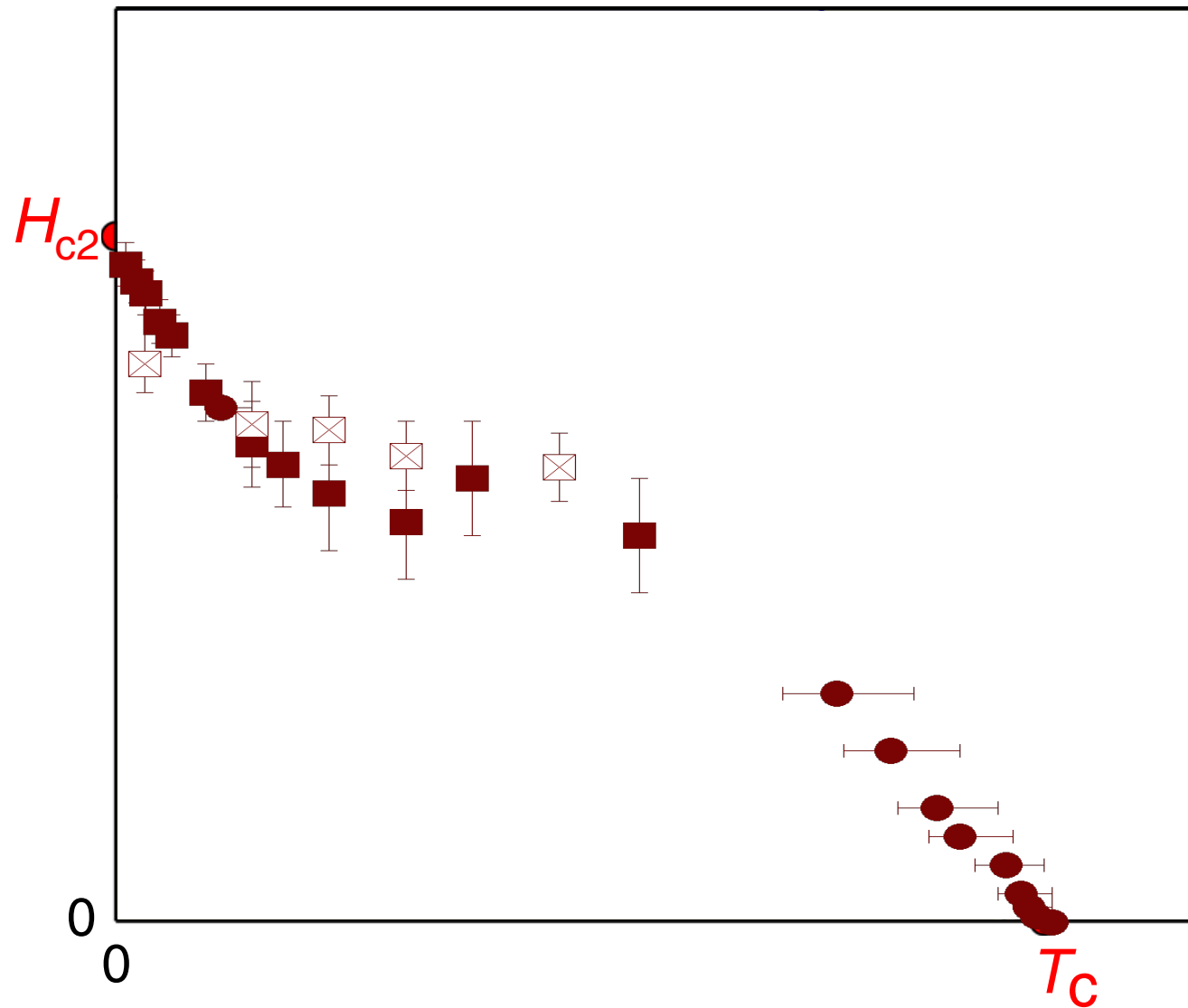
**(Knight shift) measurements**

Group of M-H. Julien

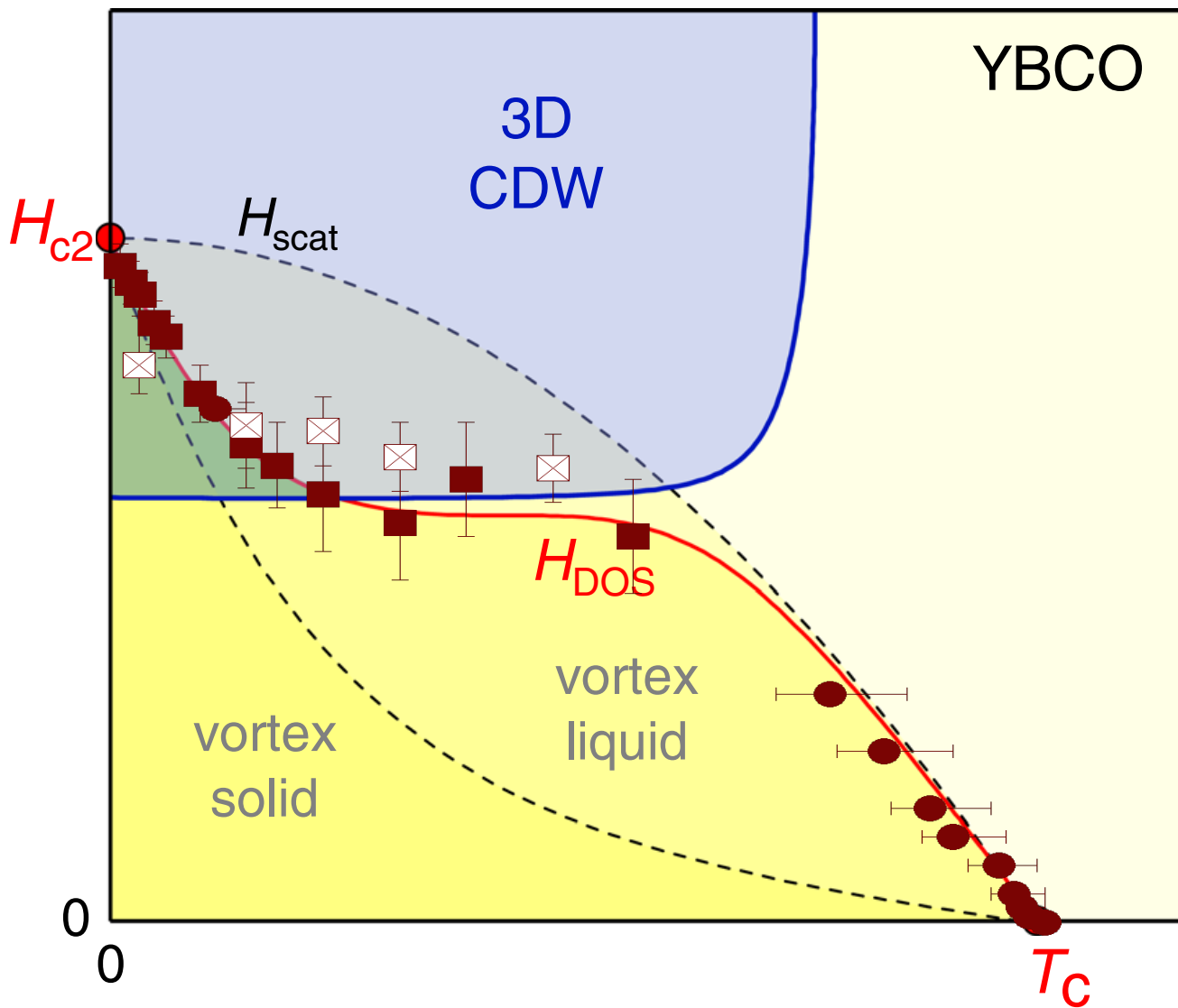
see J.Kacmarcik *et al.* PRL 2019



**Upturn of  $H_{\text{DOS}}(T)$   
at low T?**



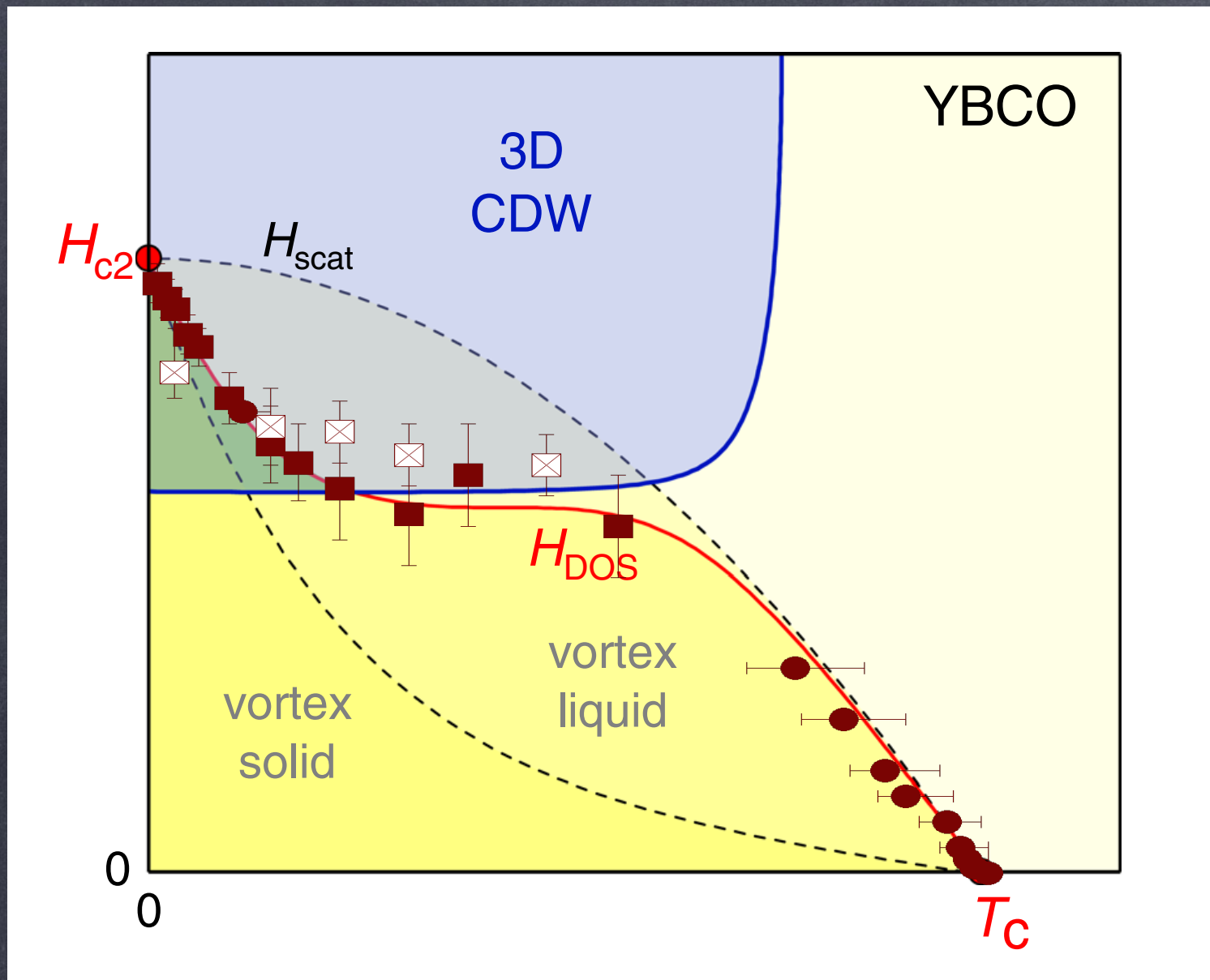




**Upturn of  $H_{\text{DOS}}(T)$   
at low T?**

SC & CDW  
eventually establish  
a form of  
**cooperation**  
at low T





**Upturn of  $H_{\text{DOS}}(T)$   
at low  $T$ ?**

SC & CDW  
eventually establish  
a form of  
**cooperation**  
at low  $T$

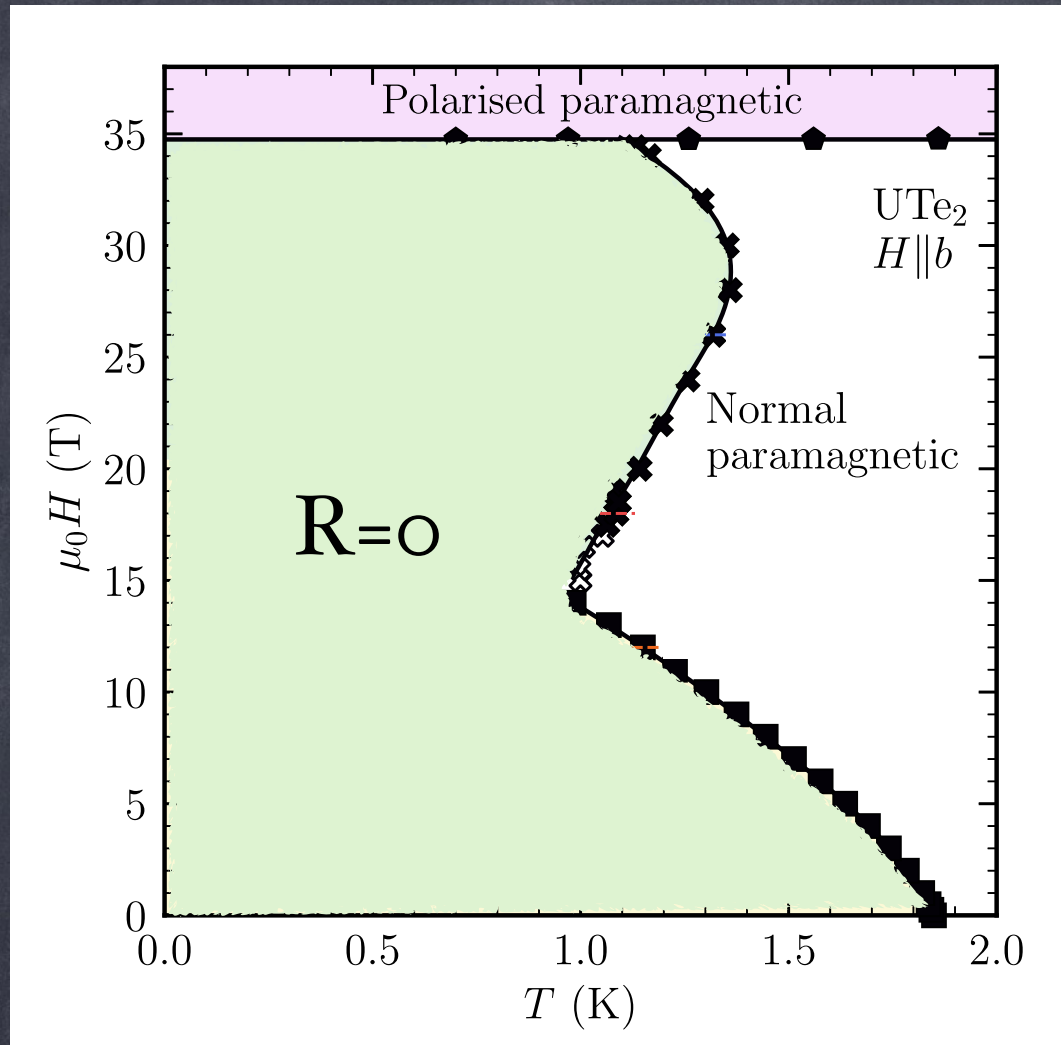
giving rise to some kind of **filamentary SC** at the interface of CDW domains ?  
(or *fragile* SC at CDW dislocations). Yu & Kivelson PRB 2019, Leridon et al. New J.Phys. 2020

or «FFLO-like» upturn, related to the **pair-density wave order** ?

Agterberg et al. PRB 2015, Berg et al. PRL 2007, Dai et al. PRB 2018



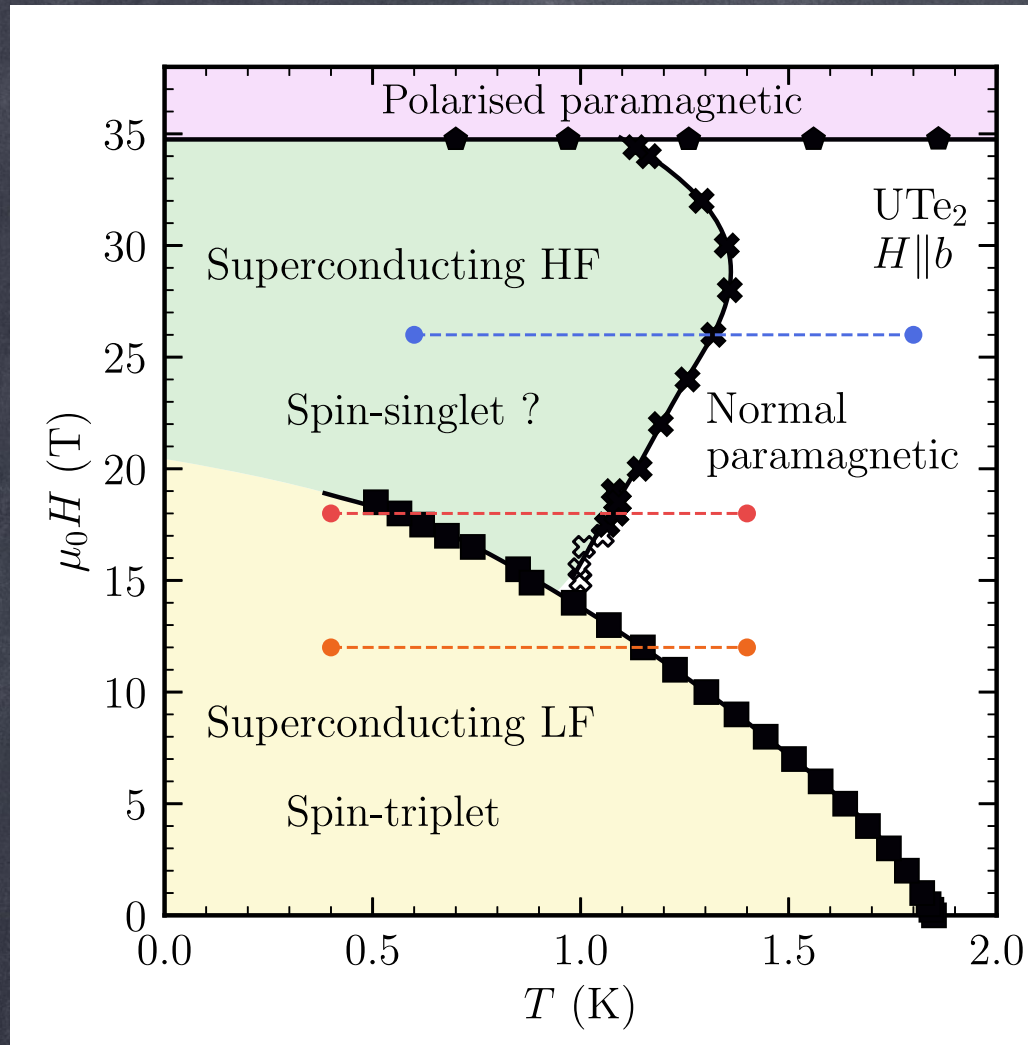
A last exemple to flash....



**Re-entrant** superconductivity in  
**UTe<sub>2</sub>**  
(possible spin-triplet and topological SC)



A last exemple to flash....



**Re-entrant** superconductivity in

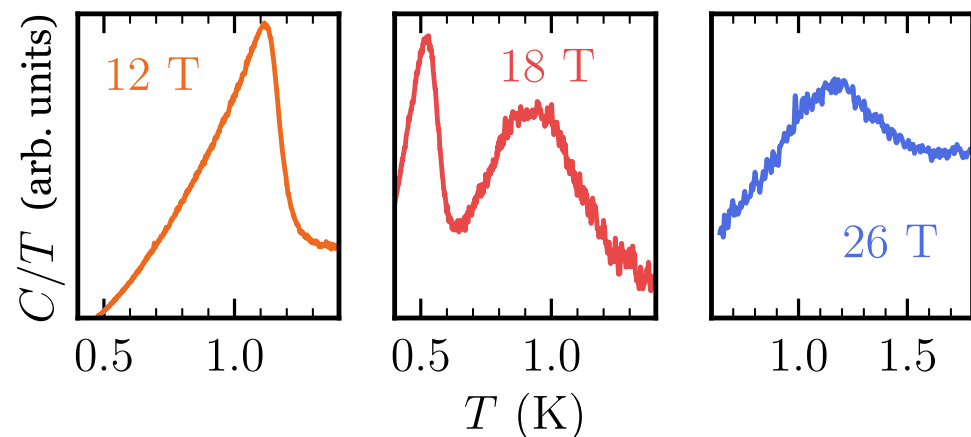
**$\text{UTe}_2$**

(possible spin-triplet and topological SC)

$C/T$  measurement

$\Rightarrow$  phase transition **within** the superconducting state

A Rosuel *et al.* PRX 2023





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Thank you for your attention