

# Probing exotic superconductors by high sensitivity microcalorimetry

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CEA-Grenoble, IRIG-LATEQS

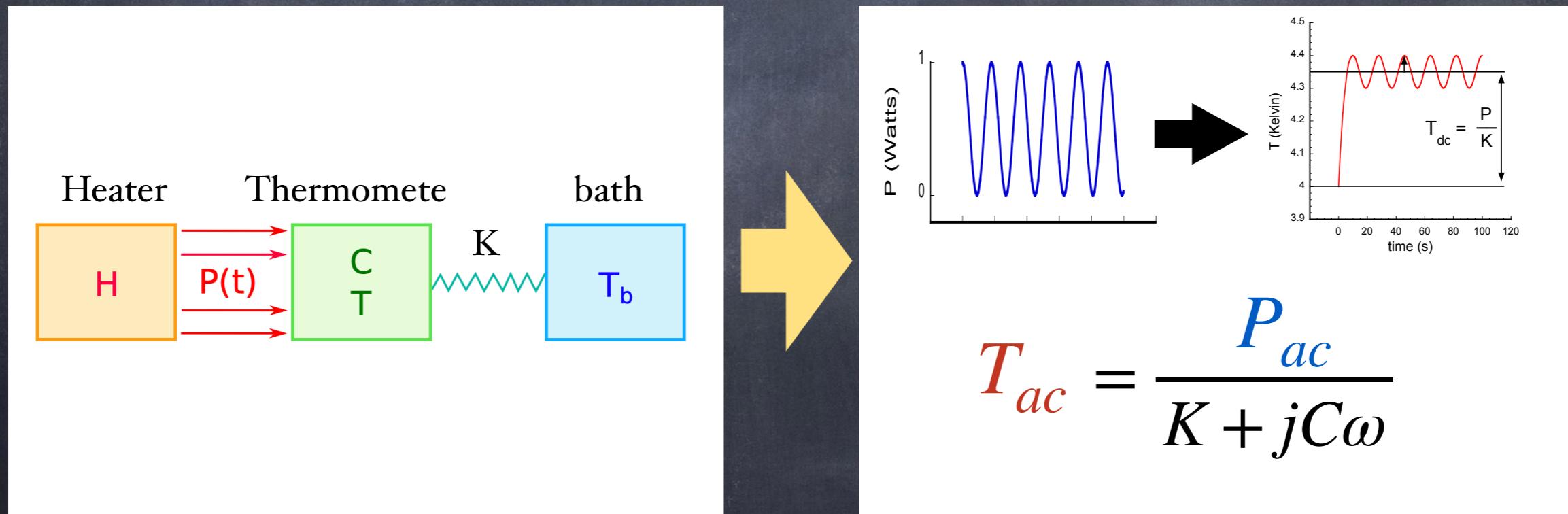
# Alternative calorimetry

applying an alternative **heating** power  $P_{ac}$  (at  $\omega$ )

to a sample of heat capacity **C**

linked to the thermal bath through **K**

and recording corresponding **temperature oscillations**  $T_{ac}$



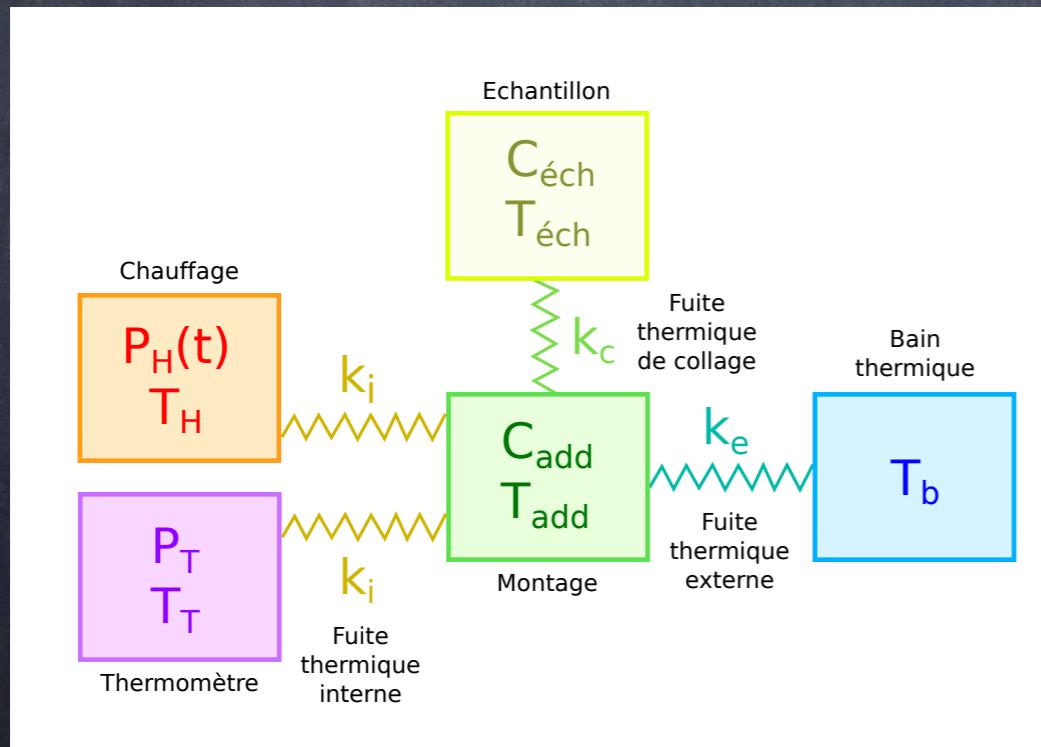
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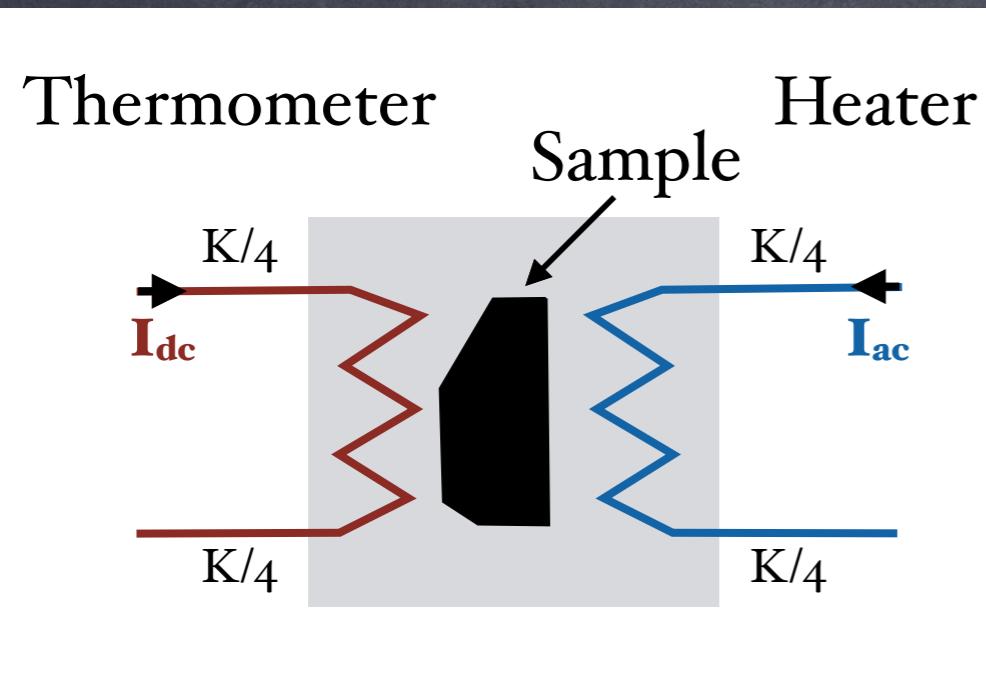
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Unfortunately life is a little bit more complicated (internal couplings)

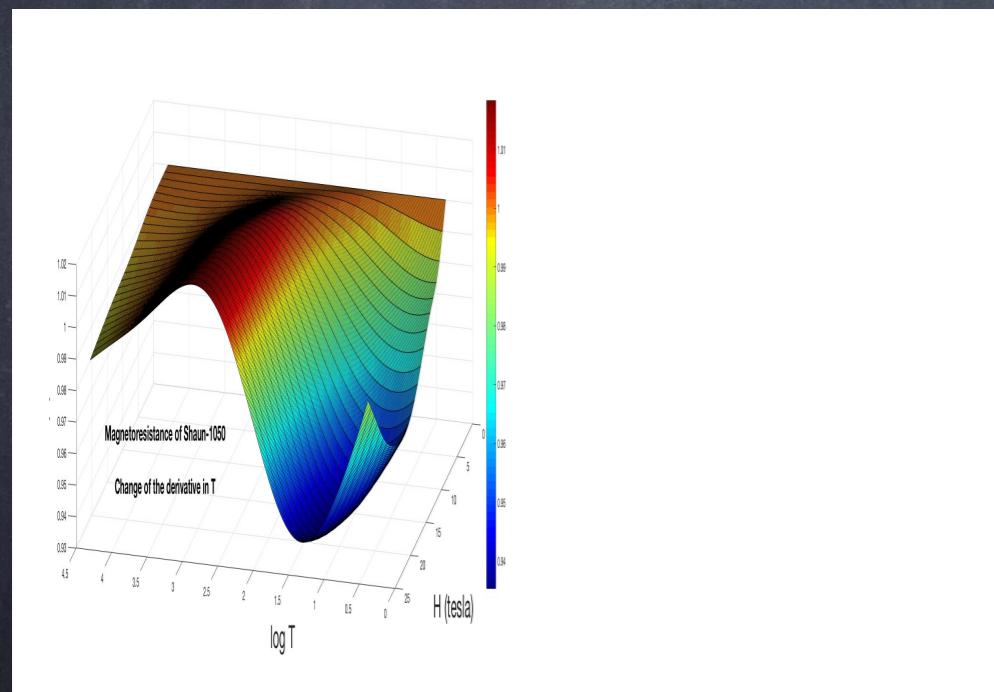
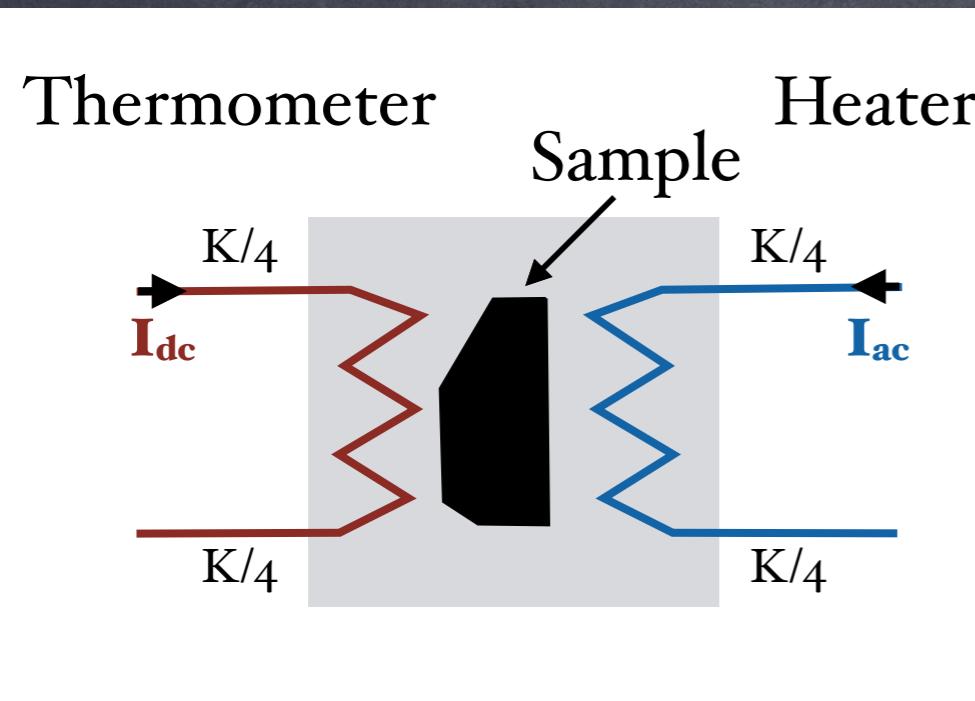
$$T_{ac} = \frac{P_{ac}}{K_{\text{eff}} + jC_{\text{eff}}\omega}$$

but  $C_{\text{eff}} \rightarrow C$  in the *good* conditions...



**HEATER** : resistance  $R_H$  (or optical fiber,...)

**THERMOMETER** :  $R_T$  (or thermocouple,...)



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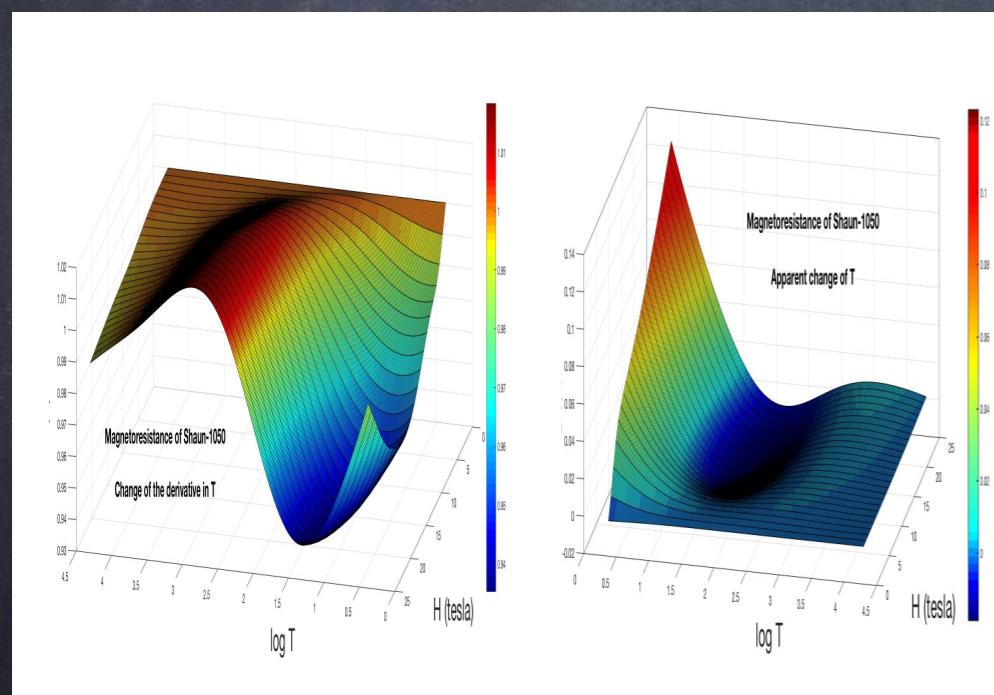
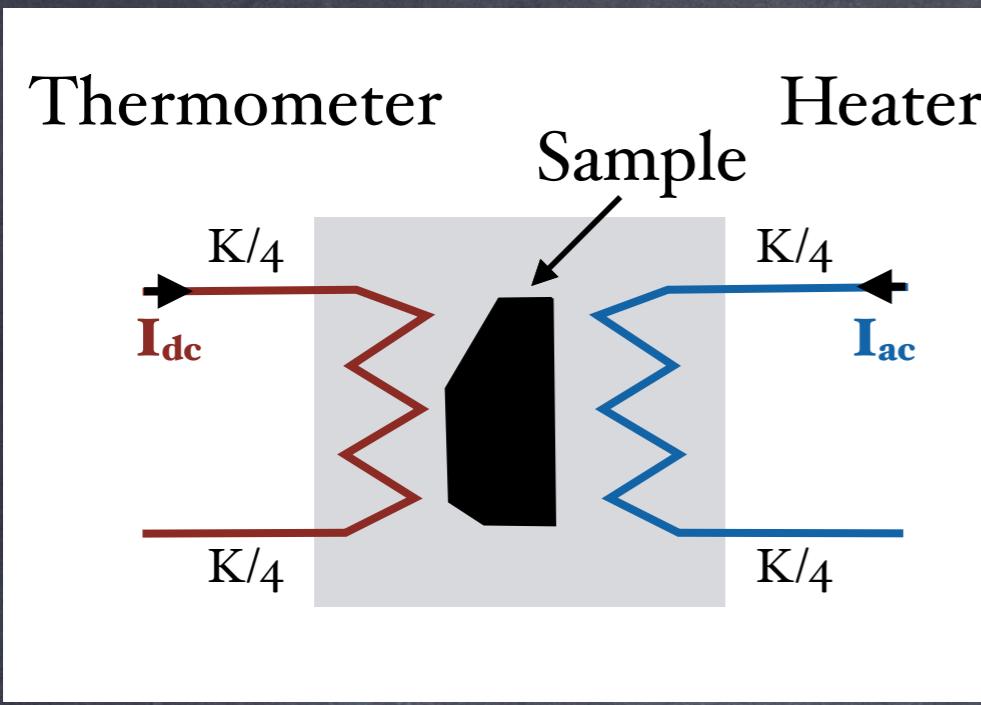
**THERMOMETER** :  $R_T$  (or thermocouple,...)

and this technique then requires

**very demanding calibrations**

for  $R(T, H)$

$$V_{dc} = R_T(T, H) I_{dc} \rightarrow T$$



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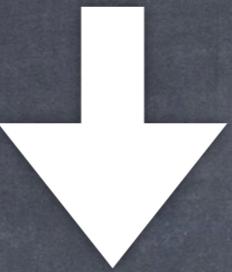
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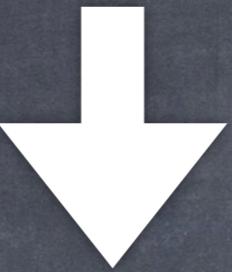
$$V_{dc} = R_T(T, H) I_{dc} \rightarrow T$$

**AND  $dR/dT$**

$$V_{ac} = \frac{dR_T}{dT}(T, H) T_{ac} I_{dc} \rightarrow C$$



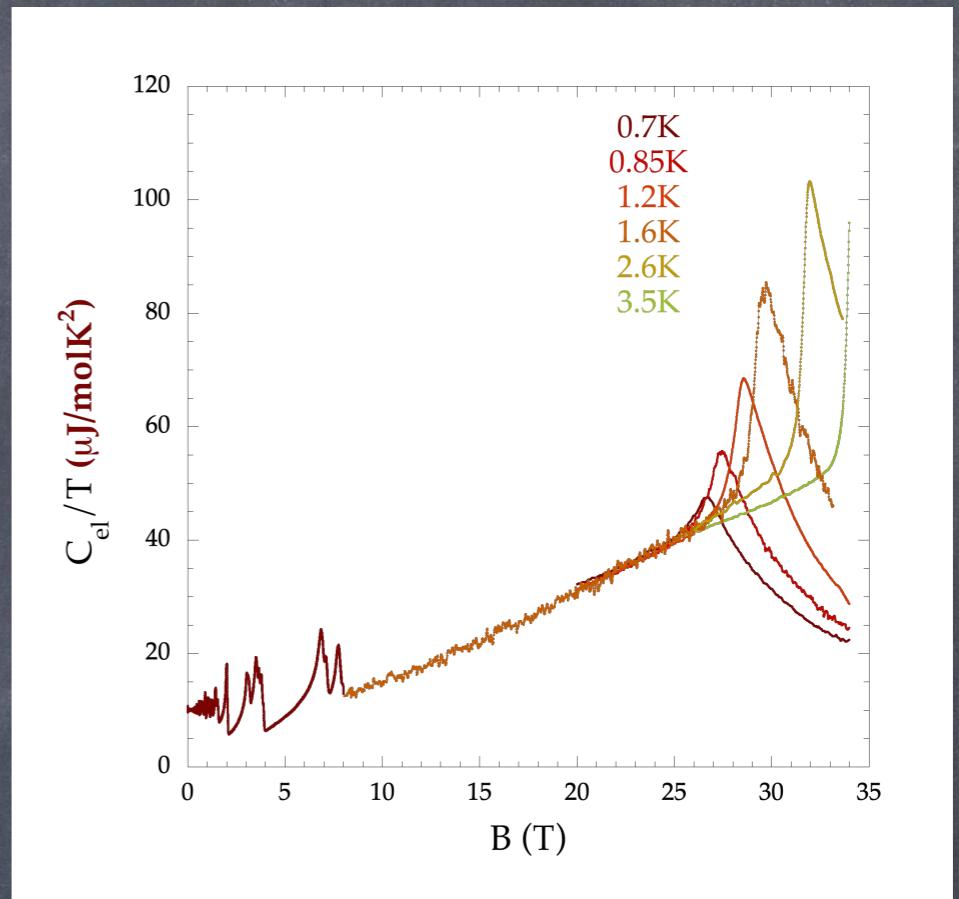
- **Small samples**  
a few milligrams down to ~ 10 micrograms (or less)
- **Continuous H and/or T sweeps**  
in **extreme conditions** : 36T-0.1K (even under pressure)
- **Good absolute accuracy (> 95%)**  
as deduced from measurements in ultra pure Cu (img)



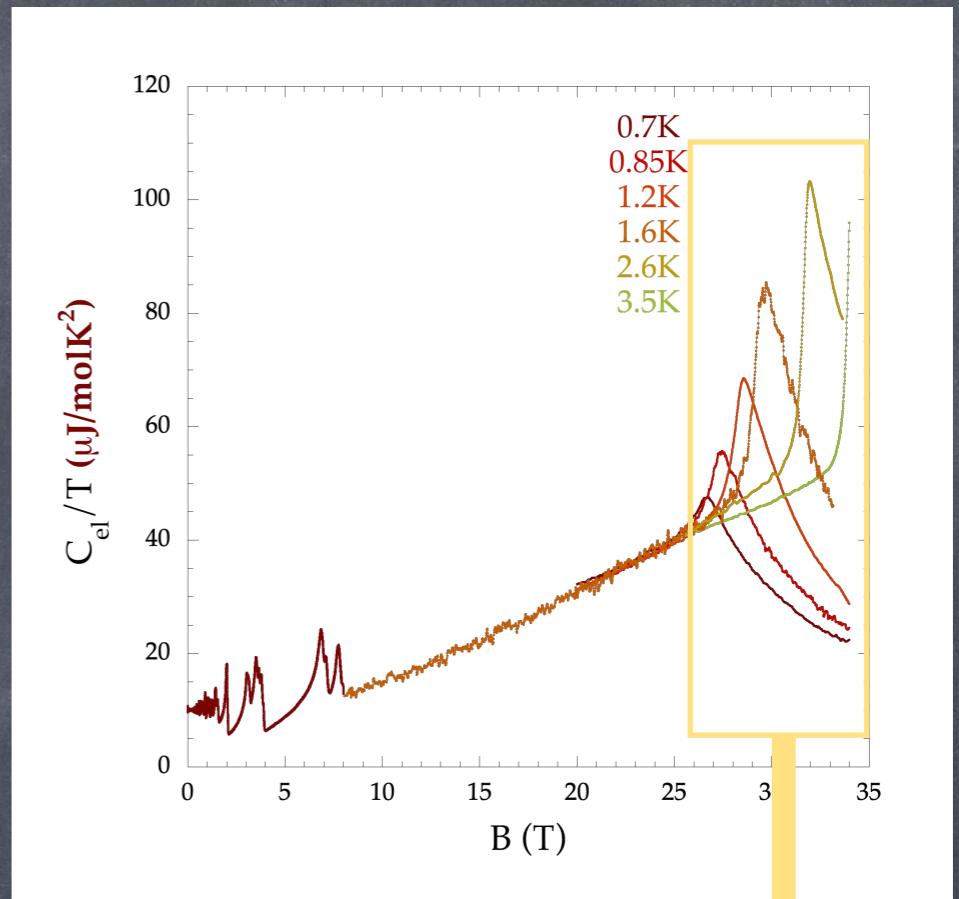
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as deduced from measurements in ultra pure Cu (1mg)
- **excellent resolution (down to a few  $10^{-5}$  of the total signal)**  
Lock-in detection, filters →  $\Delta C \sim 10^{-13} \text{ J/K}$

⇒ detection of **small *features*** in C/T

as for instance **quantum oscillations**  
in semimetals (Graphite)



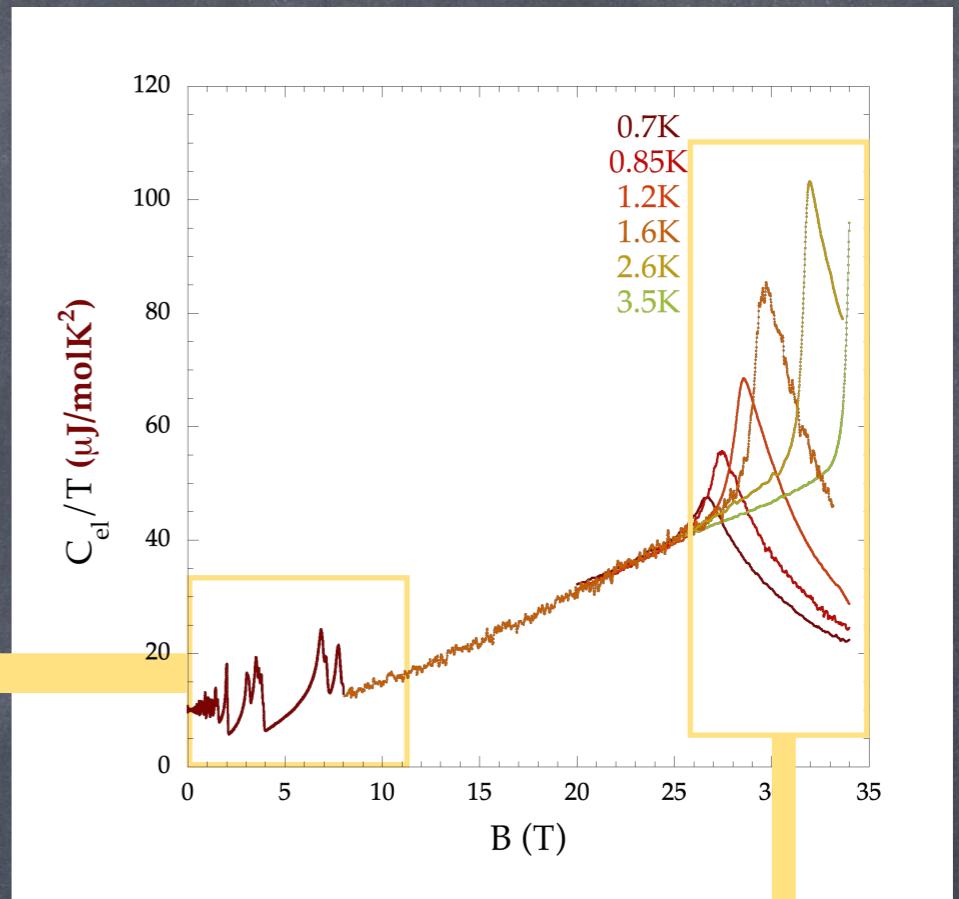
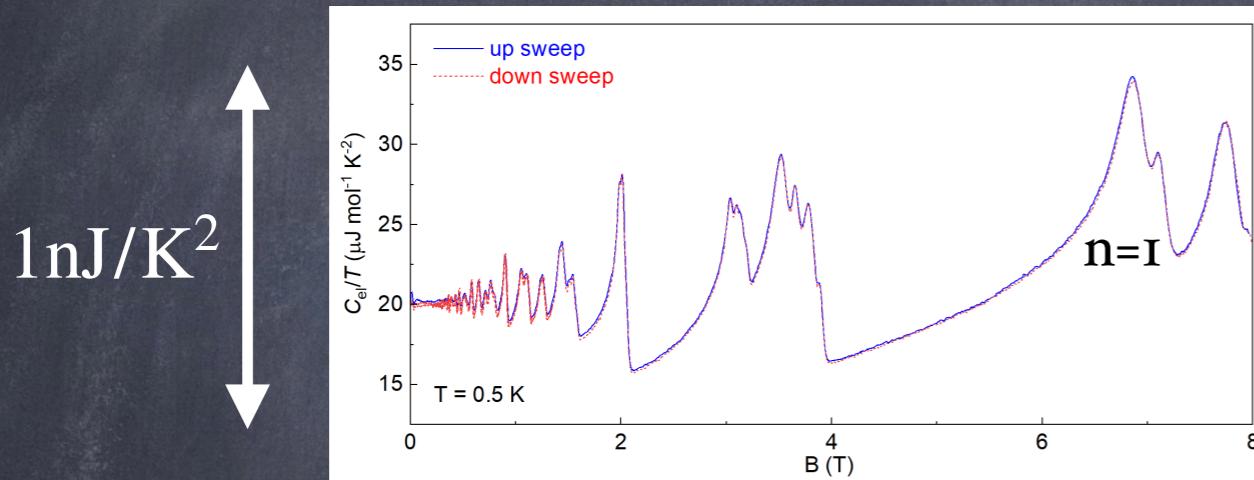
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Electronic phase  
transition in the  
quantum limit (1D)  
Marcenat *et al.* PRL 2021

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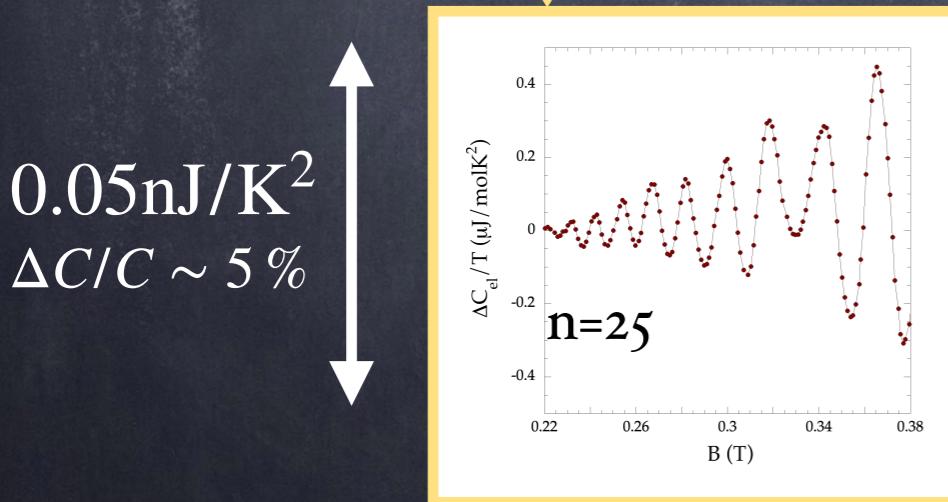
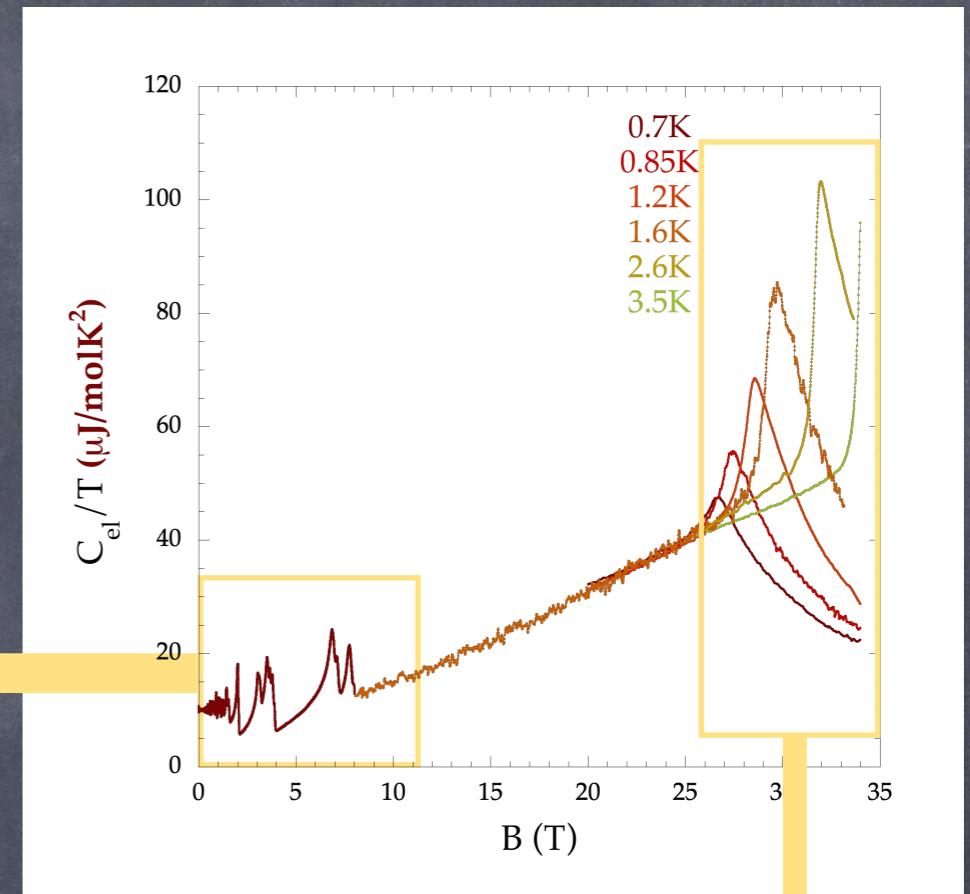
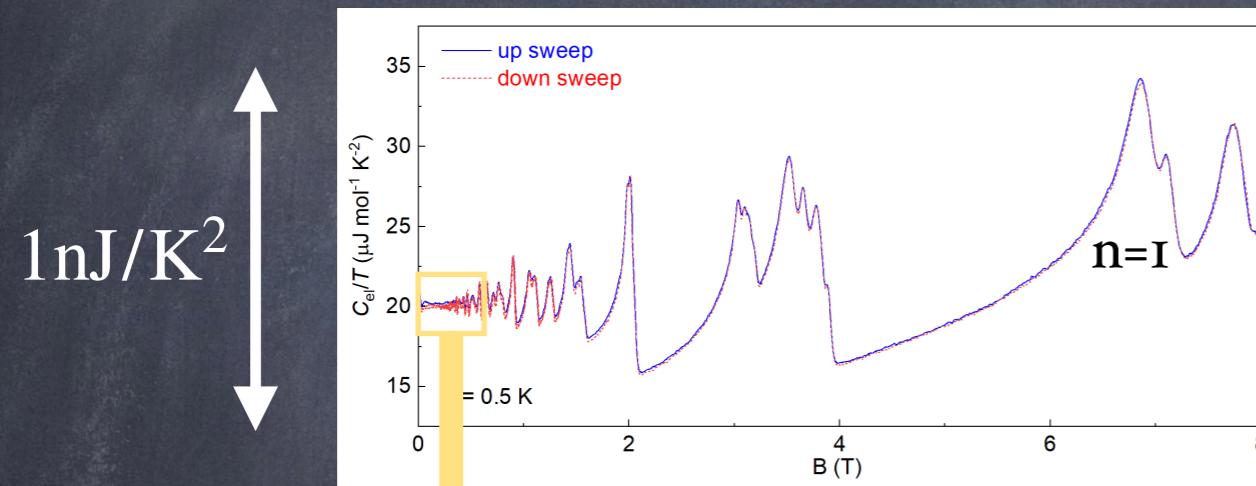
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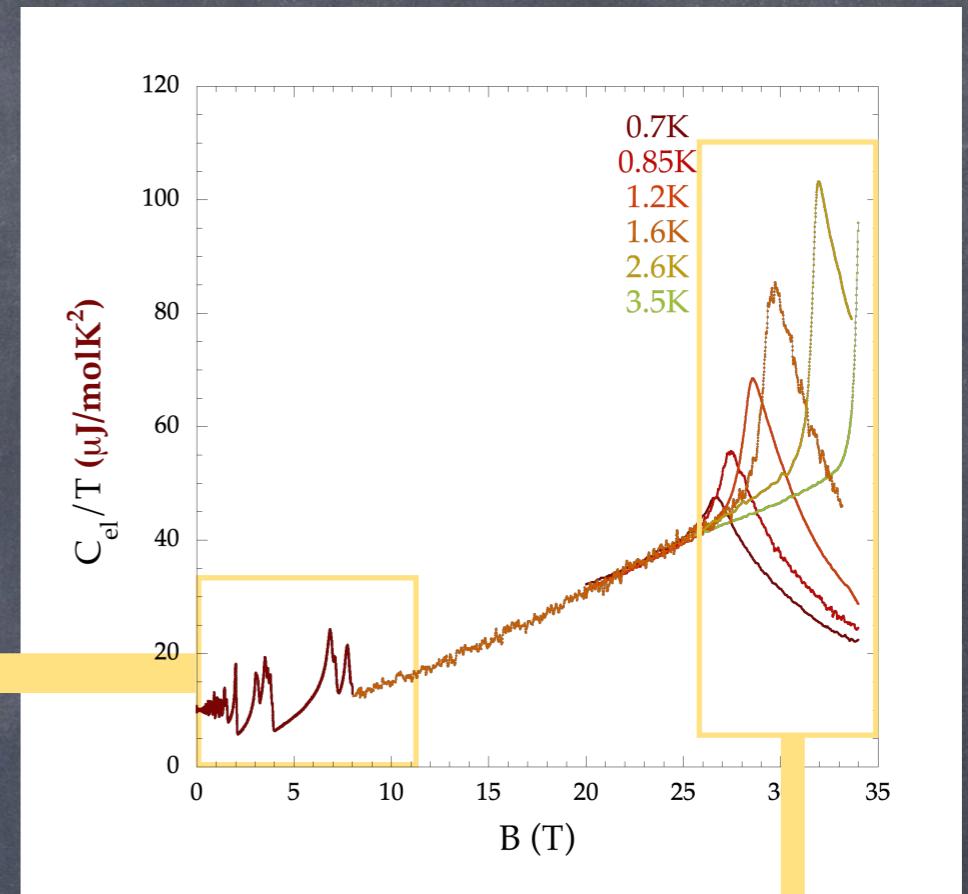
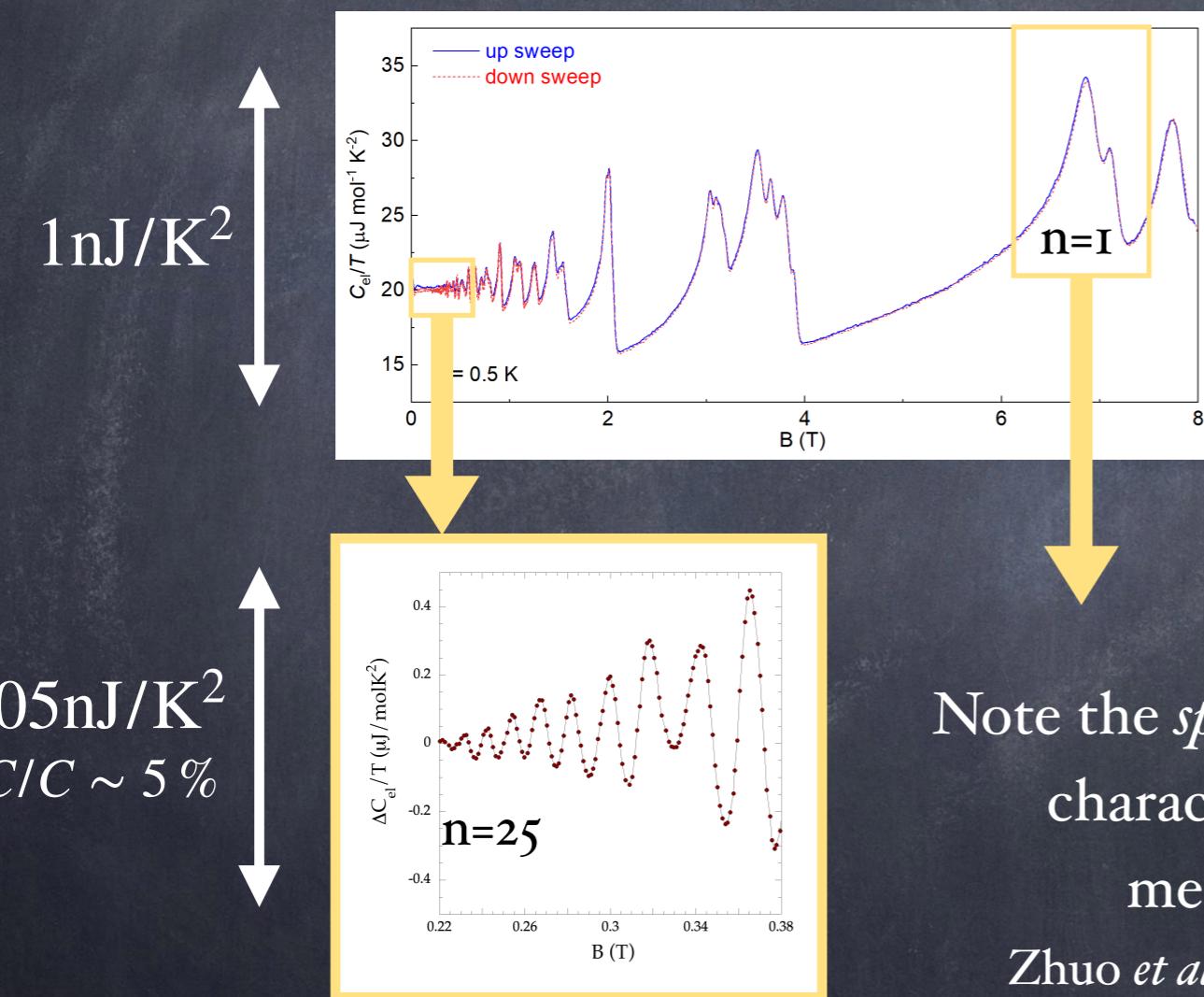
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Note the *splitting* of the peaks  
characteristic of C/T  
measurements

Zhuo *et al.* Nature Com 2023

Electronic phase  
transition in the  
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# Outline

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Things that we do understand and that we do **NOT** understand on :

- **The FeSe nematic superconductor**  
H-T phase diagram and T & H dependence of the gap structure
- **Thermodynamic properties of the normal state in cuprates**  
Quantum criticality at the onset of the pseudo-gap and charge order

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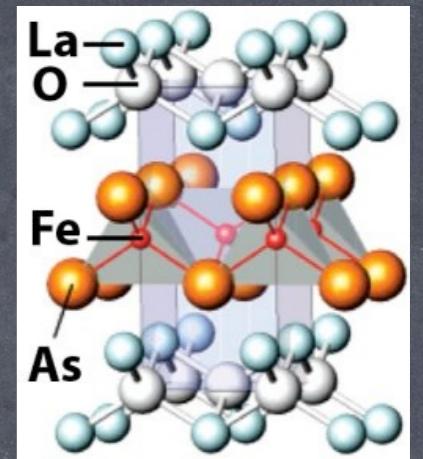
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H-T phase diagram and T & H dependence of the gap structure

# FeSe = iron based superconductor

attracted considerable interest due to the interplay between superconductivity and magnetism

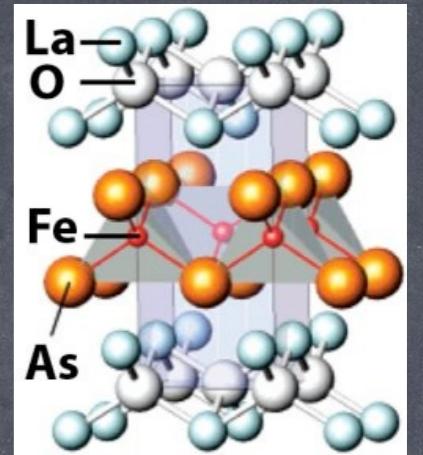
and  $T_c$  rising up to  $\sim 50\text{K}$  in  $\text{Gd}(\text{O},\text{F})\text{FeAs}$  (so called I<sub>III</sub>-phase)



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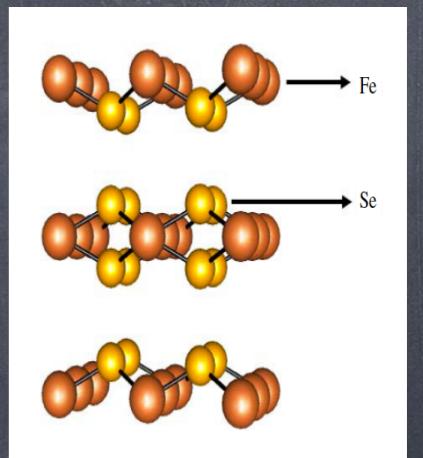


- **FeSe** = c-axis stacking of SC layers **without** any charge reservoir.
- Moderate  $T_c \sim 9$ K, but **very low carrier concentration**

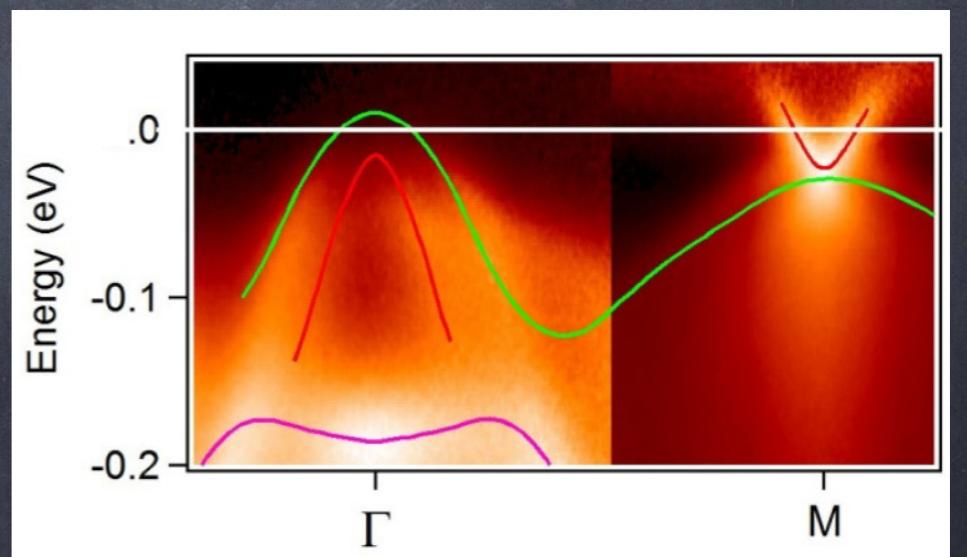
**semi-metal** : small *e+hole pockets*

$E_F \sim \Delta$  : *high*  $T_c$  (two gap-) superconductor

at the verge of a Bose Einstein Condensation



L.Fanfarillo *et al.*, PRB 2016



## interesting vortex physics

It all started in the 90s in high  $T_c$  cuprates

⇒ Strong thermal fluctuations

$$G_i = (1/8)(k_B T_c / \epsilon_{\text{cond}})^2 \sim 10^{-2}$$

where  $\epsilon_{\text{cond}} = \epsilon_0 \xi$  with  $\epsilon_0 = \Phi_0^2 / 4\pi\lambda^2$

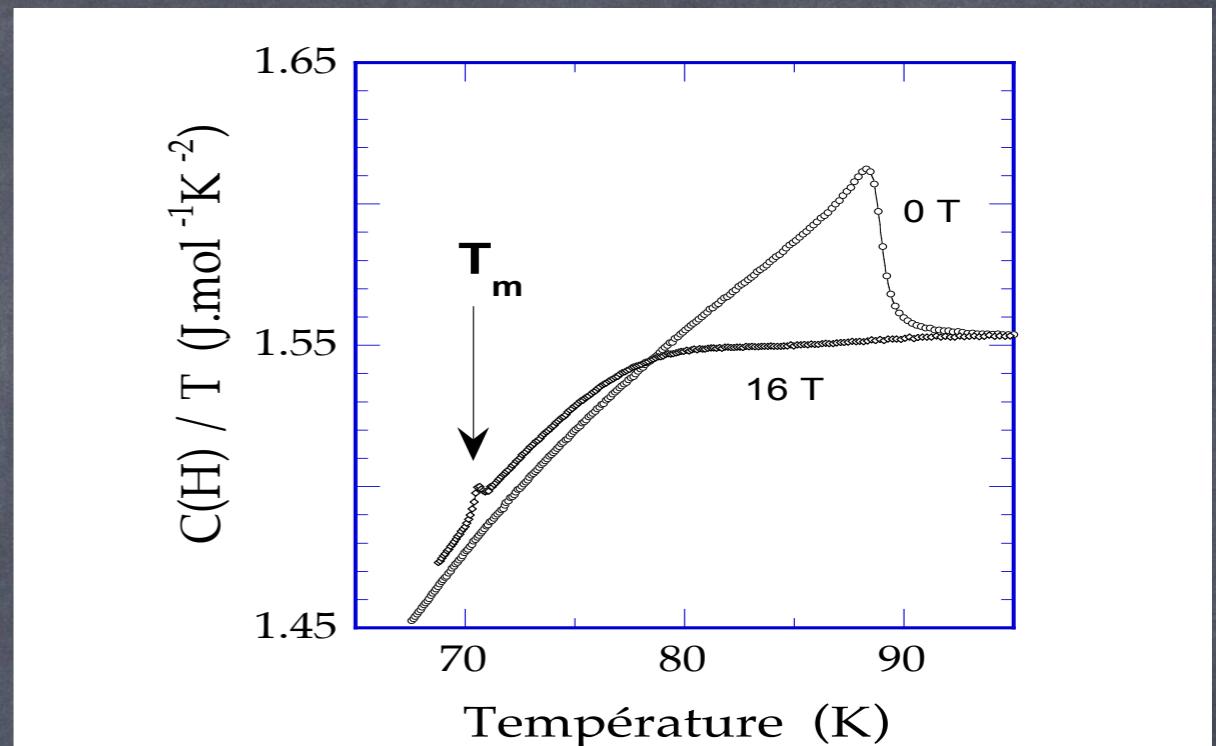
⇒ **melting** of the vortex solid

**Sharp (1<sup>st</sup> order) peak in C/T**

... but observed only in (a few)

high quality optimally doped

YBaCuO single crystals



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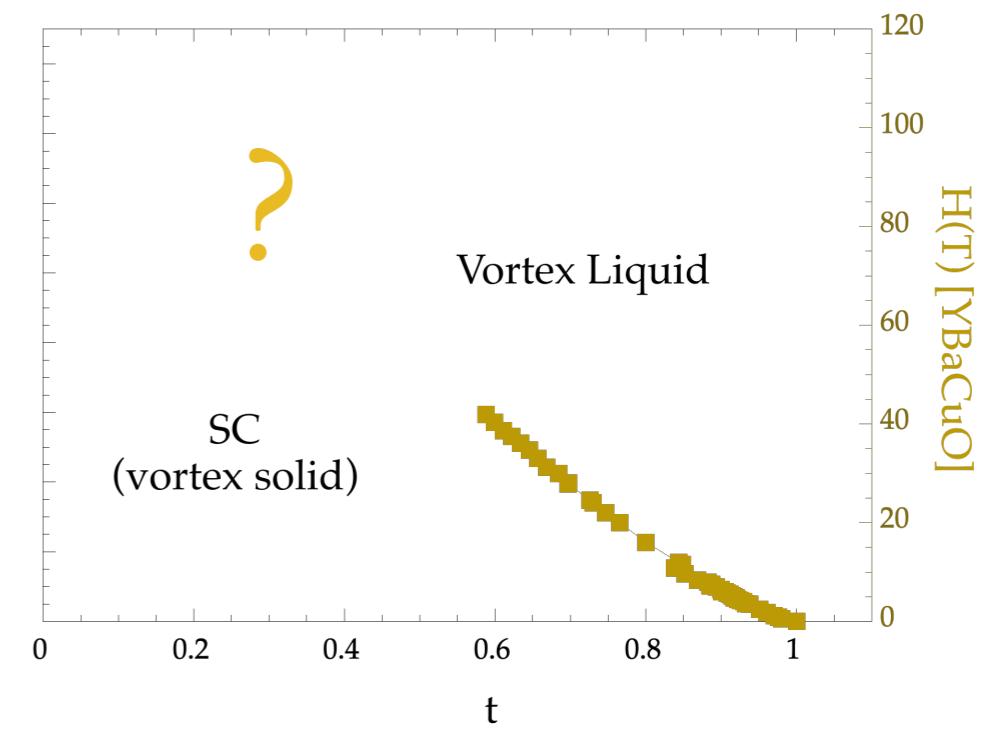
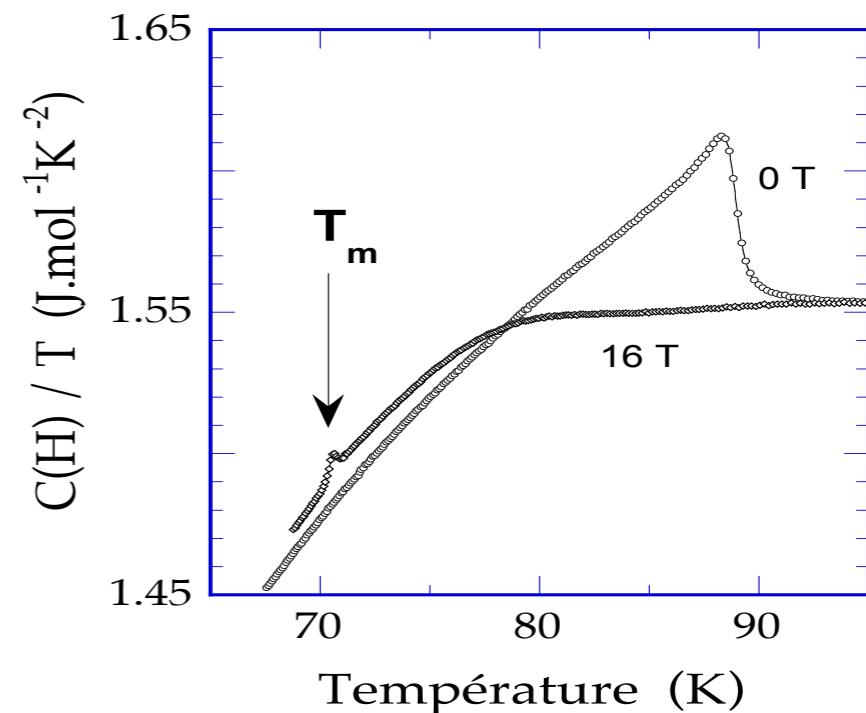
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The melting line can only be  
tracked down to  $\sim T_c/2$



**FeSe** : Small superfluid density

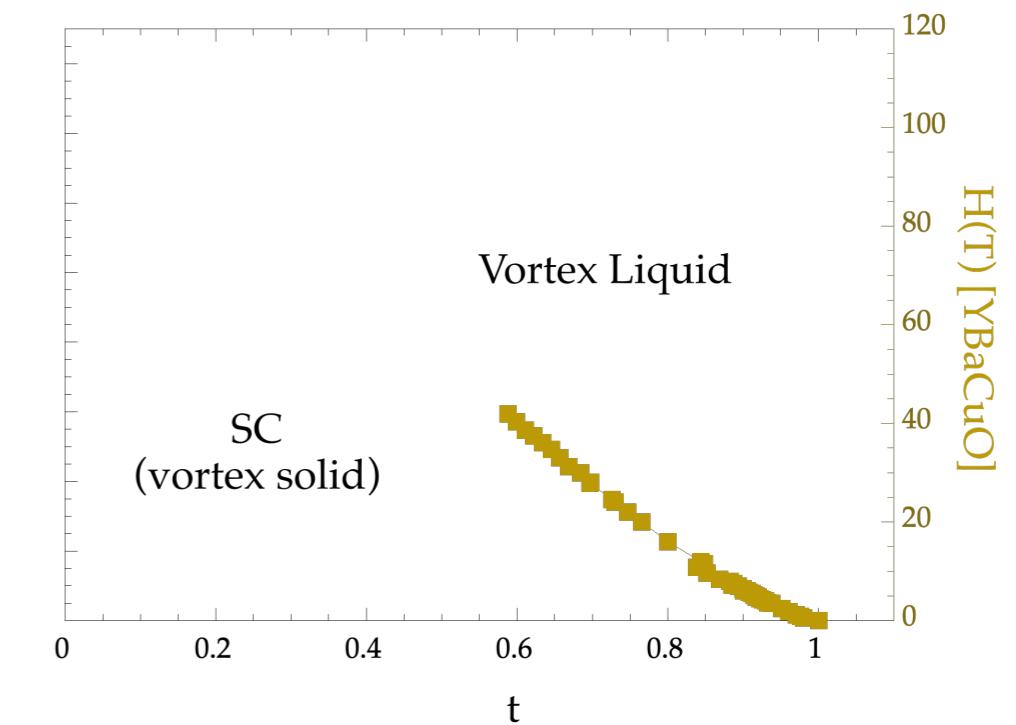
⇒ large  $\lambda$  value

⇒ **Very** small condensation energy

$$\epsilon_{\text{cond}} = \epsilon_0 \xi_c \sim 160 \text{ K}$$

⇒ (still a) **Large Gi value**

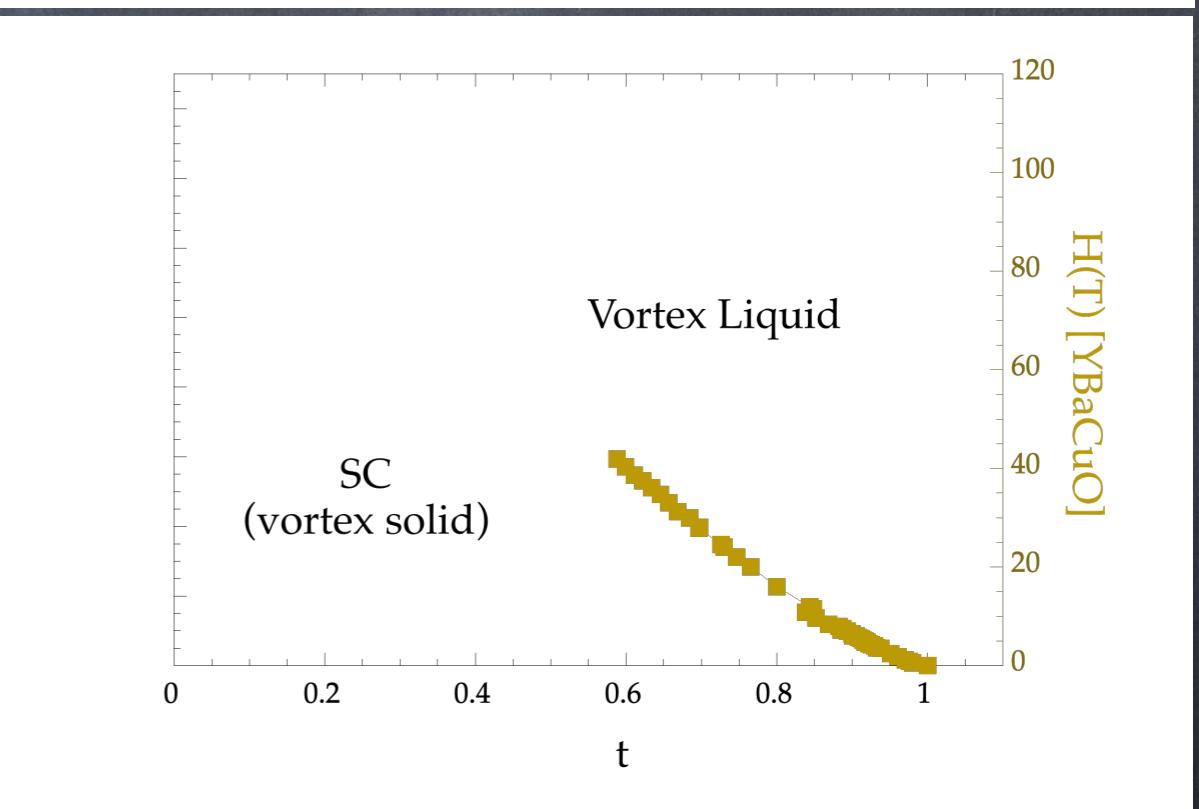
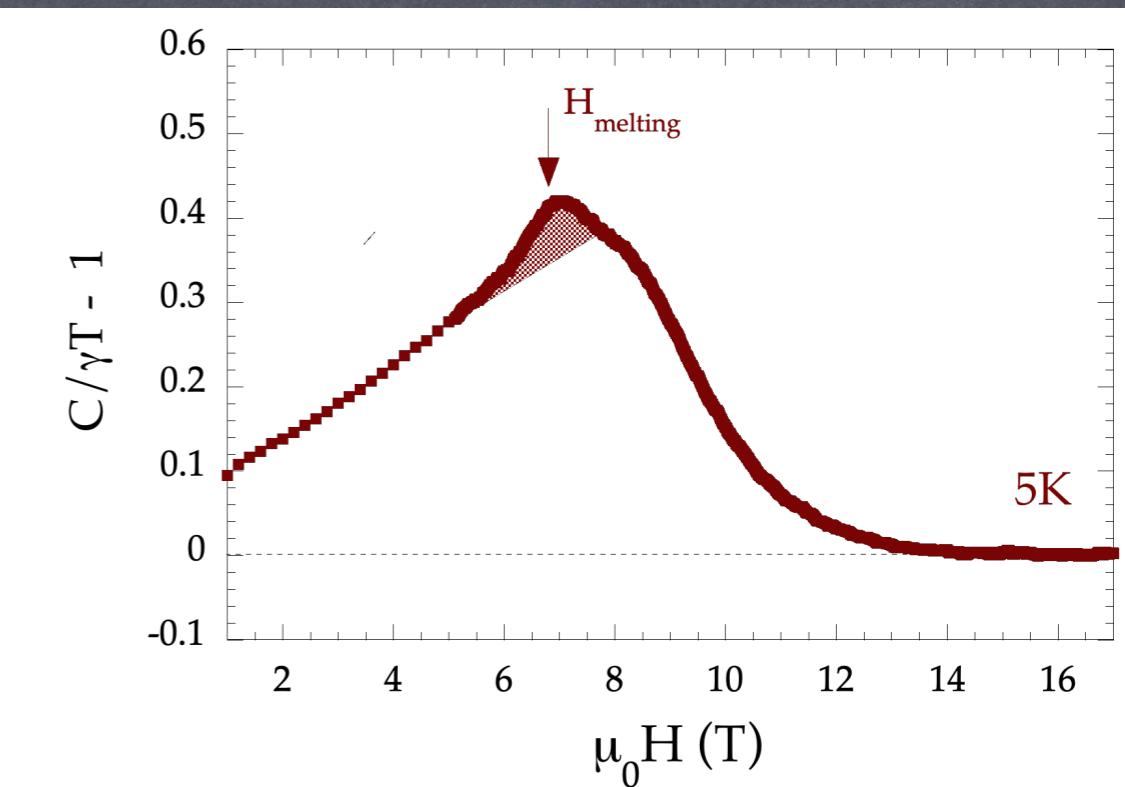
	<b>FeSe</b>	Nb	YBaCuO
$T_c$	9	9	92
$\lambda$ (A)	5000	400	1200
$\epsilon_0$ (K/A)	8	1200	140
$\xi_c$ (A)	20	400	4
$\epsilon_{\text{cond}}$ (K)	160 !	$5 \cdot 10^5$	560
Gi	$10^{-3}$	$3 \cdot 10^{-9}$	$5 \cdot 10^{-3}$



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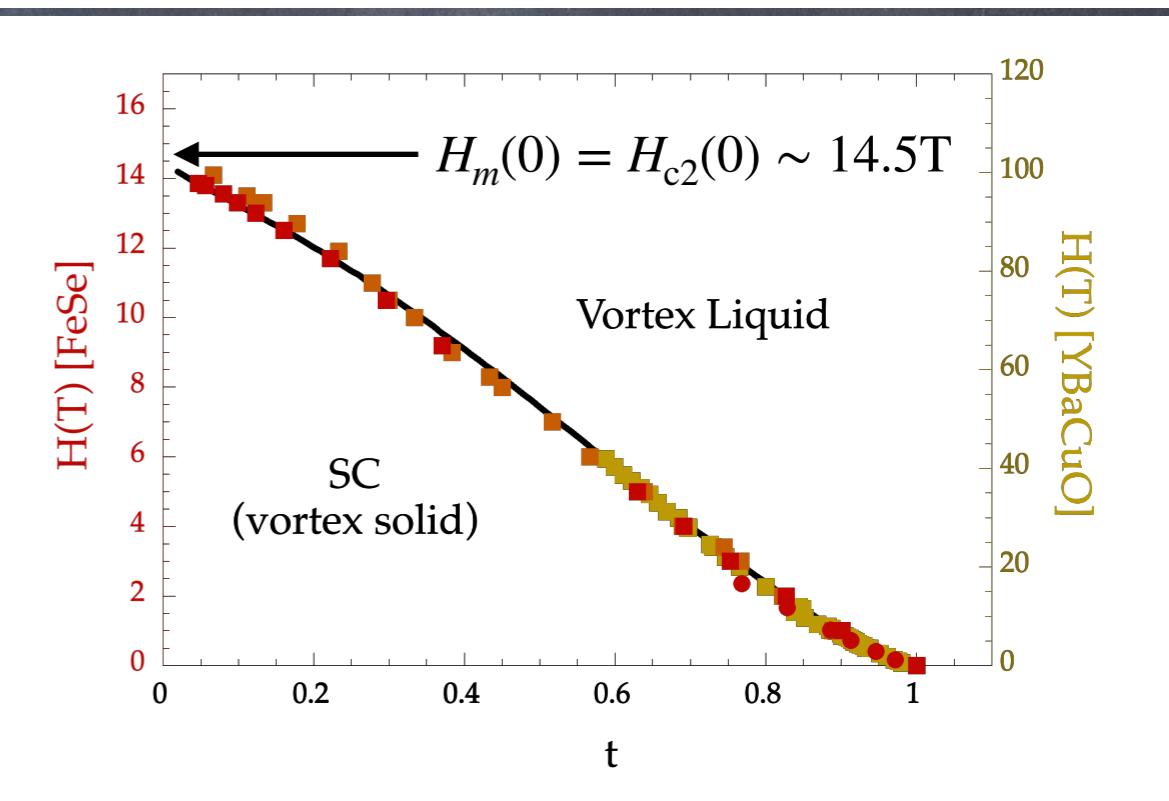
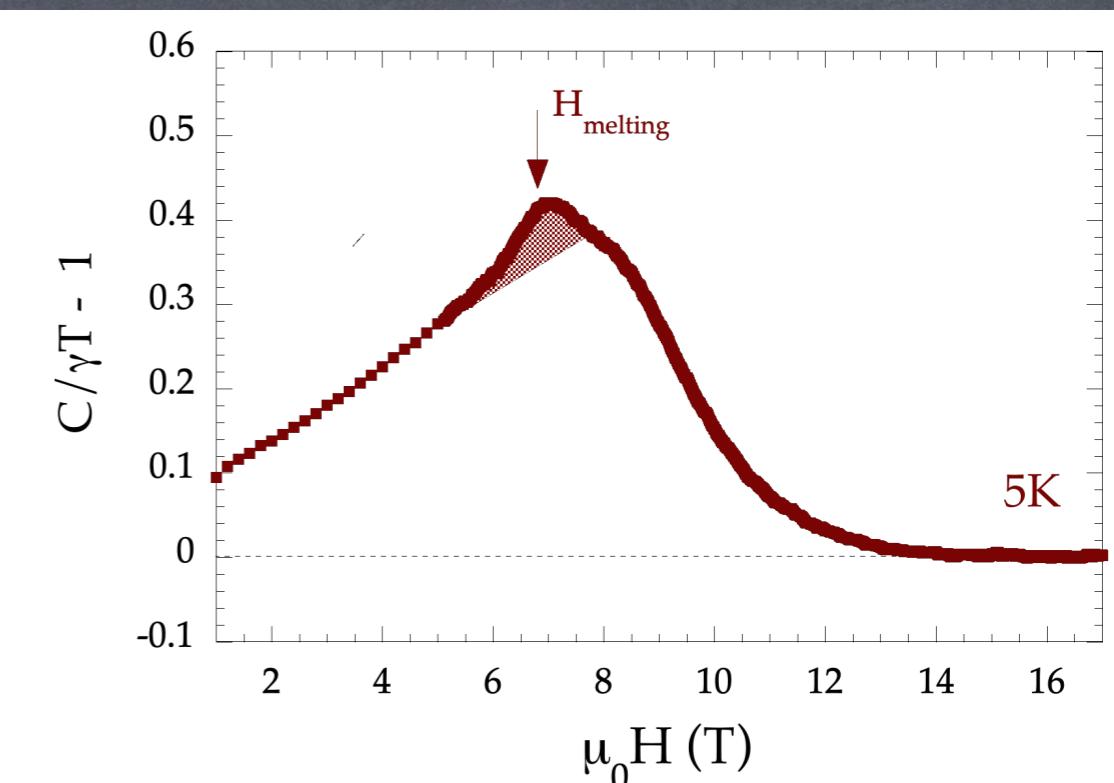
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...which can be studied (and well fitted)

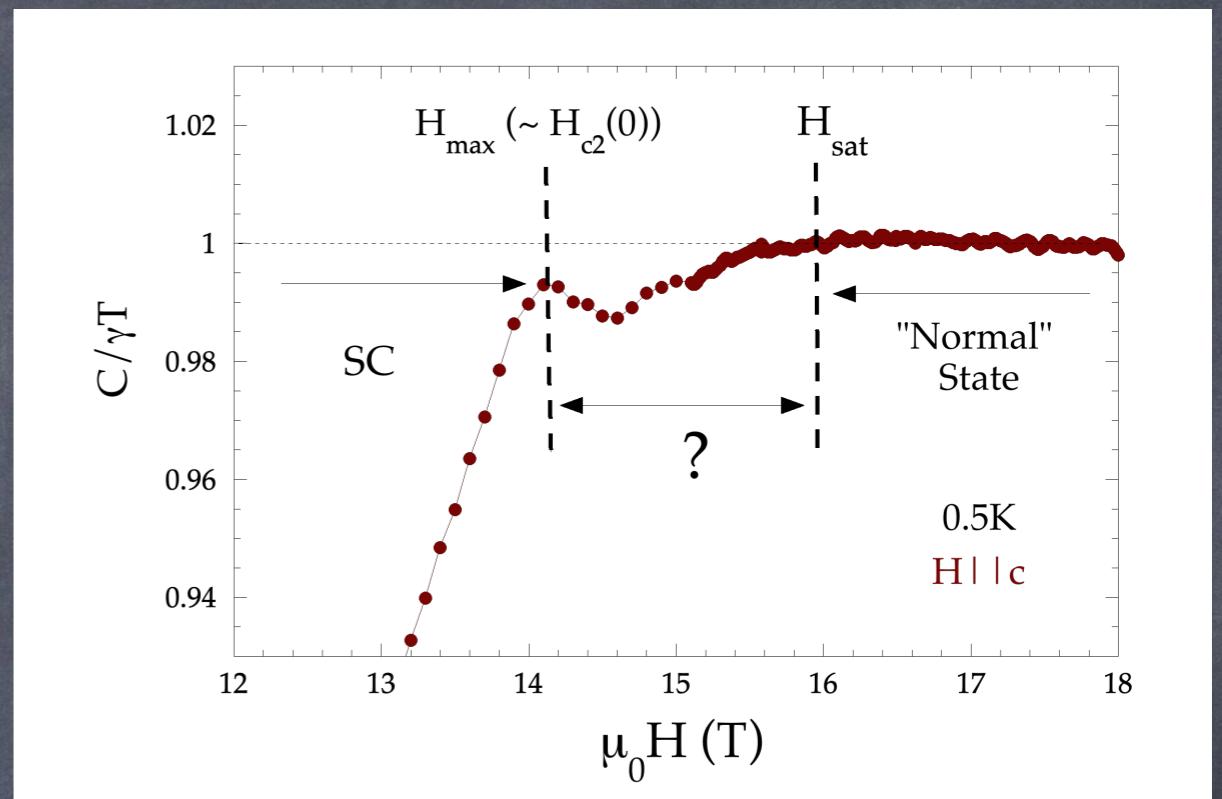
**down to the lowest T**

$$(H_{c2}(0) \sim 14.5 \text{ T})$$

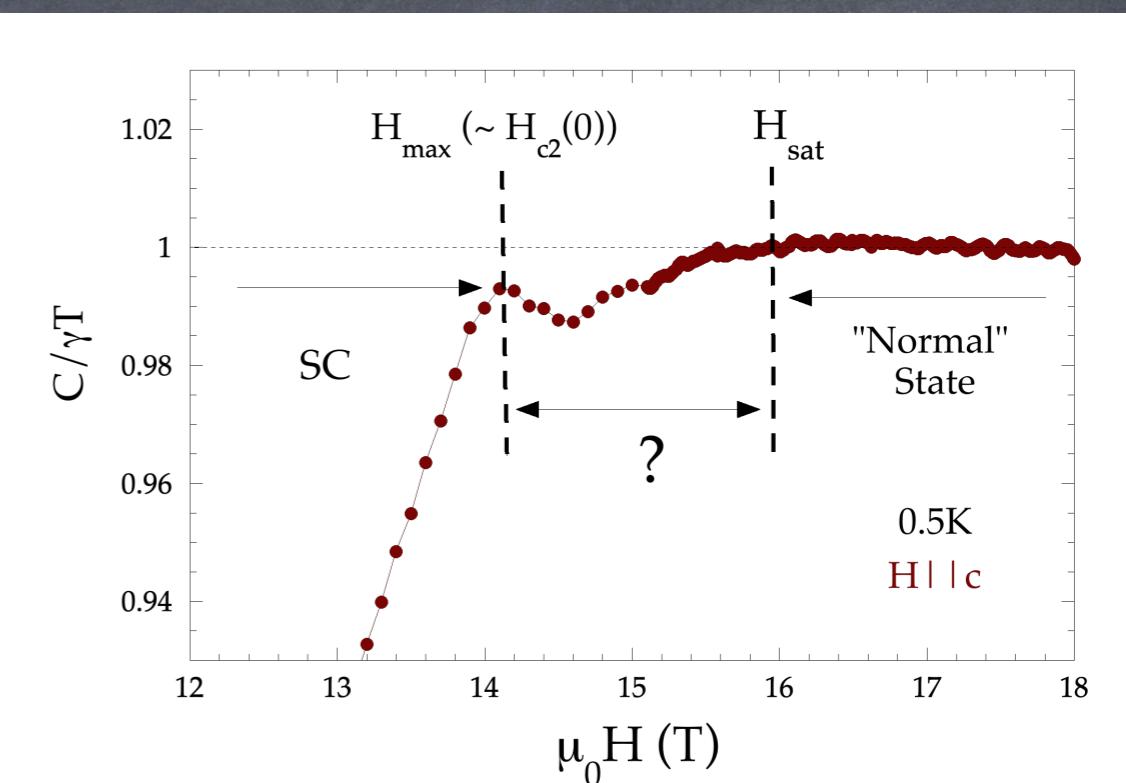
(interplay with paramagnetic limit for  $H \parallel \text{ab}$   
see F.Hardy *et al.* PRR 2020)



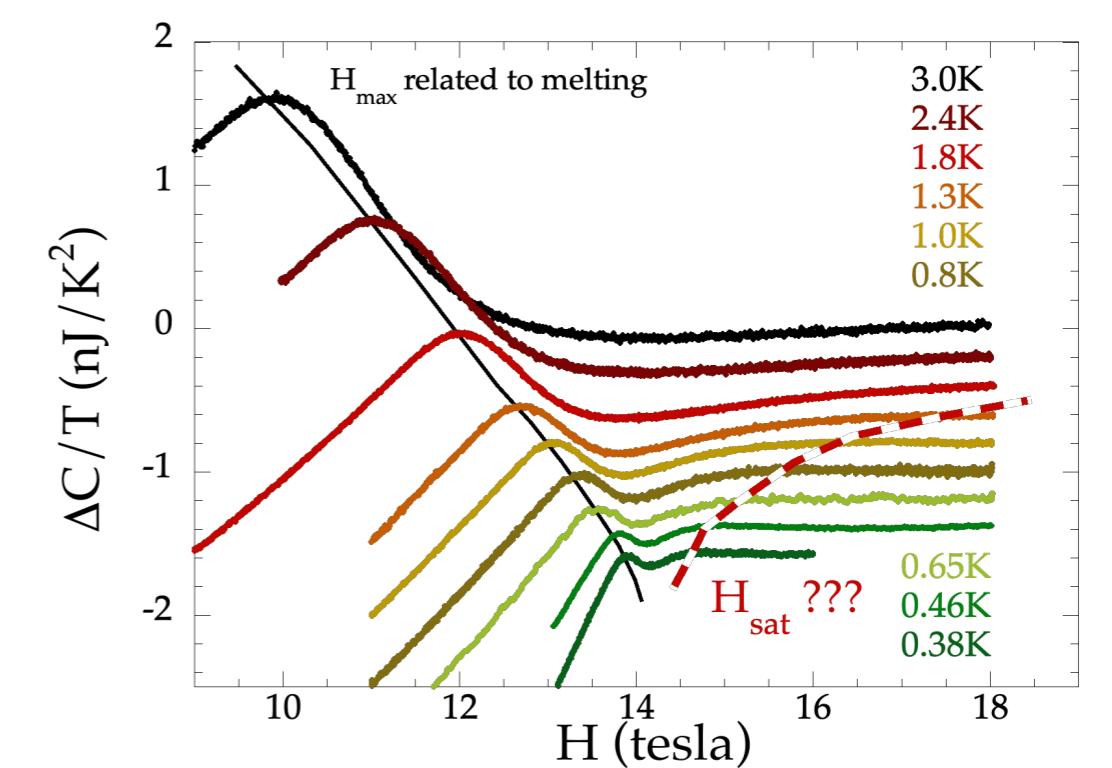
but  $C/T$  still increases with  $H$   
**well above  $H_{c2}(0)$  ???**  
and only saturates above  $H_{\text{sat}}$



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**Nature of the  $H_{\text{sat}}$  field ?**  
 increases with T !  
 ( → 22 T @ 1.8K)  
 Signature of an electronic transition ?



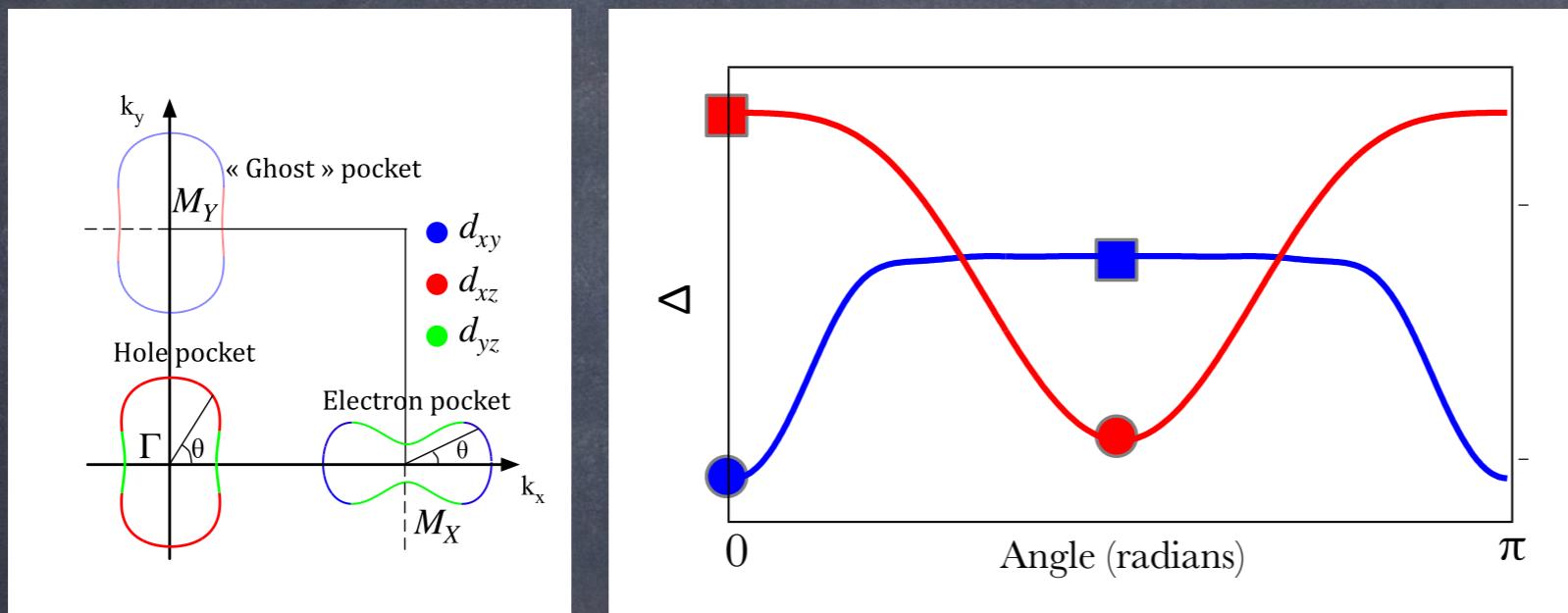
- No magnetic order (still a structural phase transition)  
but orbitally ordered **nematic state** (breaking of the  $C_4$  symmetry )

Mukherjee *et al.* PRL 2015, Aichhorn *et al.* PRB 2010, Yamakawa *et al.* PRX 2016, Watson *et al.* PRB 2017

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## **C<sub>2</sub> anisotropy of (the spectral weight and) superconducting gaps**



H.Cercellier *et al.*, PRB 2019 and references therein

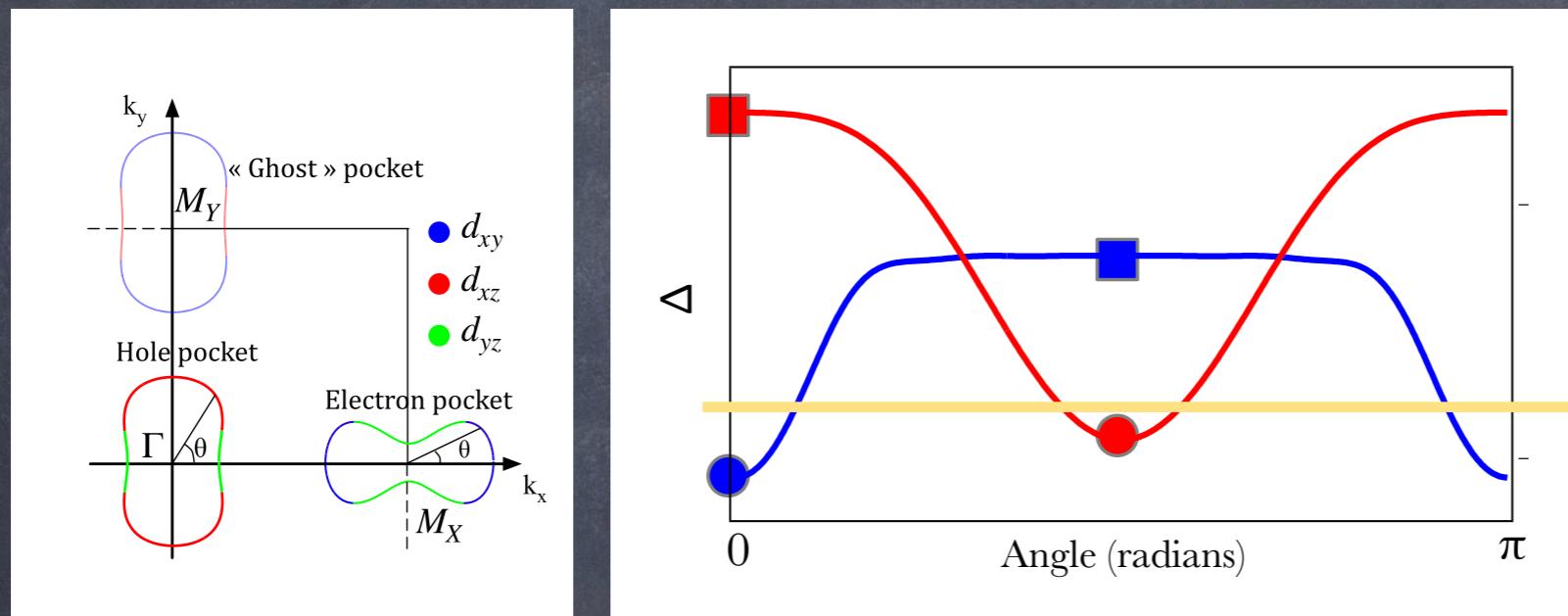
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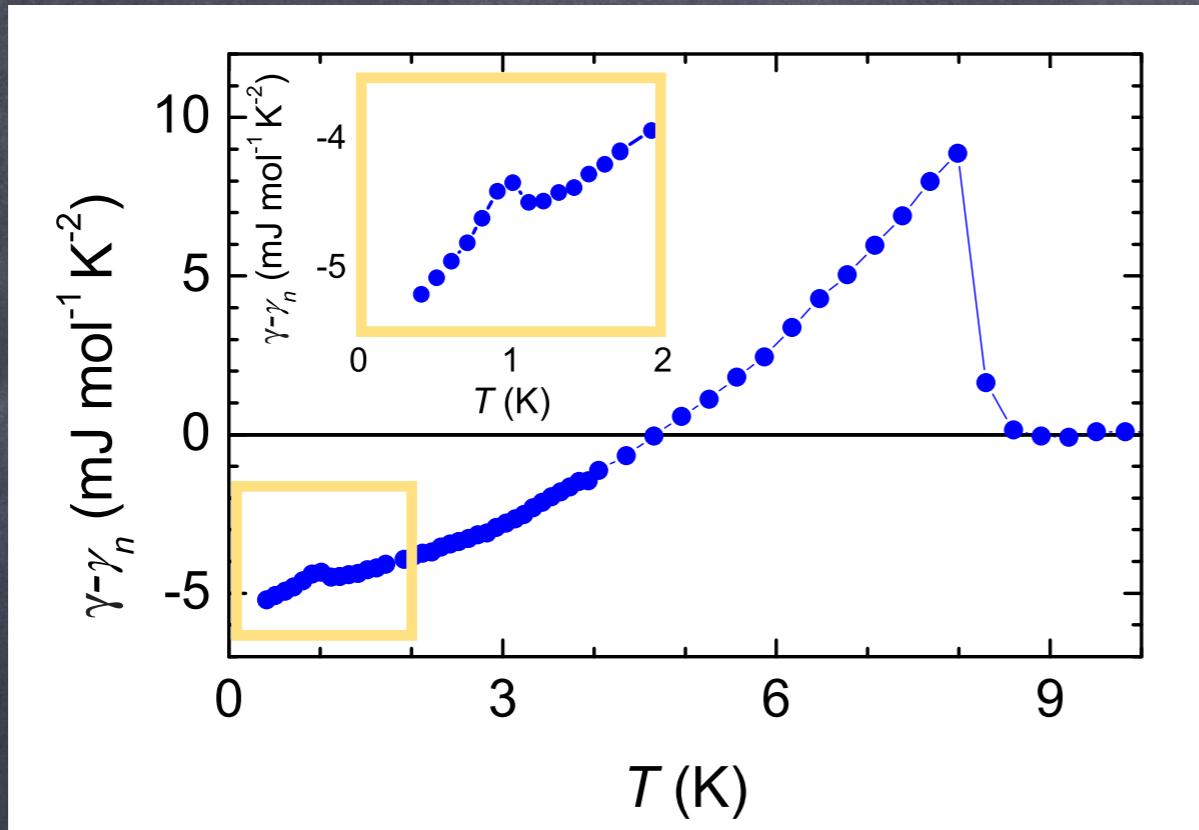
$\Delta_{\text{hole}}^{\max} \sim 2 - 3 \text{ meV}$   
 $\Delta_{\text{elec}}^{\max} \sim 1 - 2 \text{ meV}$   
 $\Delta_{\text{hole}}, \Delta_{\text{elec}} < 0?$   
 accidental nodes ?

Nematic order couples the s and d wave harmonics of the gap (**s+d** symmetry)

$\Delta_s$  and  $\Delta_d$  sensitive to **nematicity and intra/interband couplings**.

→ *Accidental* gap nodes can show off if  $\Delta_d > \Delta_s$

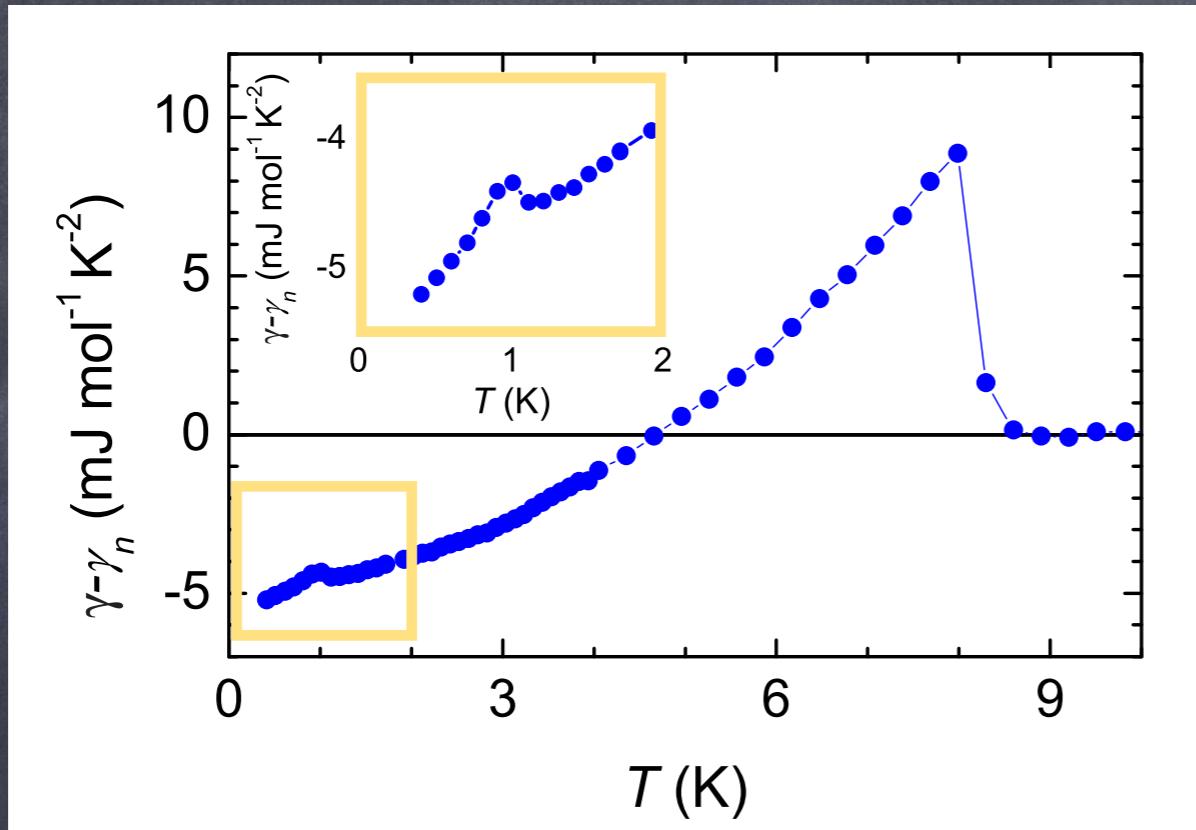
Moreover : *anomalous* specific heat anomaly **around 1K**  
(but not observed in all samples ?)



G.Y.Chen *et al.* PRB 2017

possible  $s + d \rightarrow s + e^{i\theta}d$   
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The symmetry of the gap is still an open question  
which can be probed by specific heat measurement  
in **rotating**  $H \parallel \text{ab}$  (Oxy plane)

DOS (=C) maxima when Doppler shift :  $\vec{v}_s \cdot \vec{k}_F \sim \Delta$

velocity of vortex screening  
current = rotating field

(anisotropy of)  
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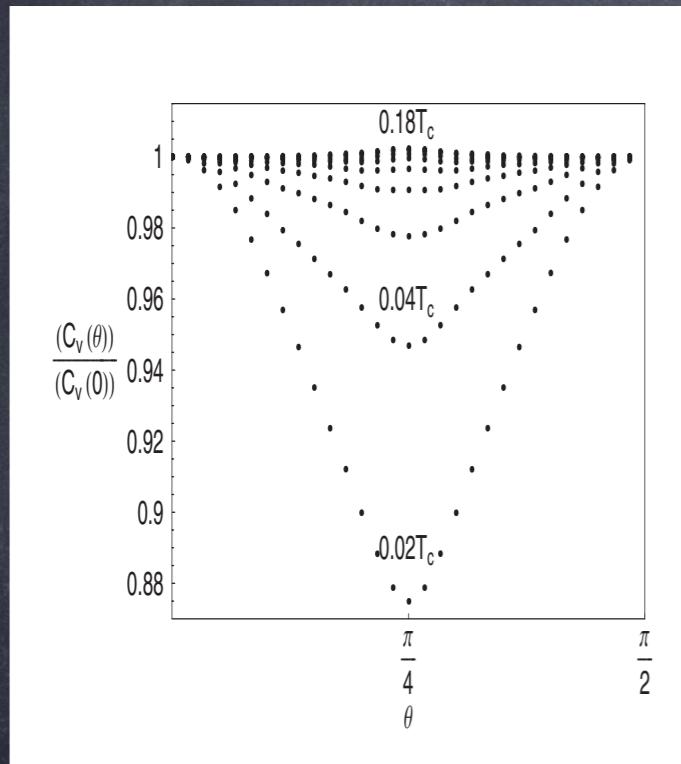
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However  
 $\Delta C/\gamma T < 1\%$   
 above  $T_c/10$   
 and  $\pi/4$ -shift  
 $(\min \Leftrightarrow \max)$   
 for  $T \sim T_c/10$

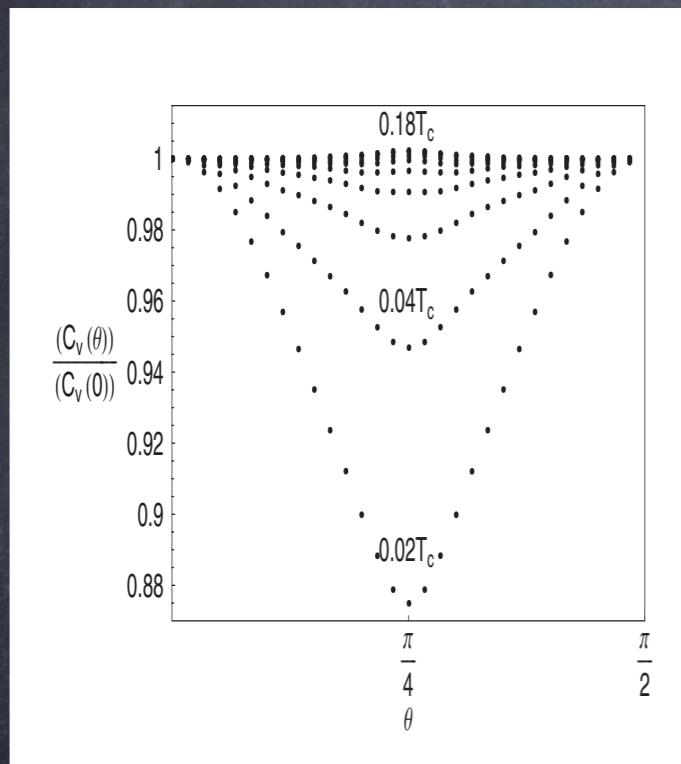
Numerical calculations  
 d-wave gap  
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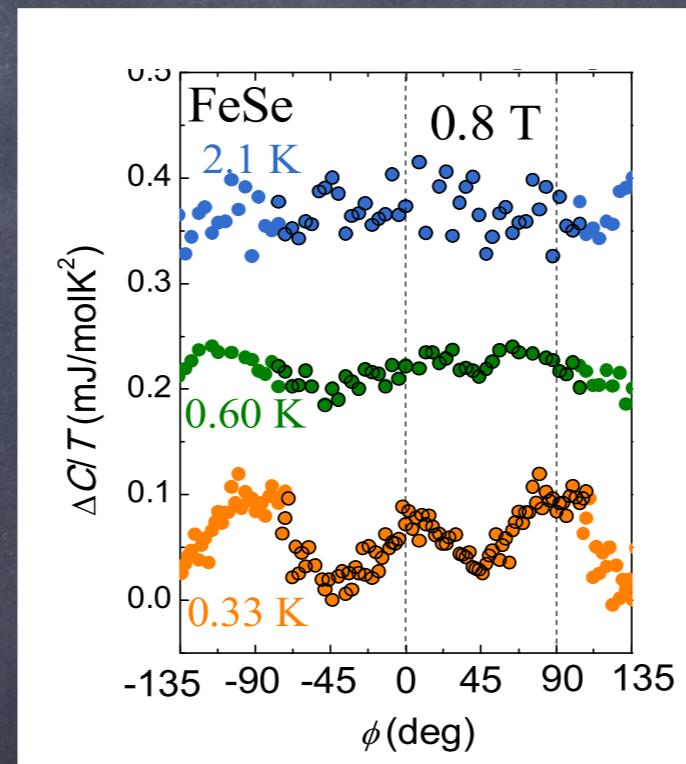
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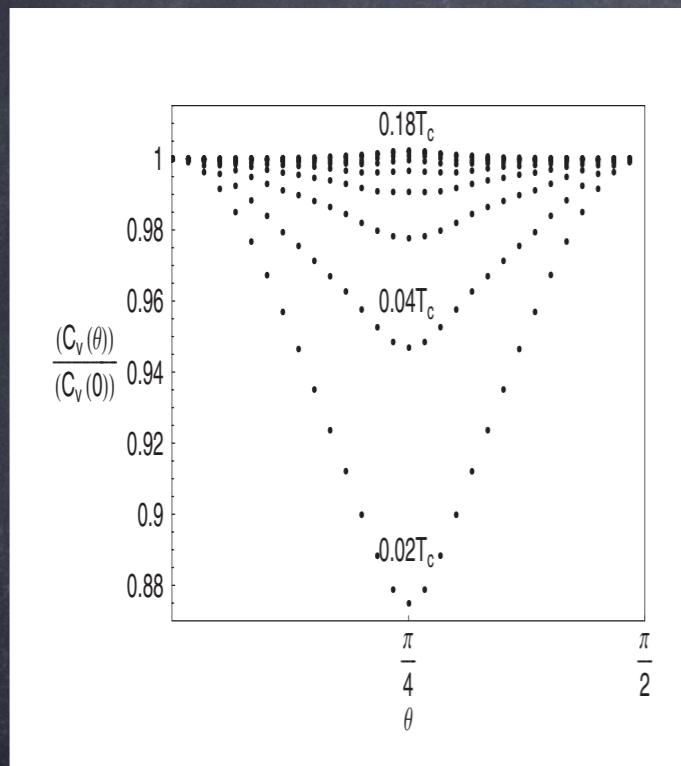
Observed in FeSe  
**but only low T/H**  
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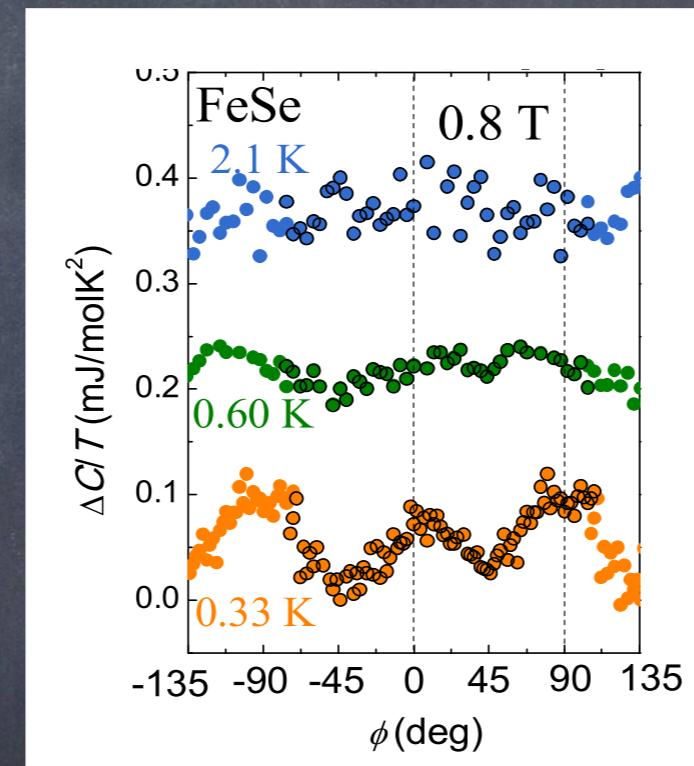
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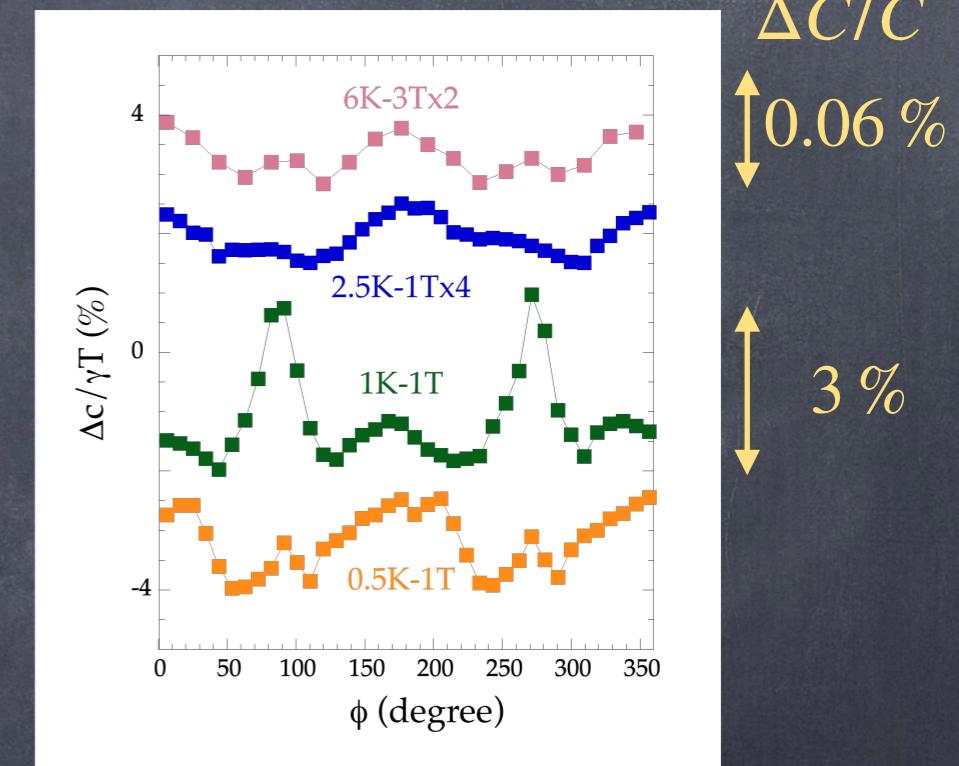
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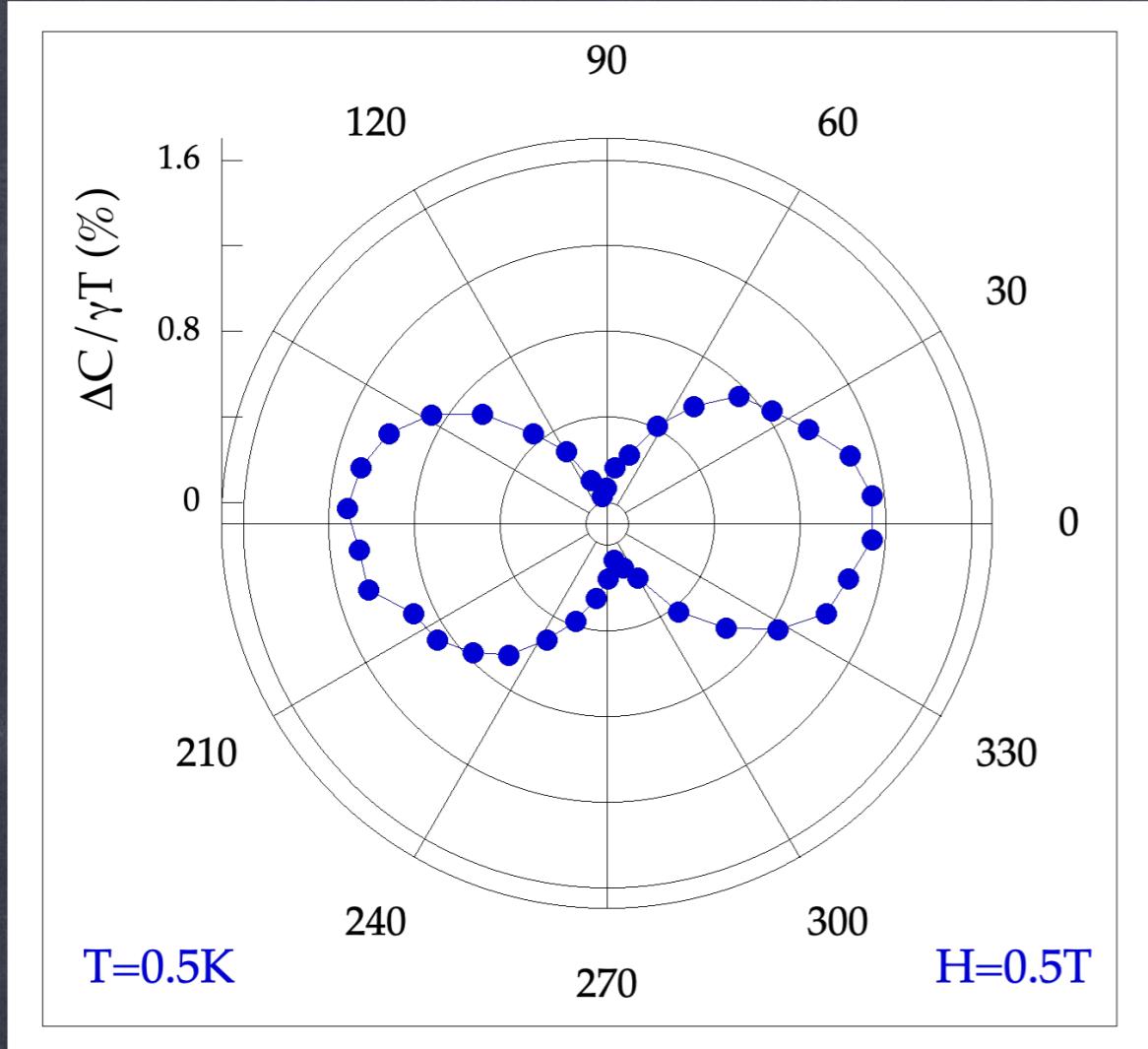
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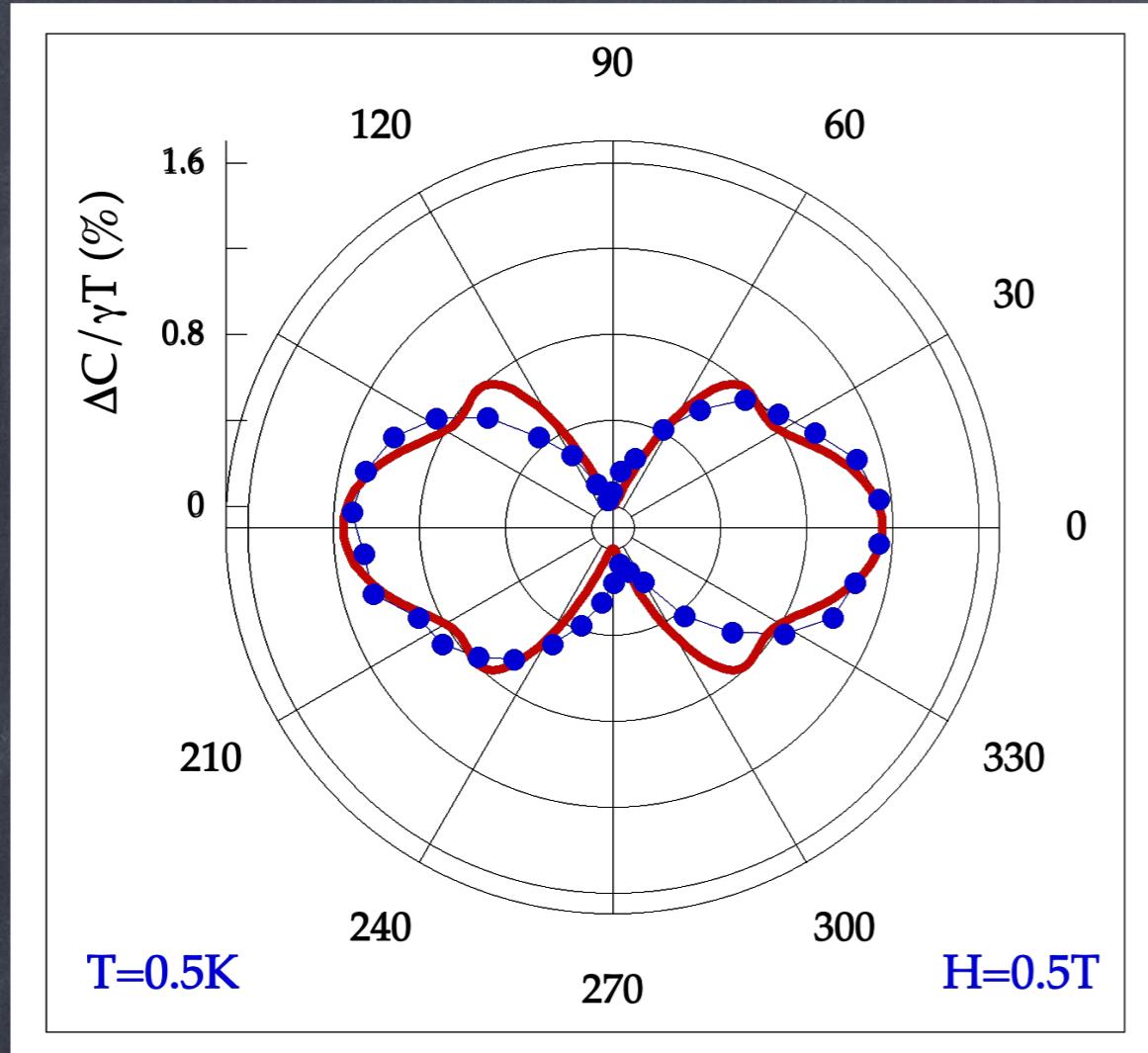
Observed in FeSe  
up to 6K and/or 6T  
AC measurements



**twofold ( $C_2$ ) symmetry**

at low T/low H

= nematic character of FeSe  
from thermodynamic data



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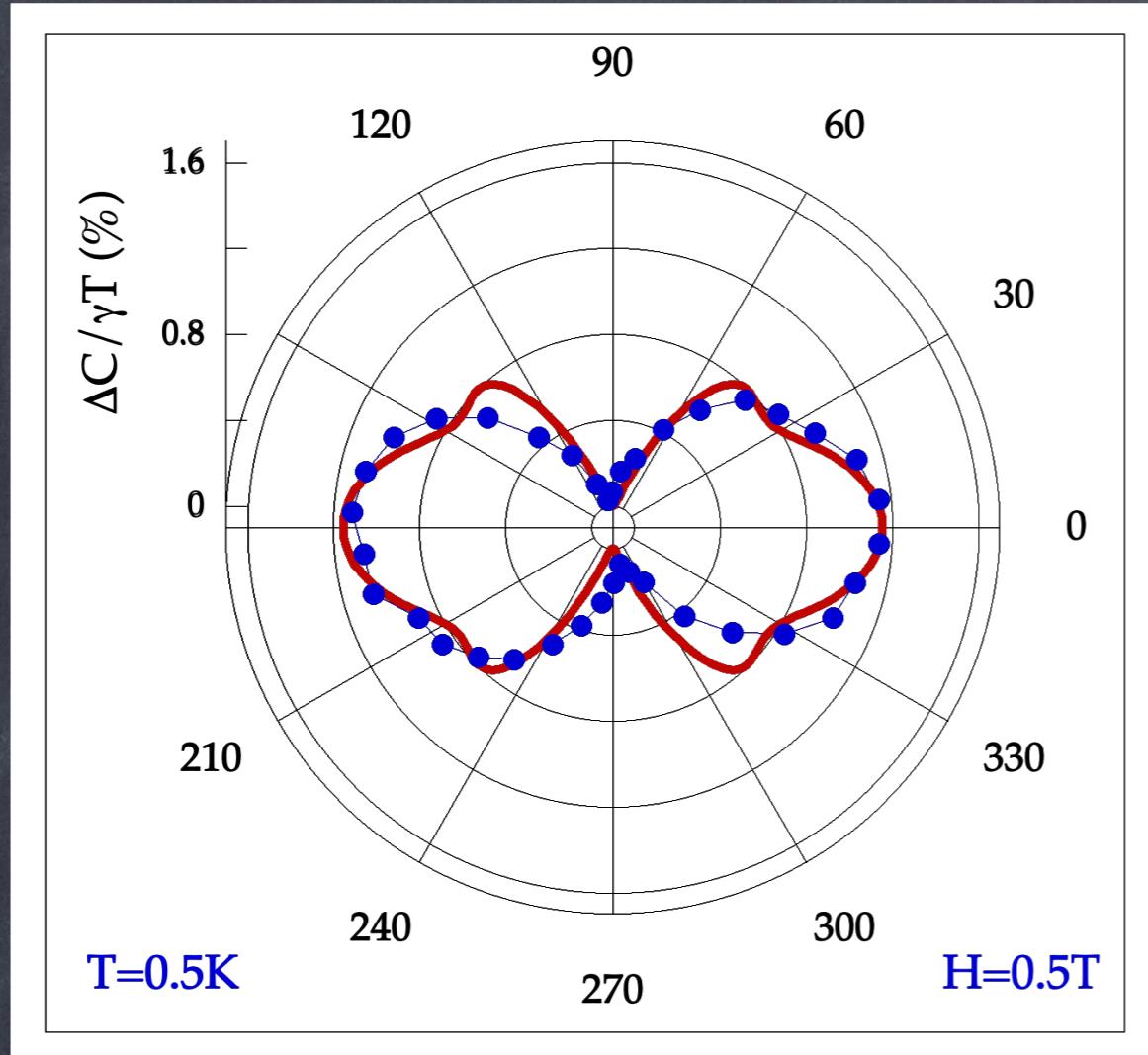
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**(H.Cercellier)**

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in very reasonable agreement with other measurements

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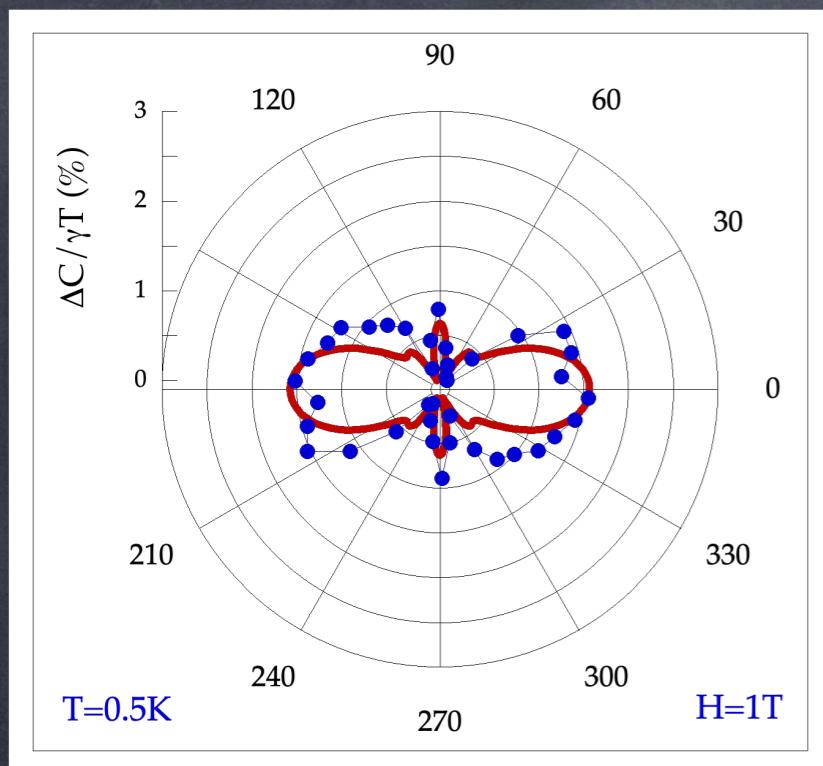
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but *exotic* temperature and field dependence of  
the gap structure !...

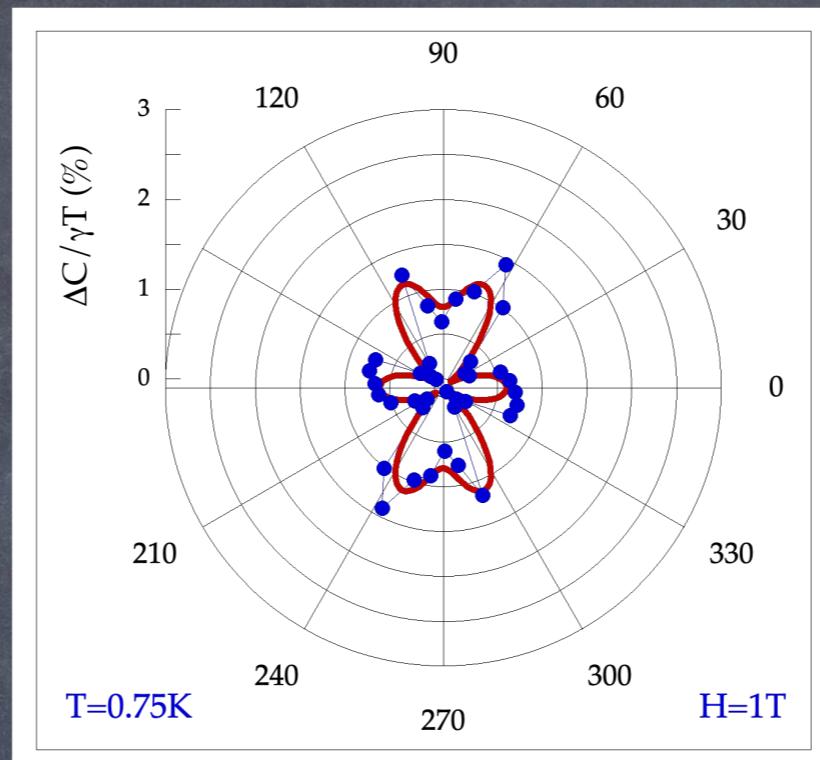
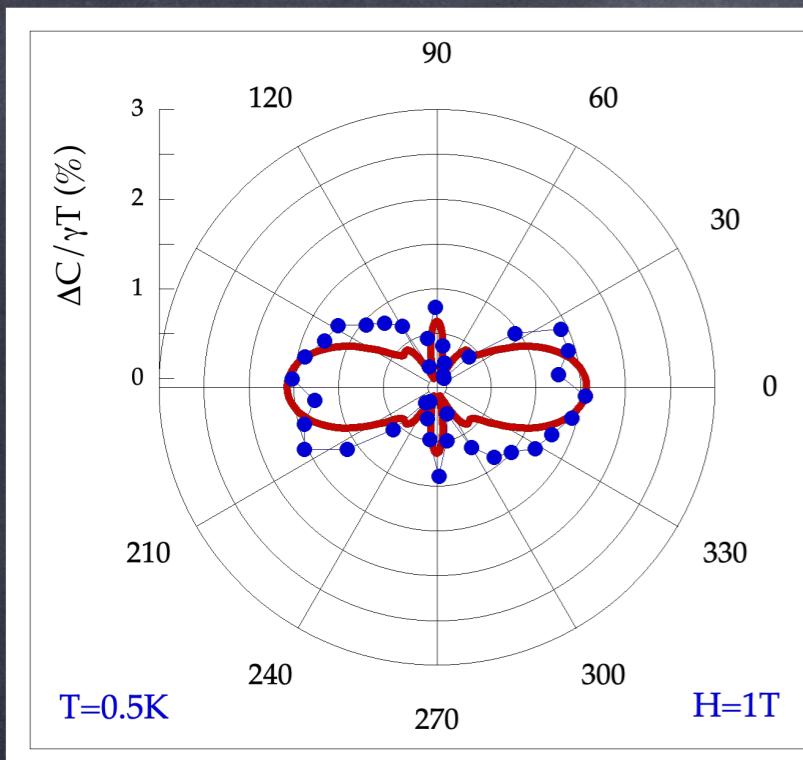
increasing temperature



$$\Delta_{\text{hole}}^{\max} \sim 2 \text{ meV}$$

$$\Delta_{\text{elec}}^{\max} \sim 1 \text{ meV}$$

increasing temperature

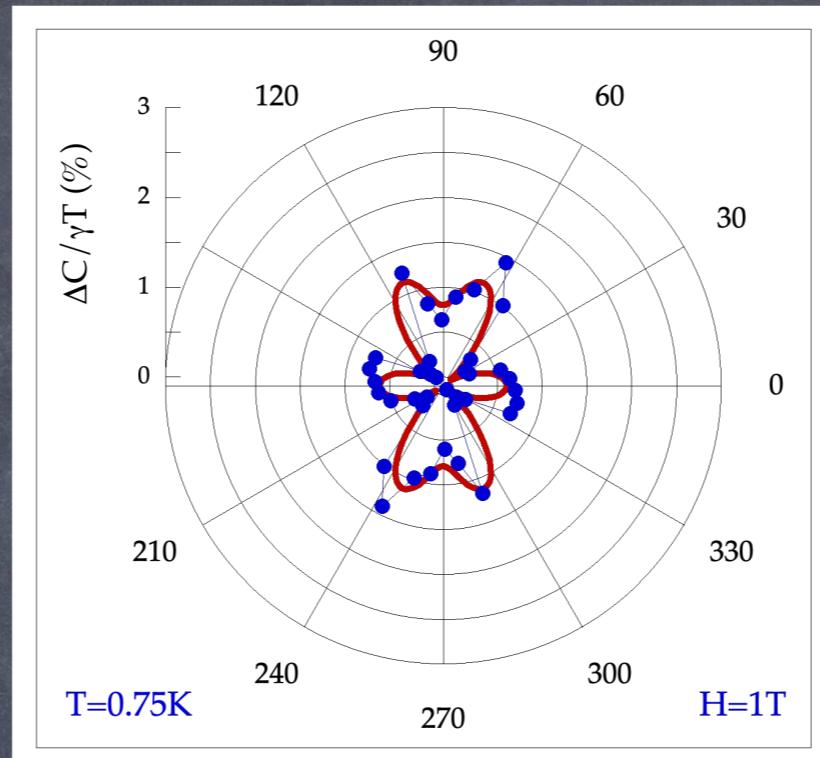
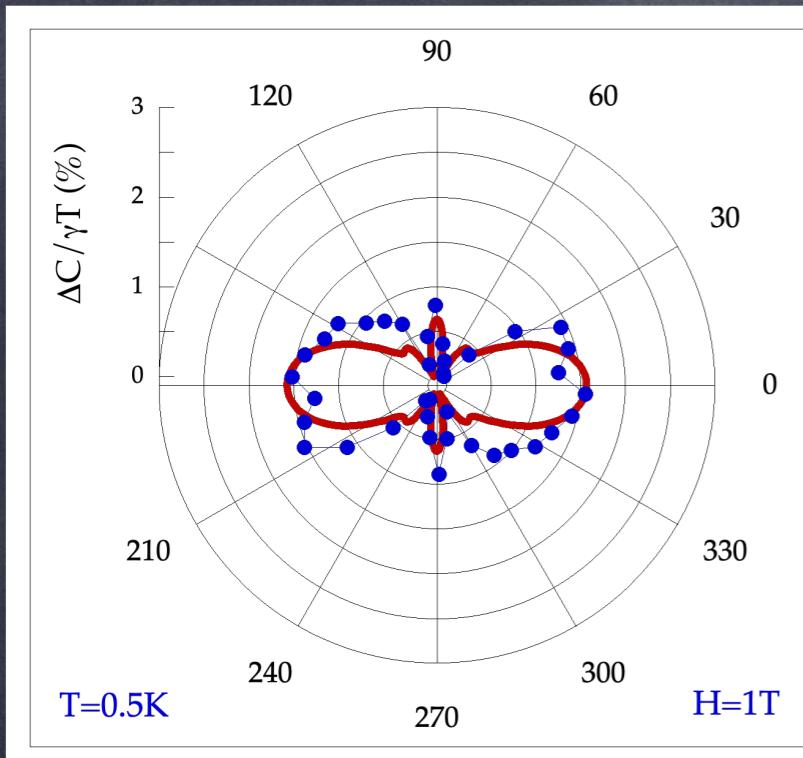


intriguing «butterfly»  
structure

$$\Delta_{\text{hole}}^{\max} \sim 2 \text{ meV}$$

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intriguing «butterfly»

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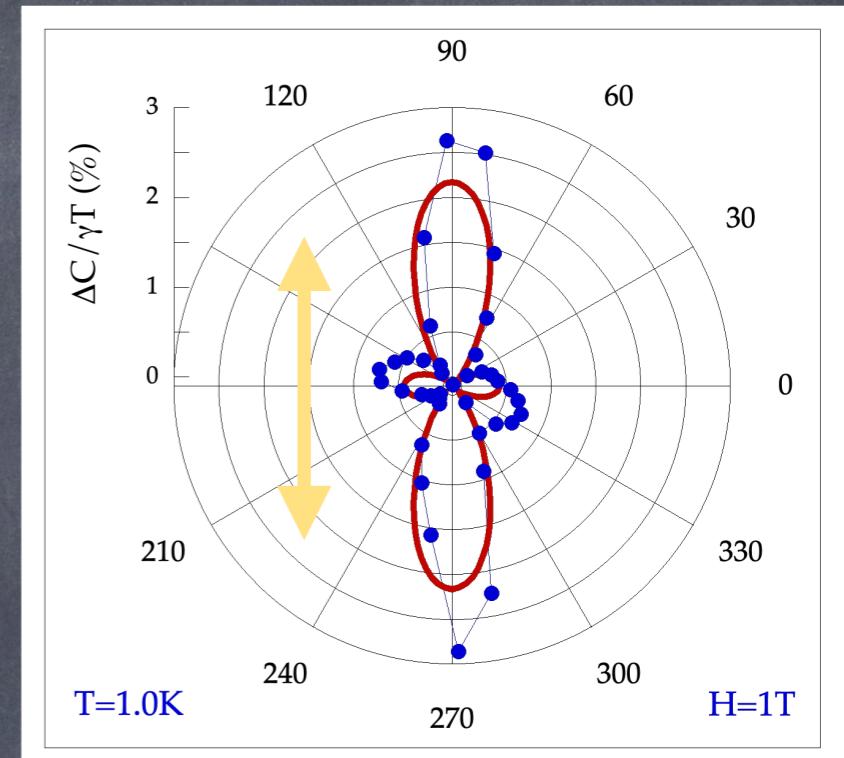
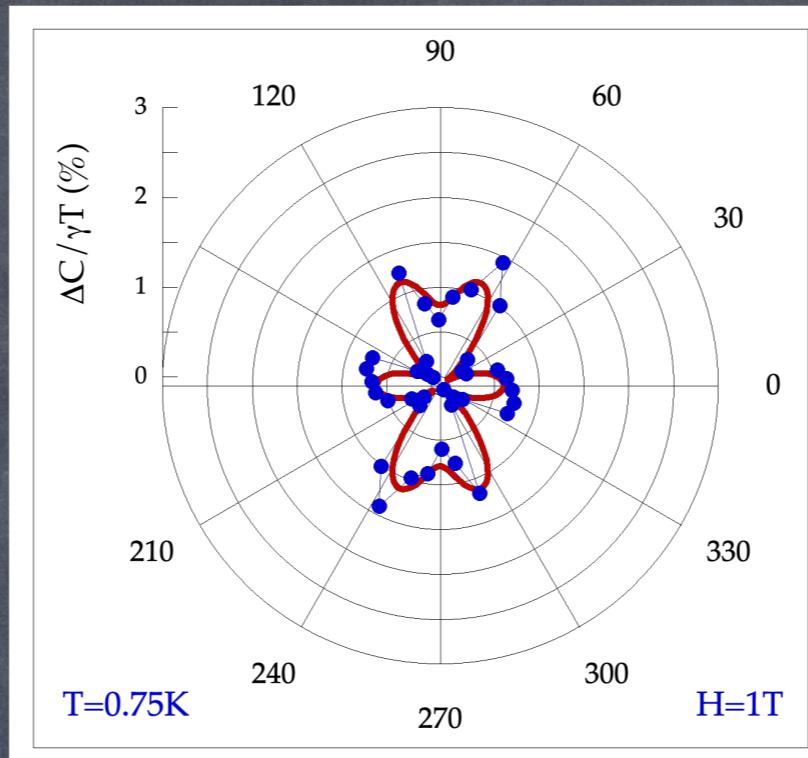
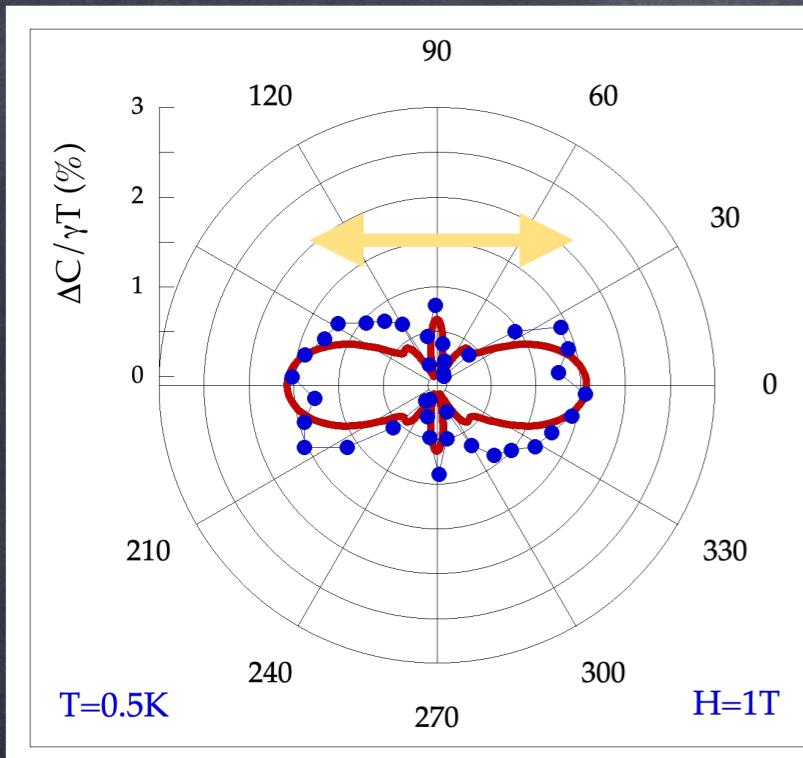
characteristic of  
accidental nodes

$$\Delta_{\text{hole}}^{\max} \sim 2\text{meV}$$

$$\Delta_{\text{elec}}^{\max} \sim 1\text{meV}$$

$$\Delta_{\text{hole}}^{\min} \sim \Delta_{\text{elec}}^{\min} \sim -0.2\text{meV}$$

increasing temperature



intriguing «butterfly»  
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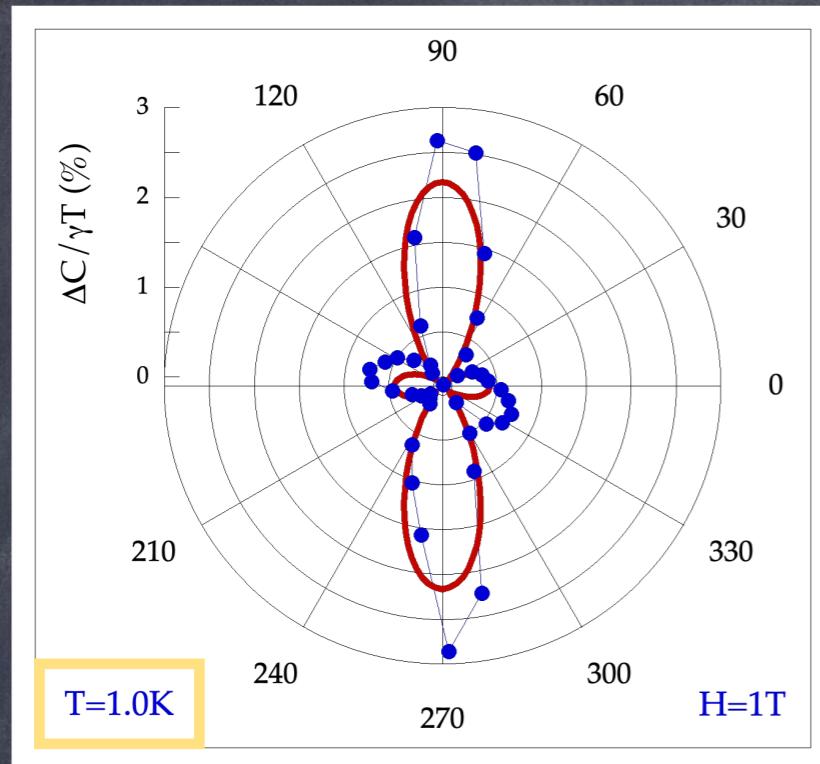
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$\pi/2$ –shift of the  
symmetry axis  
(for  $T \sim T_c/10$ )  
also well reproduced

increasing temperature



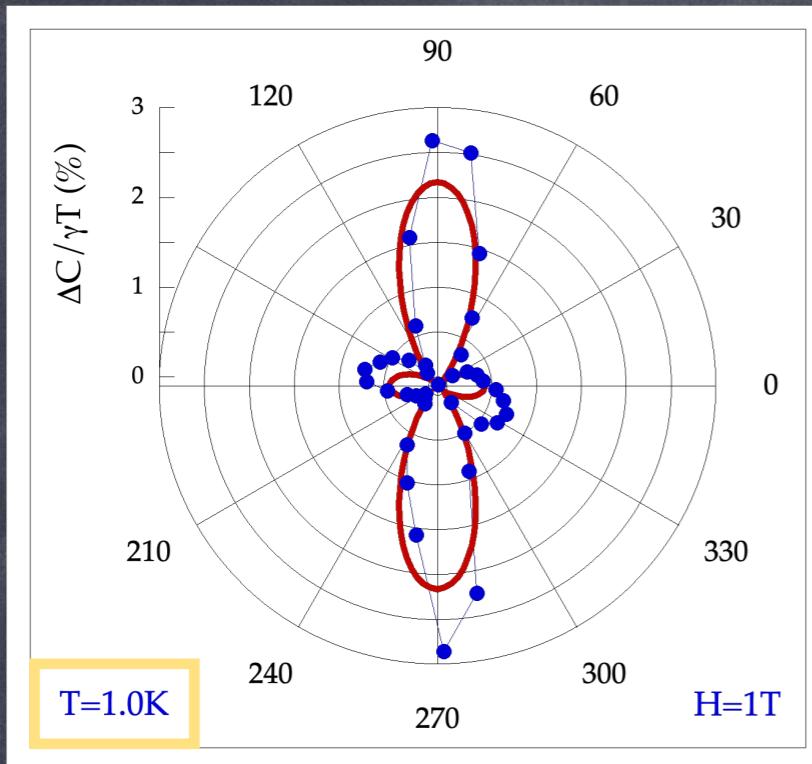
$$\Delta_{\text{hole}}^{\max} \sim 2\text{meV}$$

$$\Delta_{\text{hole}}^{\min} \sim -0.2\text{meV}$$

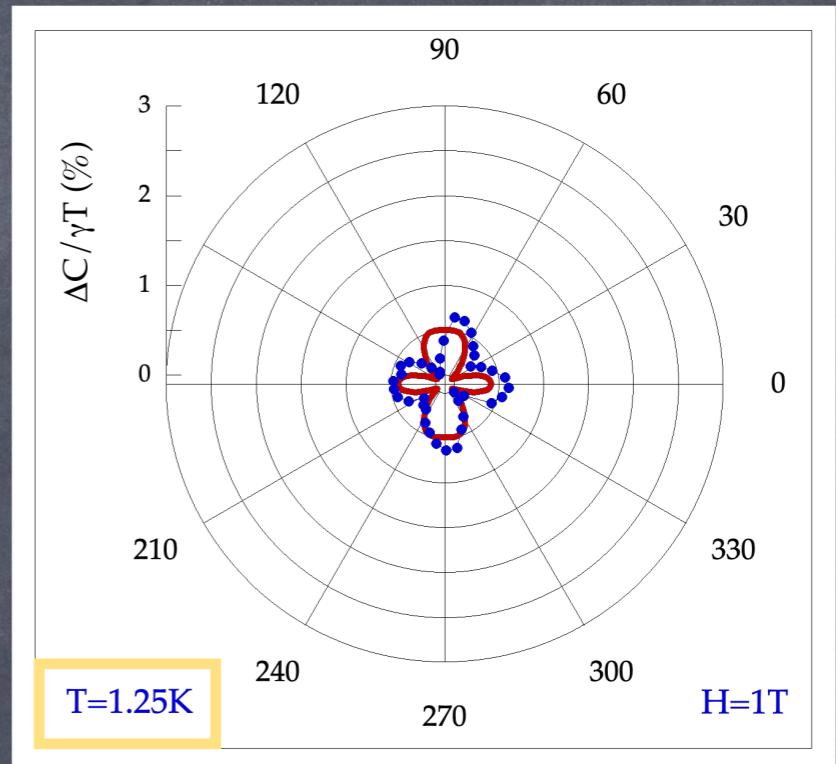
$$\Delta_{\text{elec}}^{\max} \sim 1\text{meV}$$

$$\Delta_{\text{elec}}^{\min} \sim -0.2\text{meV}$$

increasing temperature



but  
**drastic drop  
of the  
amplitude  
above 1K ?**



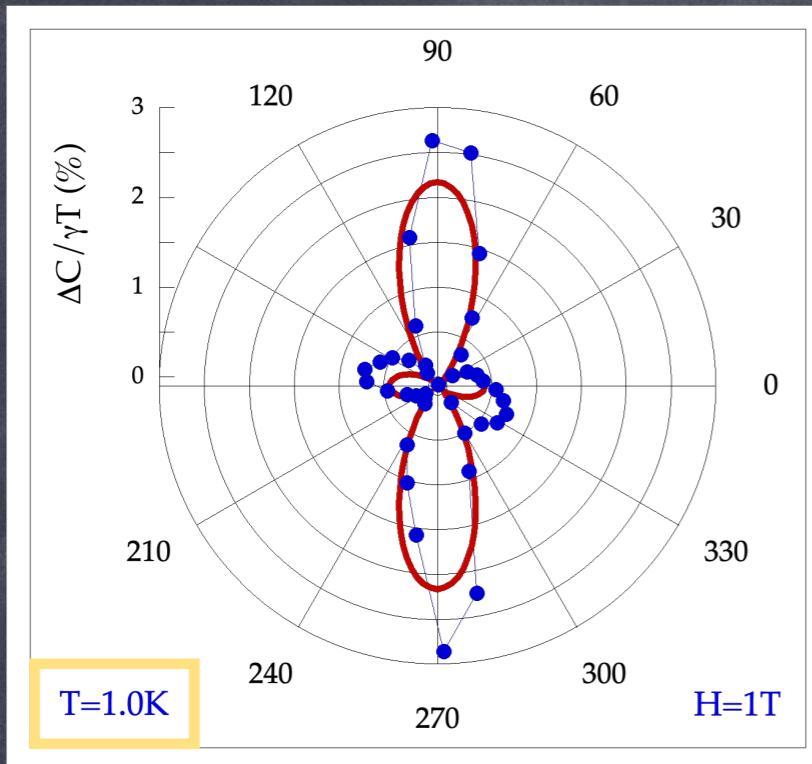
$$\Delta_{\text{hole}}^{\max} \sim 2 \text{ meV}$$

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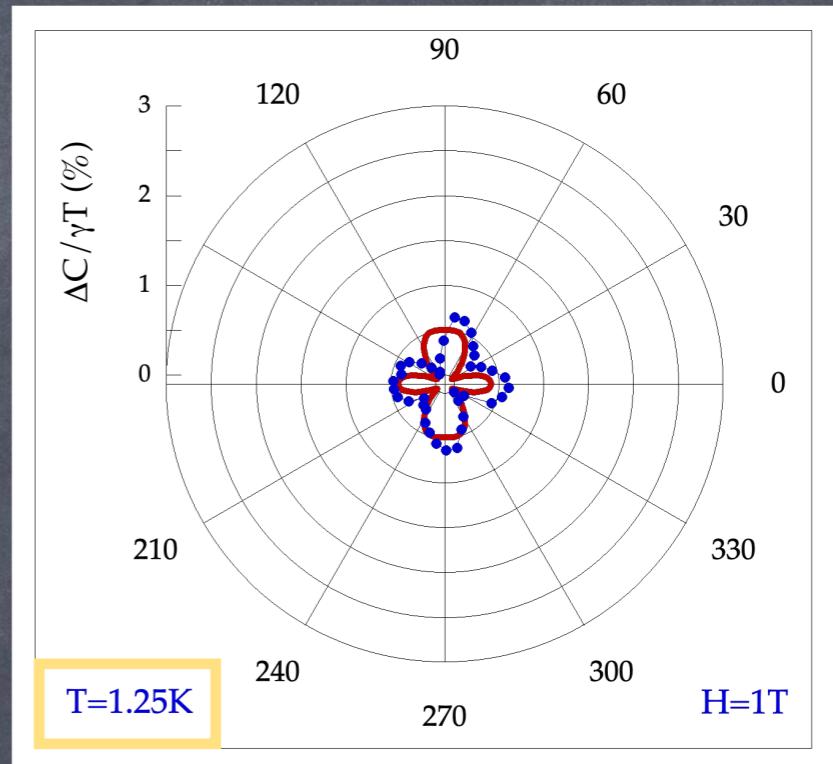
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increasing temperature

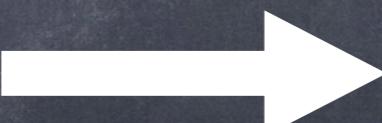


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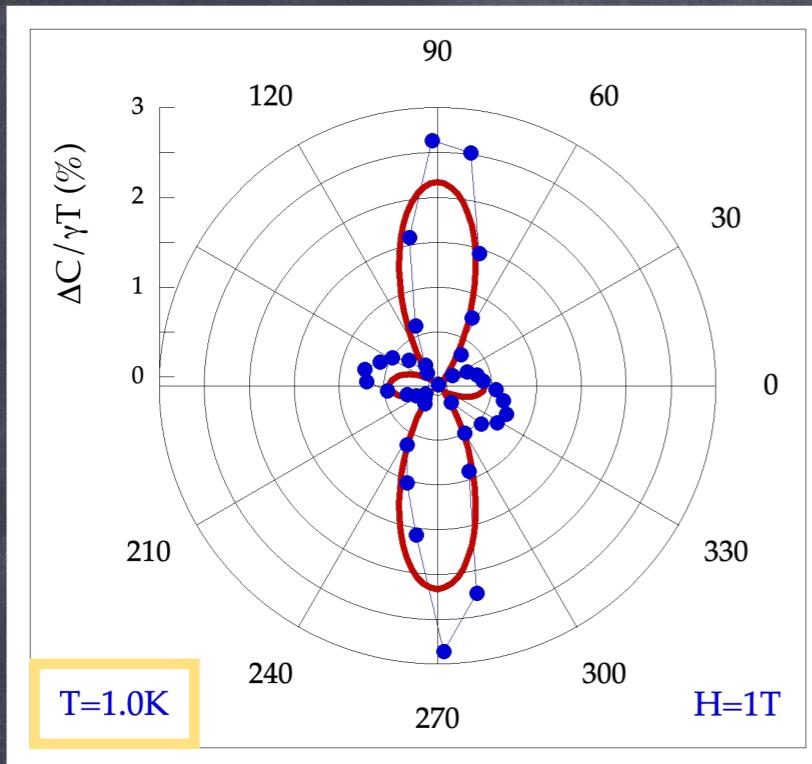
Sudden change in the gap structure

$$\left. \begin{array}{l} \Delta_{\text{hole}}^{\text{max}} \sim 2\text{meV} \\ \Delta_{\text{hole}}^{\text{min}} \sim -0.2\text{meV} \\ \Delta_{\text{elec}}^{\text{max}} \sim 1\text{meV} \\ \Delta_{\text{elec}}^{\text{min}} \sim -0.2\text{meV} \end{array} \right\}$$

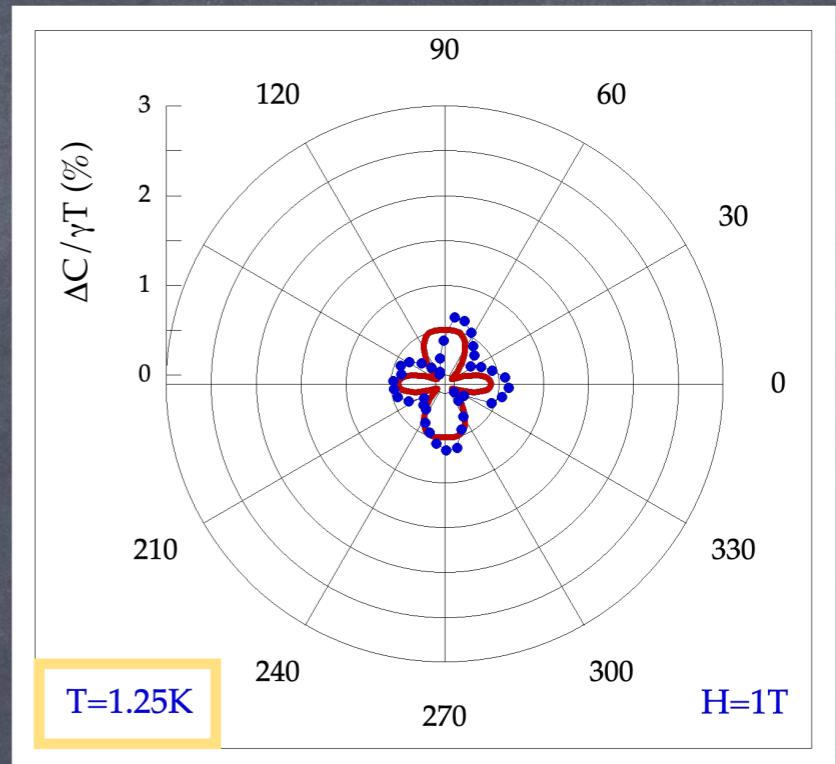


$$\left. \begin{array}{l} \Delta_{\text{hole}}^{\text{max}} \sim 2\text{meV} \\ \Delta_{\text{hole}}^{\text{min}} \sim 0.5\text{meV} \\ \Delta_{\text{elec}}^{\text{max}} \sim 0.5\text{meV} \\ \Delta_{\text{elec}}^{\text{min}} \sim -0.2\text{meV} \end{array} \right\}$$

increasing temperature

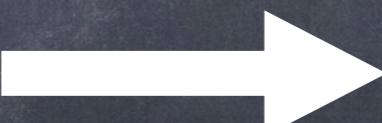


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Sudden change in the gap structure

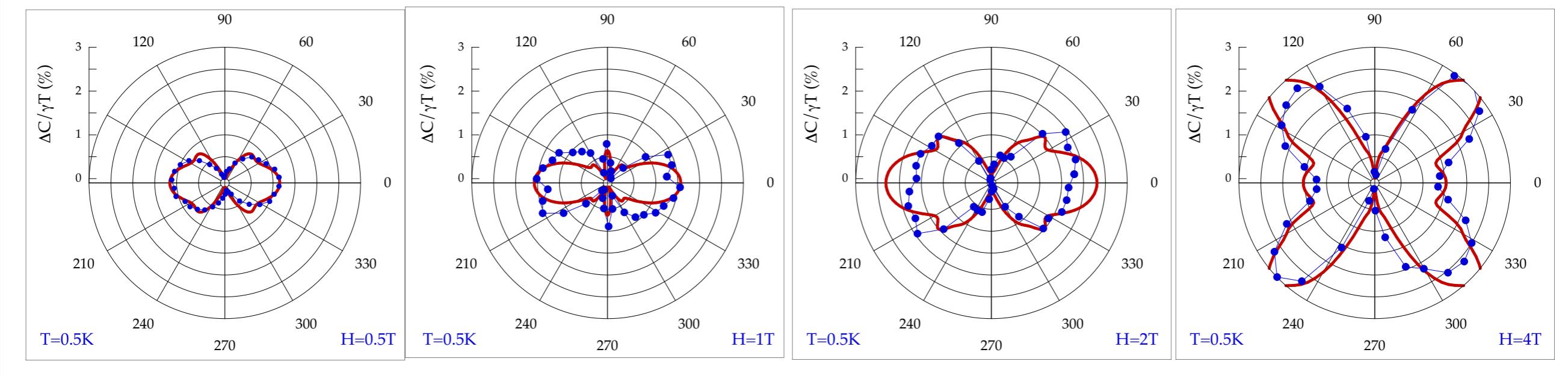
$$\left. \begin{array}{l} \Delta_{\text{hole}}^{\max} \sim 2 \text{ meV} \\ \Delta_{\text{hole}}^{\min} \sim -0.2 \text{ meV} \\ \Delta_{\text{elec}}^{\max} \sim 1 \text{ meV} \\ \Delta_{\text{elec}}^{\min} \sim -0.2 \text{ meV} \end{array} \right\}$$



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... leading to the observed specific anomaly around 1K

increasing field

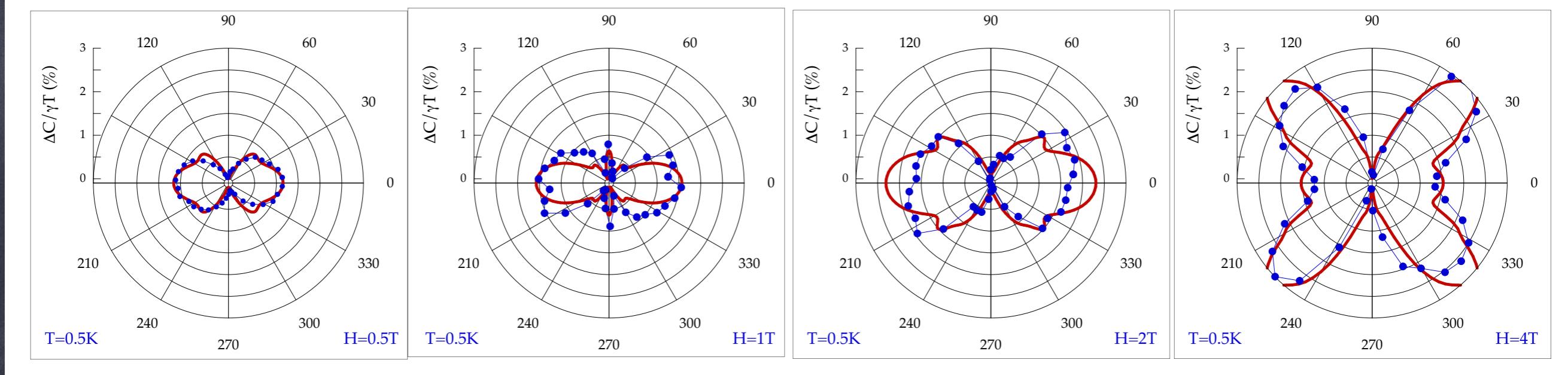


and lobes develop  
around  $45^\circ$   
above  $\sim 4\text{T}$

field dependent gap amplitude

$$\Delta_{\text{hole}}^{\max} \rightarrow \Delta_{\text{elec}}^{\max} \rightarrow 1.5\text{meV}$$

increasing field



and lobes develop  
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above  $\sim 4\text{T}$

field dependent gap amplitude

$$\Delta_{\text{hole}}^{\max} \rightarrow \Delta_{\text{elec}}^{\max} \rightarrow 1.5\text{meV}$$

This T and H dependence of the gap structure still has to be understood  
(not observed in all samples...)

H.Cercellier *et al.* submitted to PRL (2024)

# Outline

---

- **The FeSe nematic superconductor**  
H-T phase diagram and T & H dependence of the gap structure
- **Thermodynamic properties of the normal state in cuprates**  
Quantum criticality at the onset of the pseudo-gap and charge order

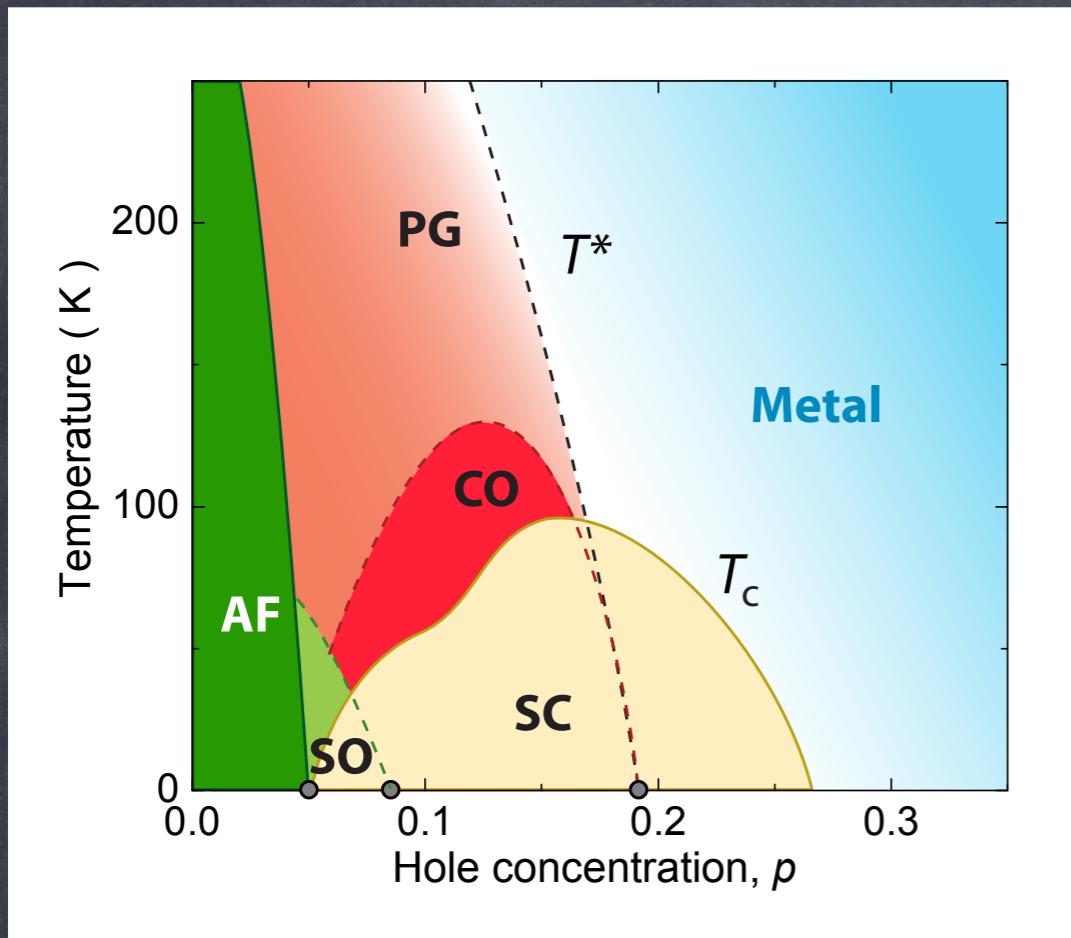
part of the PhD work of **B.Michon & C.Girod**

# Outline

---

- **Thermodynamic properties of the normal state in cuprates**  
Quantum criticality at the onset of the pseudo-gap and charge order

part of the PhD work of **B.Michon & C.Girod**



YBaCuO, Courtesy N.Doiron-Leyraud, Univ. of Sherbrooke

## Cuprates

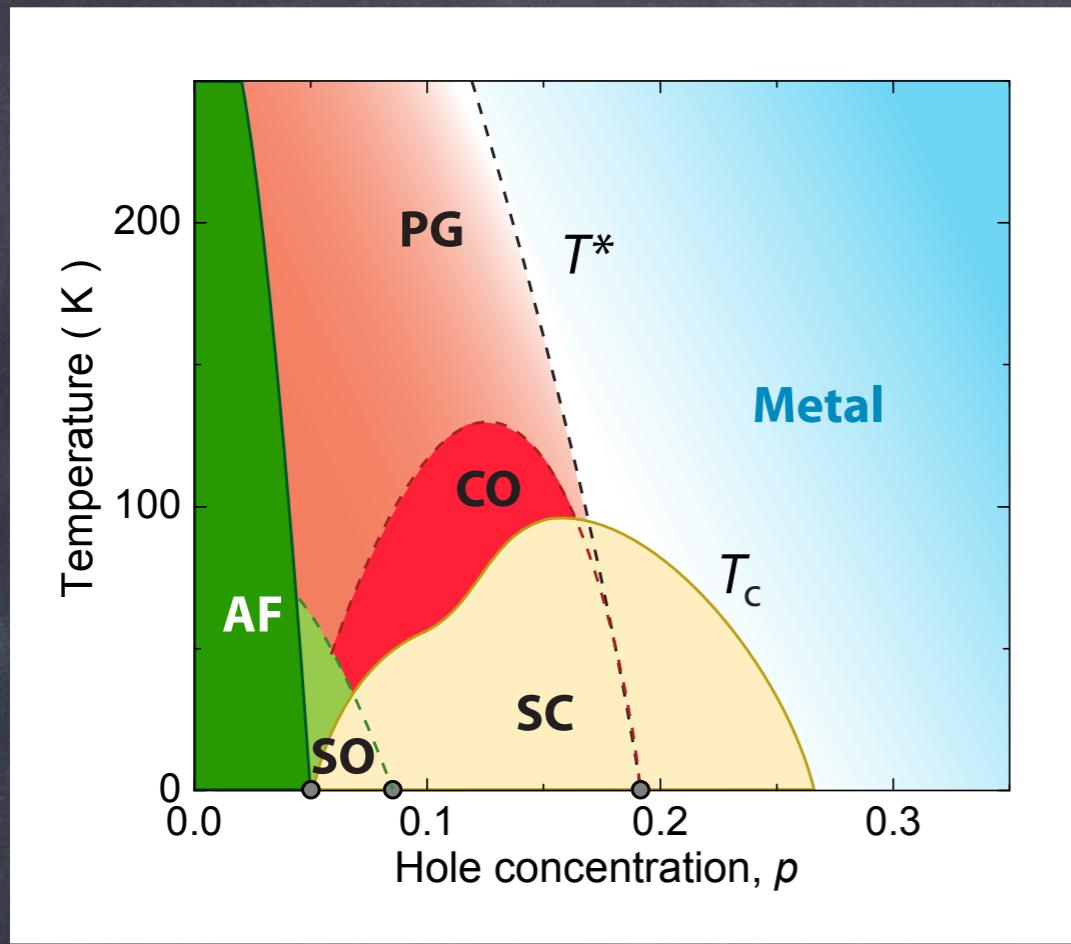
very complexe phase diagram

CO=charge order

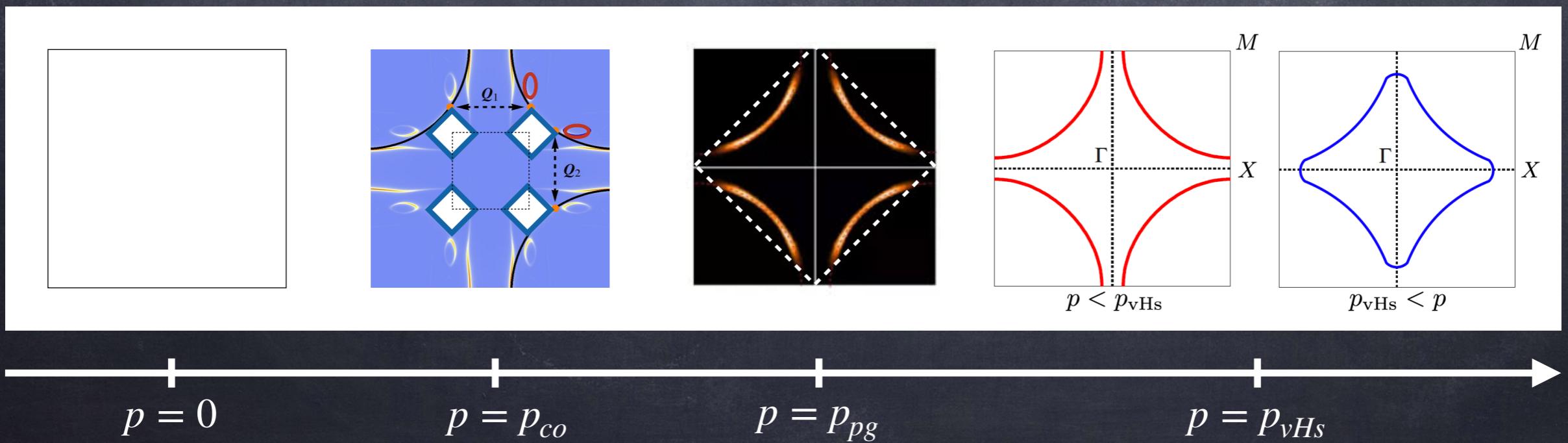
SO=spin order

PG= *mysterious* pseudo-gap phase

SC=superconductor



YBaCuO, Courtesy N.Doiron-Leyraud, Univ. of Sherbrooke



## Cuprates

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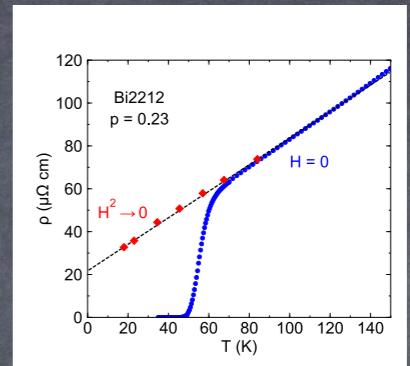
associated with major changes in the topology of the Fermi surface

# Let's start with the pseudo-gap phase...

## Linear temperature dependence

of the resistivity : so-called *Planckian* diffusion

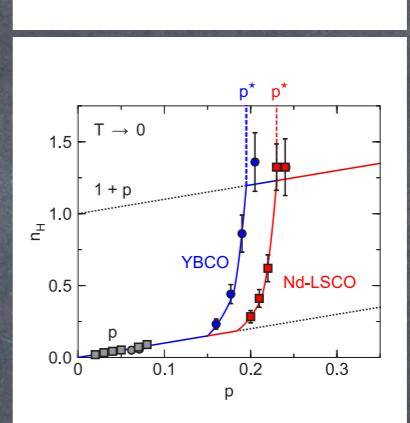
C. Collignon et al., PRB 2017, A. Legros et al., Nature 2019



## Drop in the carrier density from $n = I + p$ to $n = p$

consistent with (AF) reconstruction of the FS

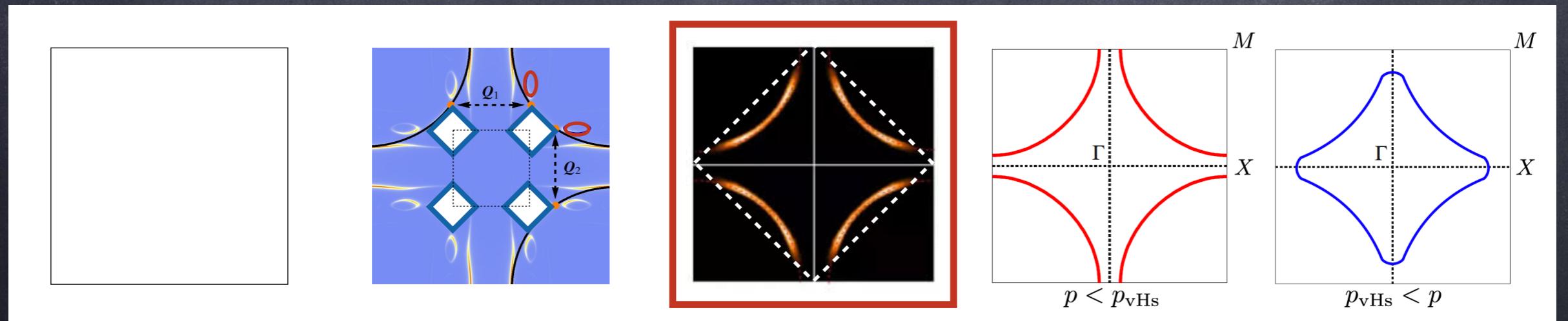
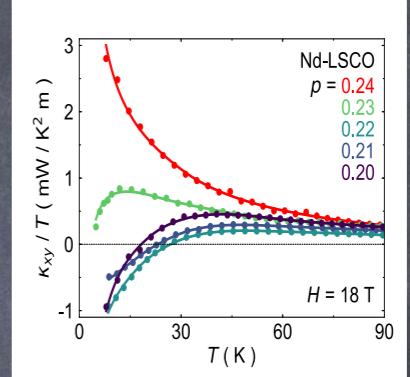
C. Collignon et al., PRB 2017, S. Badoux et al., Nature 2016



## Giant negative thermal Hall effect

from  $p_{pg}$  down the Mott insulator ( $p=0$ )

G. Grissonanche et al., Nature 2019 & 2020, M-E. Boulanger et al., Nat. Com 2020



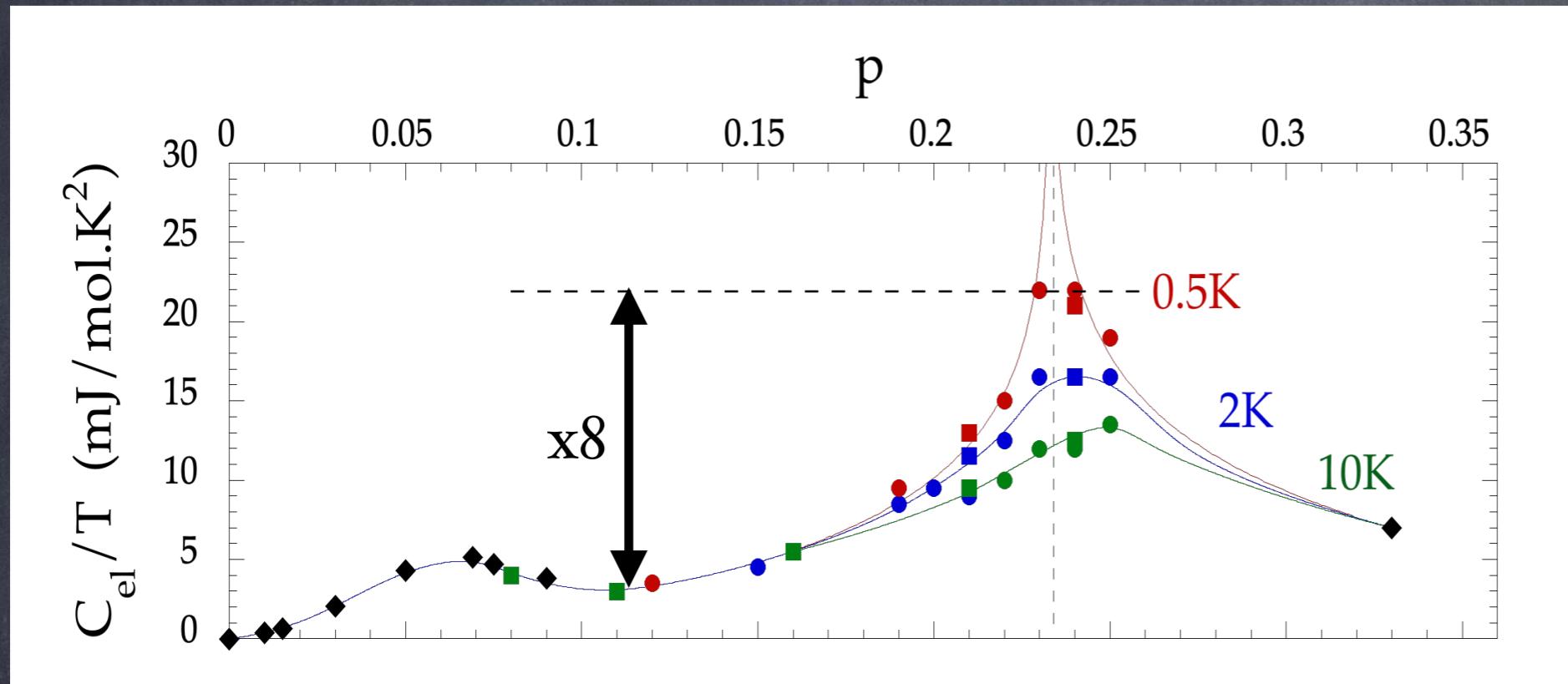
$p = 0$

$p = p_{co}$

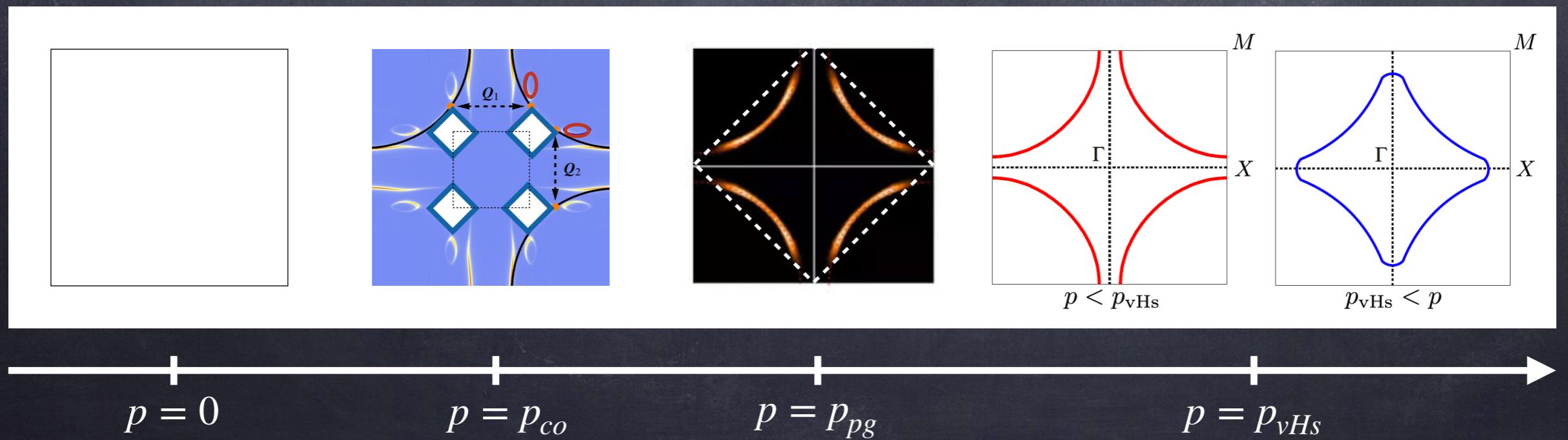
$p = p_{pg}$

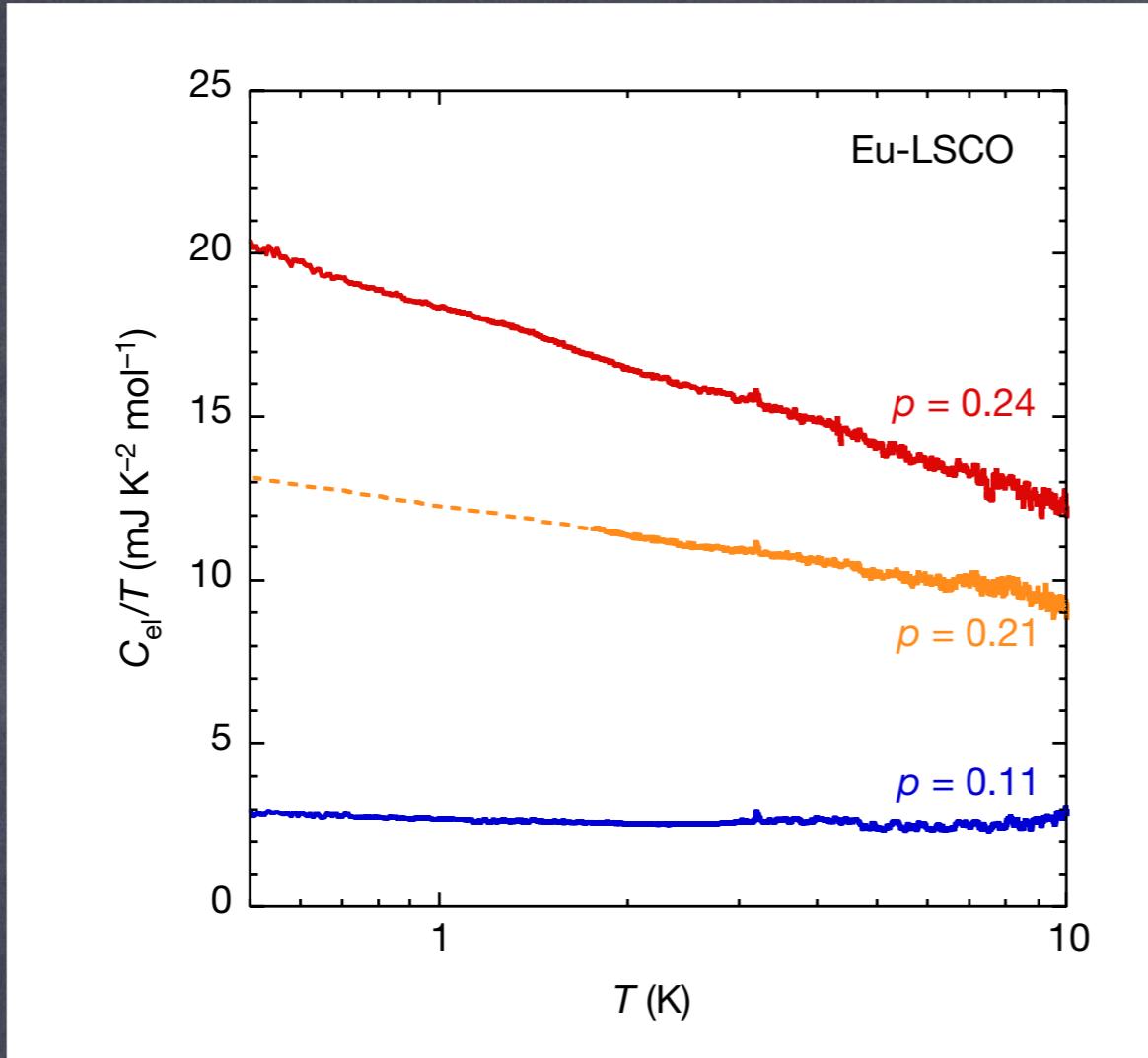
$p = p_{vHs}$

We have shown that the onset of the PG is also associated with **pronounced peak** of the Normal state specific heat for  $T \rightarrow 0$   
(as mentioned yesterday by Chandra Warma)



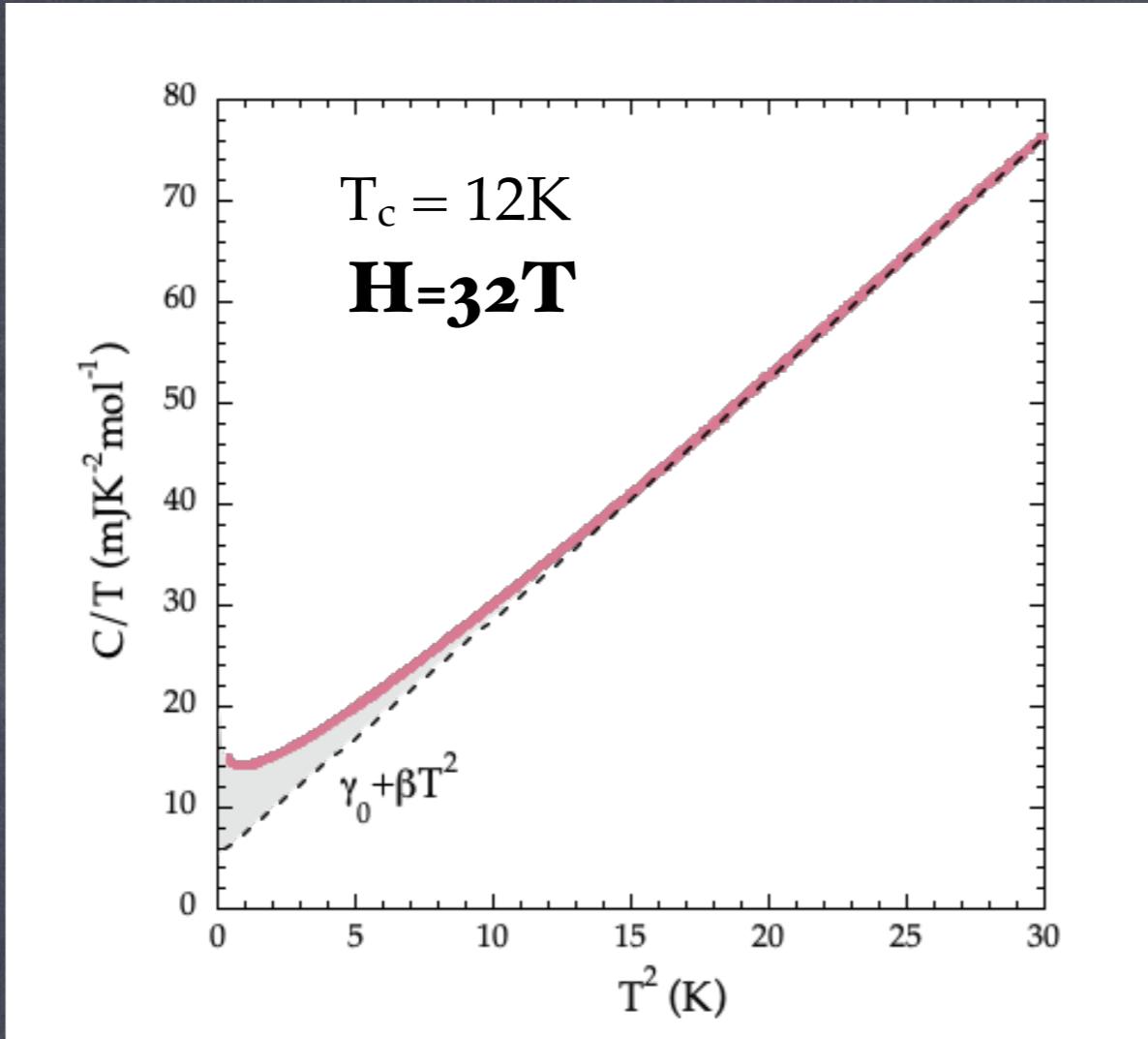
B.Michon *et al.*  
Nature 2019



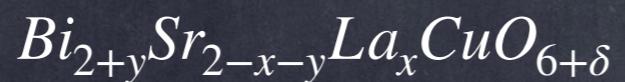


associated with a  $\text{Log}T$  dependence of  $C_{\text{el}}/T$  for  $p \rightarrow p_{\text{pg}} \sim 0.24$   
(here  $C_{\text{el}}/T = C/T - \beta T^2$ )

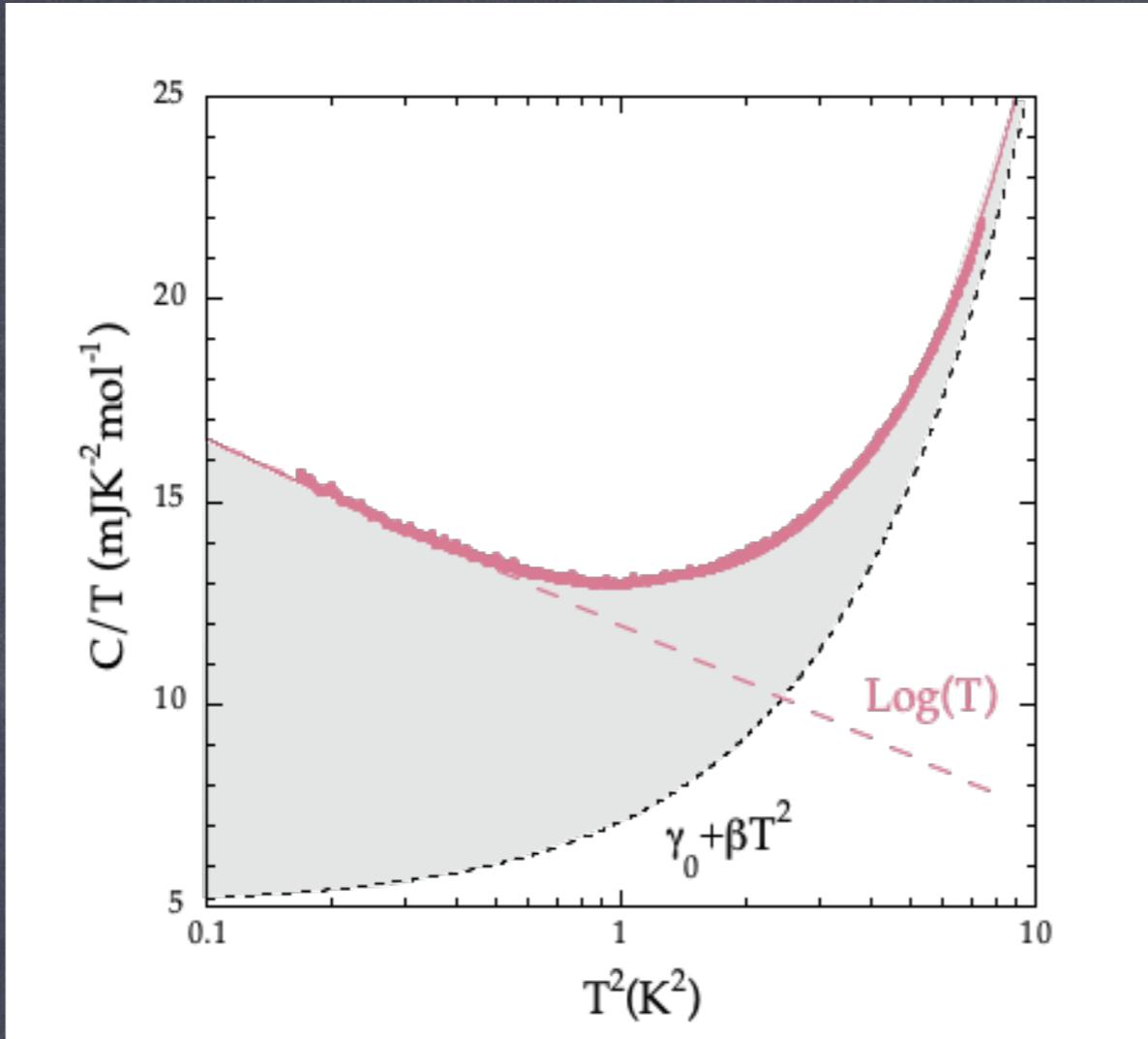
Michon *et al.* Nature 2019



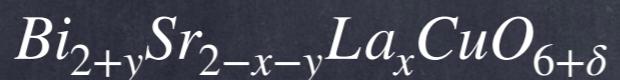
**clear deviation from the  
standard temperature  
dependence also observed in**



C.Girod *et al.* PRB 2021



**clear deviation from the  
standard temperature  
dependence also observed in**



C.Girod *et al.* PRB 2021

(again) very good fit  
to the data with

$$C/T = \beta T^2 + B \log(T/T_0)$$

LnT contribution to  
the specific heat pour  $p \sim p_c$

strong C/T peak  
for  $p \rightarrow p_c$  at low T

= *classic* thermodynamic signature of a  $z = d$  **Quantum Critical Point**

BUT...what is the diverging correlation length ?

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the specific heat pour  $p \sim p_c$

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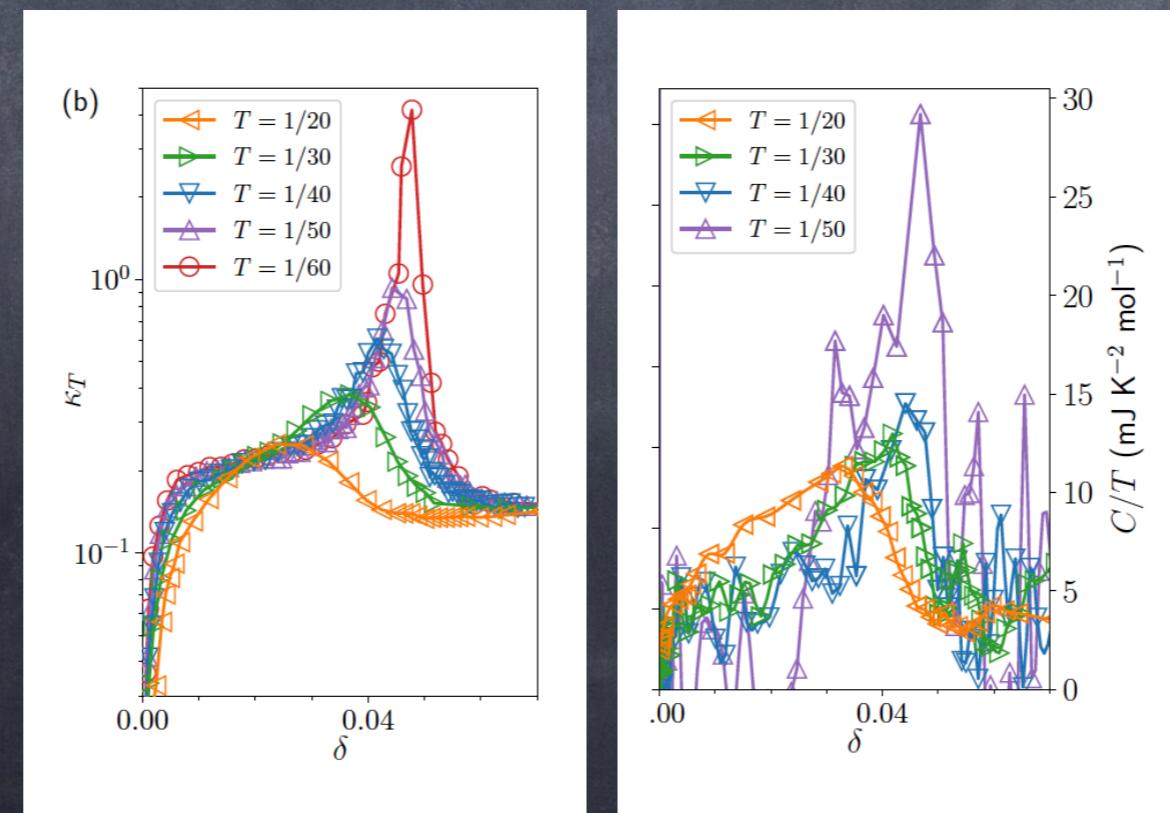
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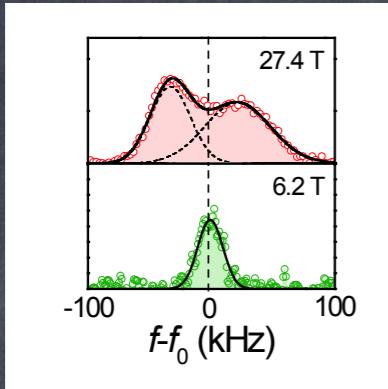
cluster-DMFT calculations in the t-U model (correlated systems)

G.Sordi *et al.* Sc. Reports 2012, 2010

T dependent peak in  
the electronic  
compressibility  
 $K_T = 1/n^2(dn/d\mu)_T$   
(diverging at the  
critical point)



**AND in the  
specific heat !  
(as observed)**

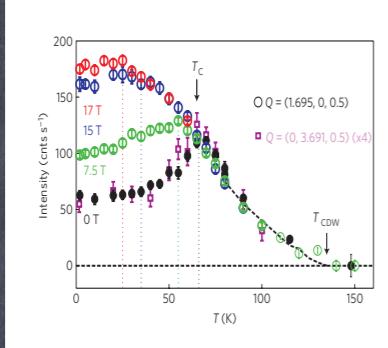


## and a few words on the Charge Order...

### Splitting of the NMR lines

modulation of the charge density

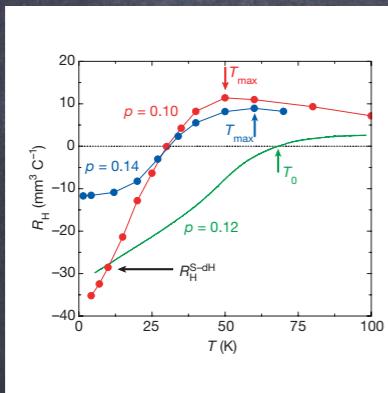
T.Wu et al. Nature 2011



### X-ray diffraction peaks

⇒ Long range CDW at high field/low T

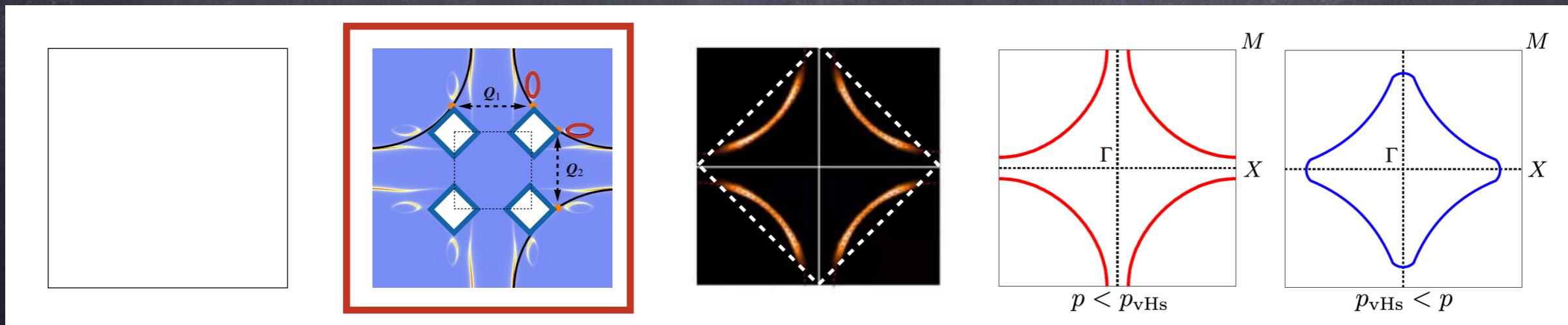
J.Chang et al. Nature Physics 2012, D.Leboeuf et al. Nature Physics 2013 (and more)



### Change of sign of Hall effect

+ low frequency quantum oscillations (FS reconstruction) & reduced  $H_{c2}$

D.Leboeuf et al. Nature 2007, Nicolas Doiron-Leyraud et al. Nature 2007,...

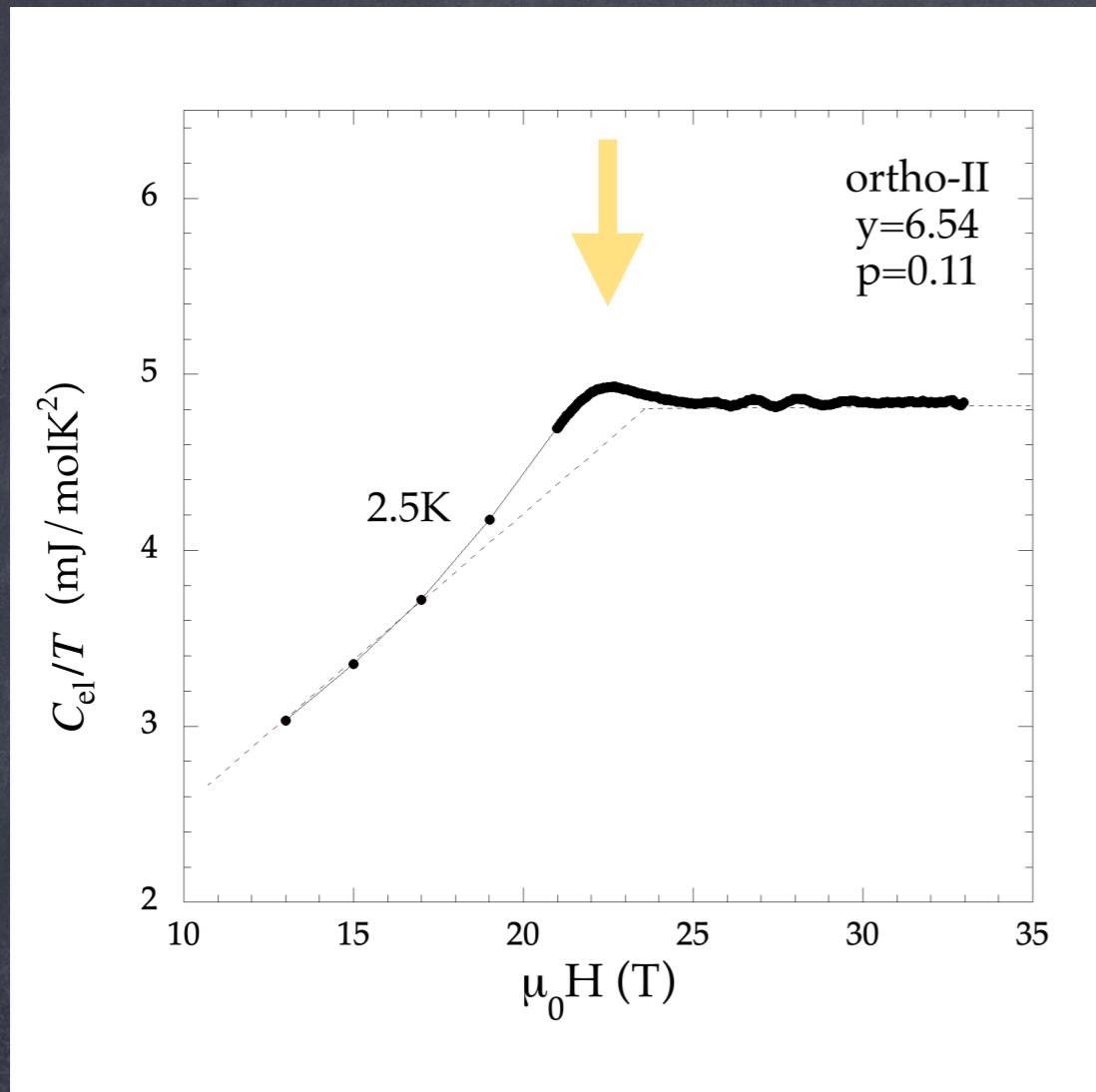


$p = 0$

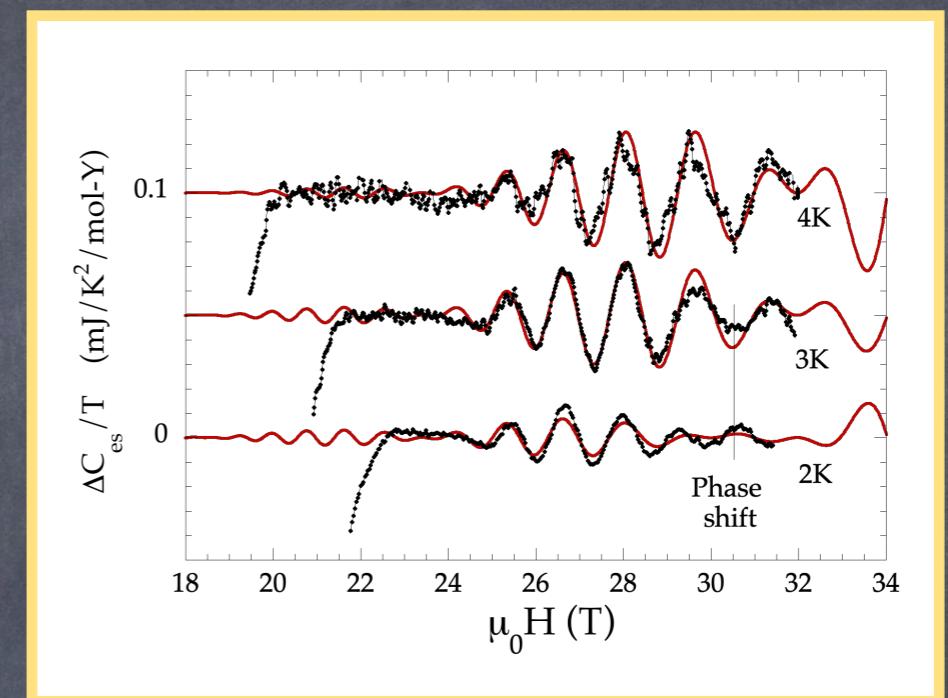
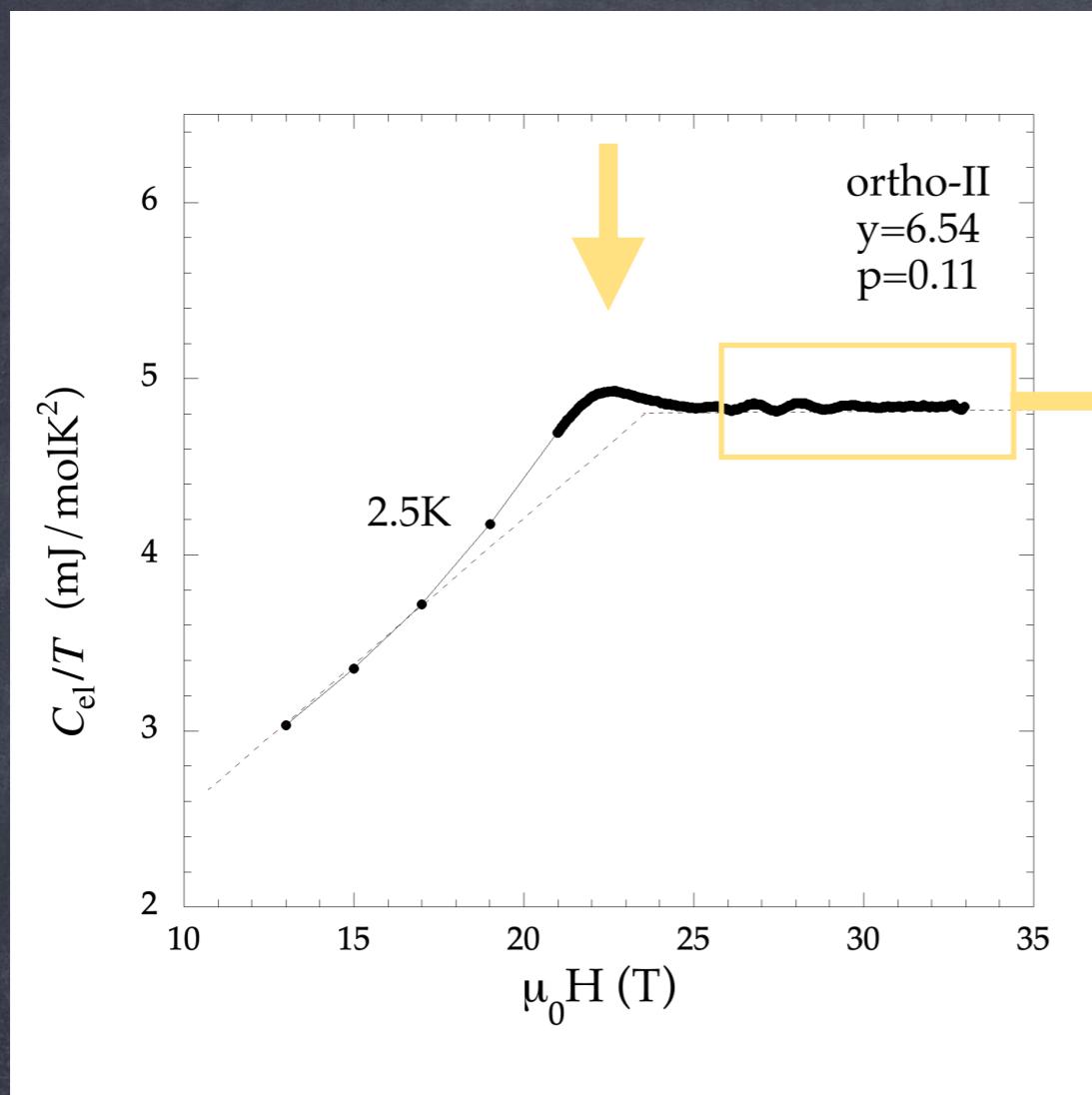
$p = p_{co}$

$p = p_{pg}$

$p = p_{vHs}$

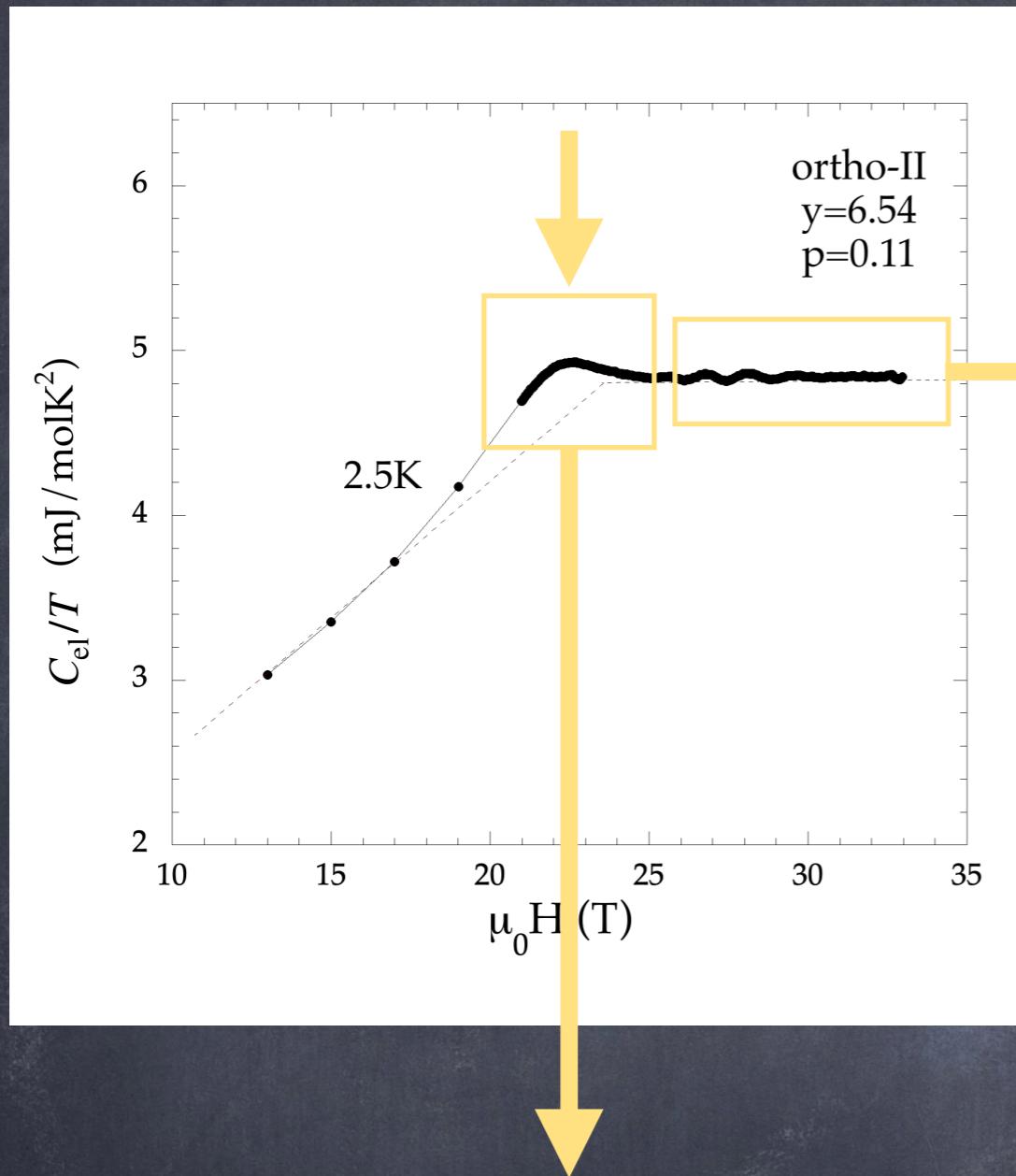


C/T saturates for  $H > H_{\text{DOS}}$   
(not  $H_{c2}$  due to thermal fluctuations)

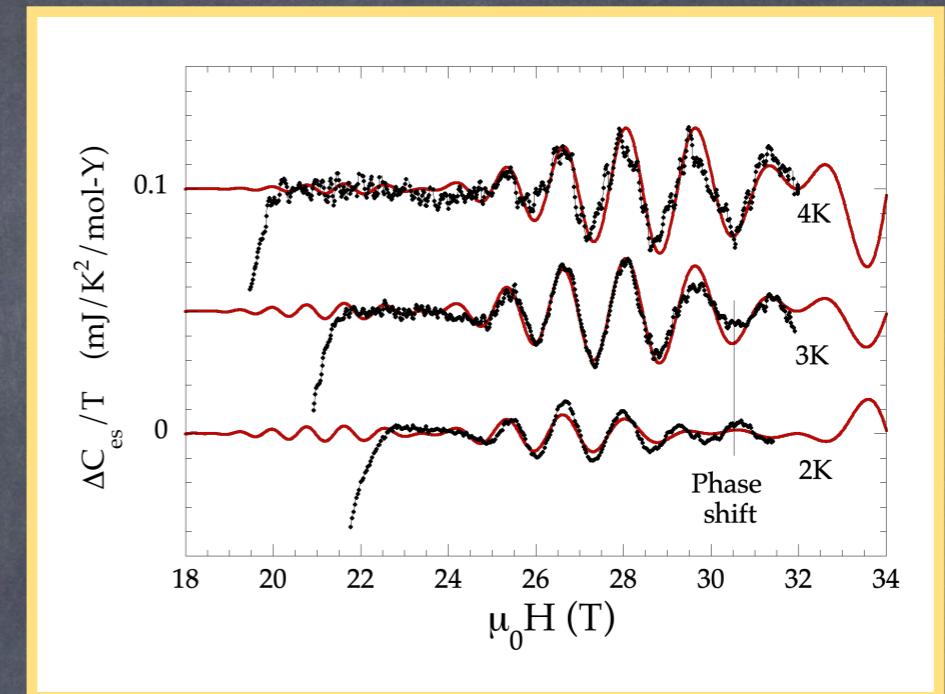


Note the presence of well resolved quantum oscillations in good agreement with **small electron pockets**

C/T saturates for  $H > H_{\text{DOS}}$   
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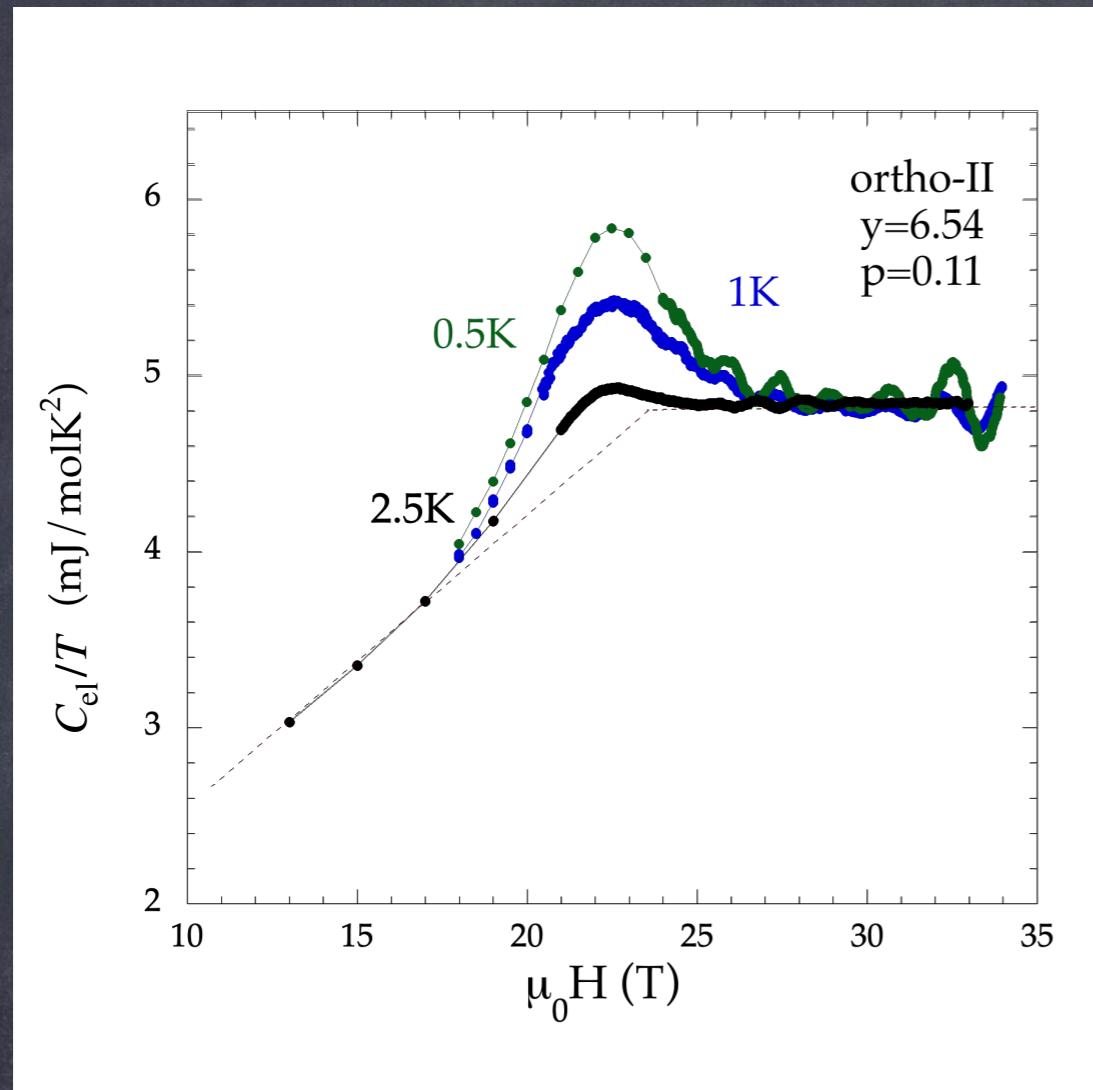


note also the small  
**Overshoot at 22T?**



Note the presence of well resolved quantum oscillations in good agreement with **small electron pockets**

**C/T saturates for  $H > H_{\text{DOS}}$**   
(not  $H_{c2}$  due to thermal fluctuations)



which **increases**

for decreasing temperature !

(unpublished)

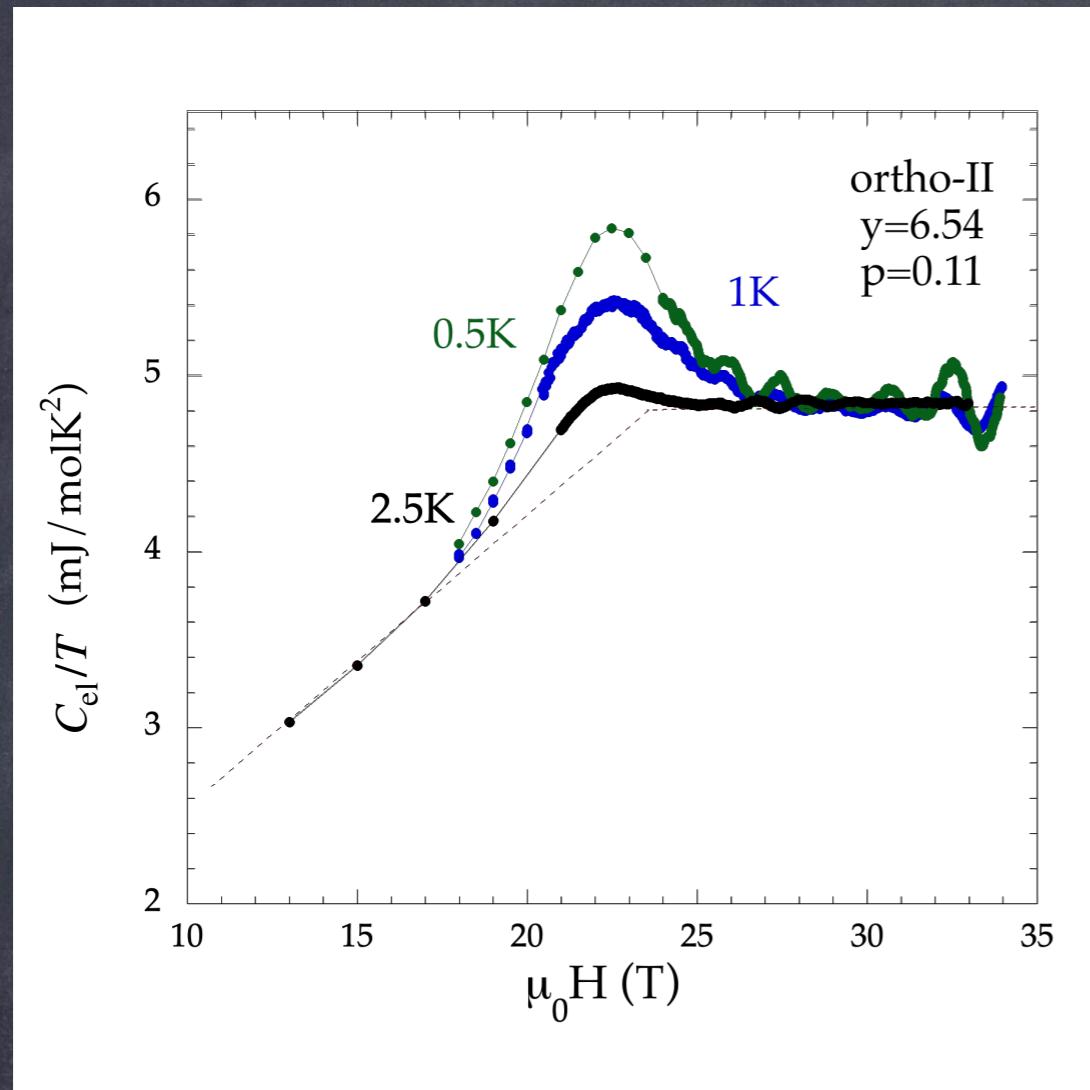
Can **not** be the standard overshoot

observed at the SC transition

Its origin still has to be clarified...

(another field induced)

quantum critical point ???



which **increases**

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(unpublished)

Can **not** be the standard overshoot

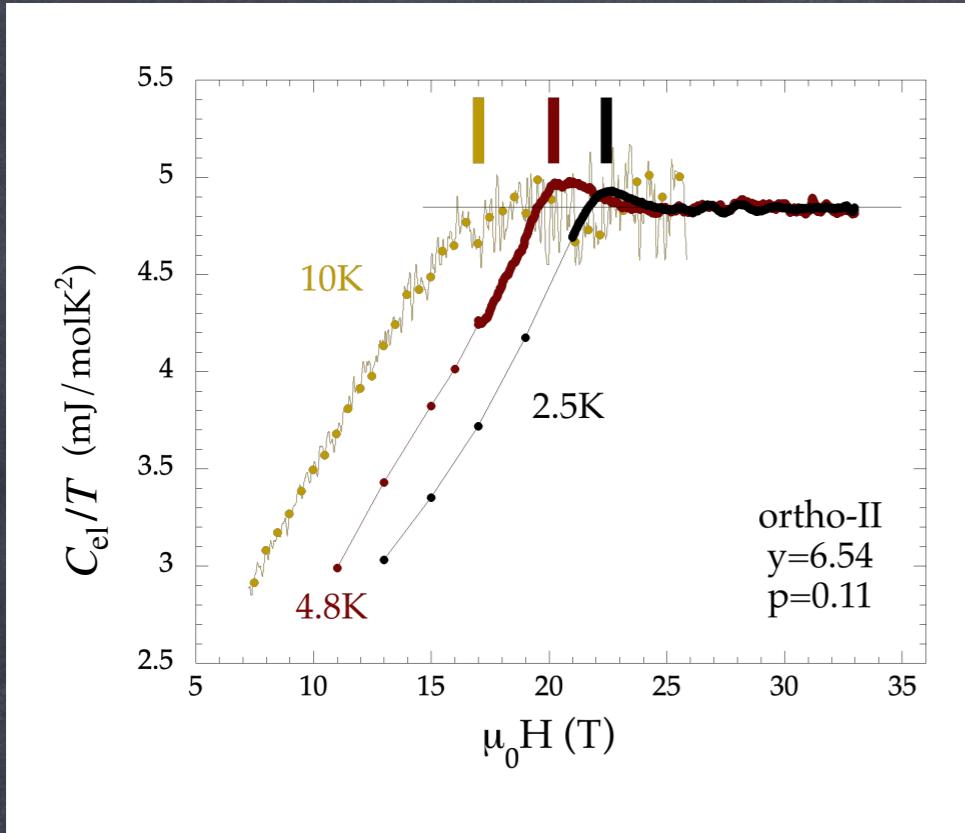
observed at the SC transition

Its origin still has to be clarified...

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quantum critical point ???

but let's follow the temperature dependence of  $H_{\text{DOS}}$

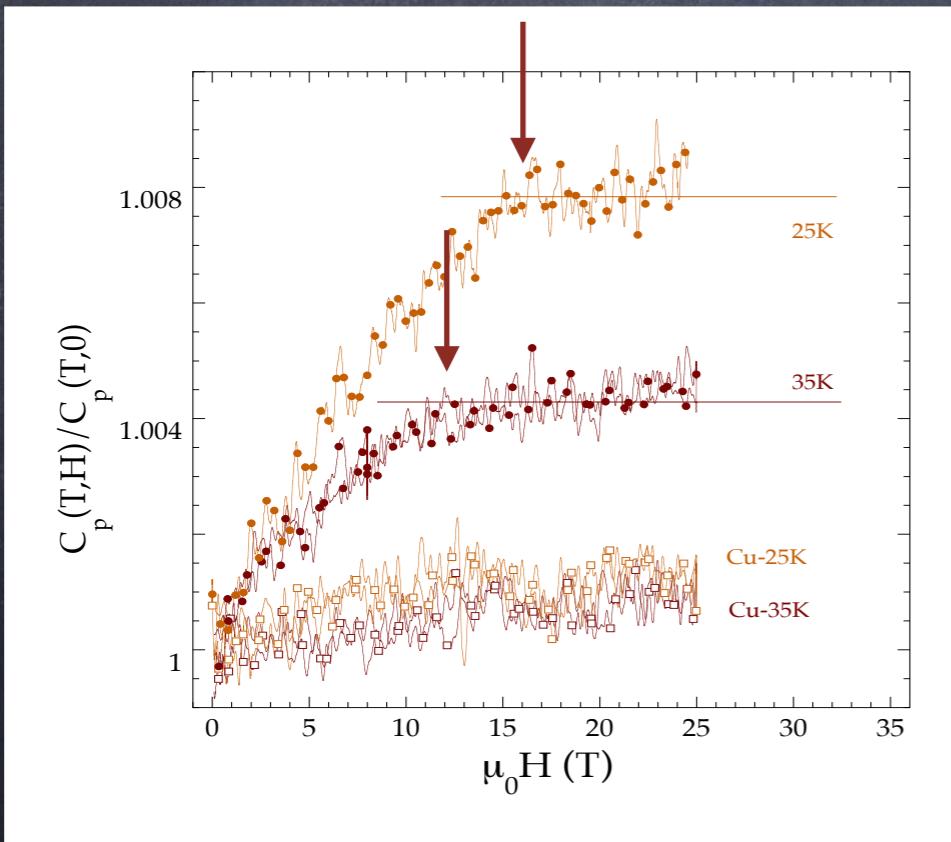
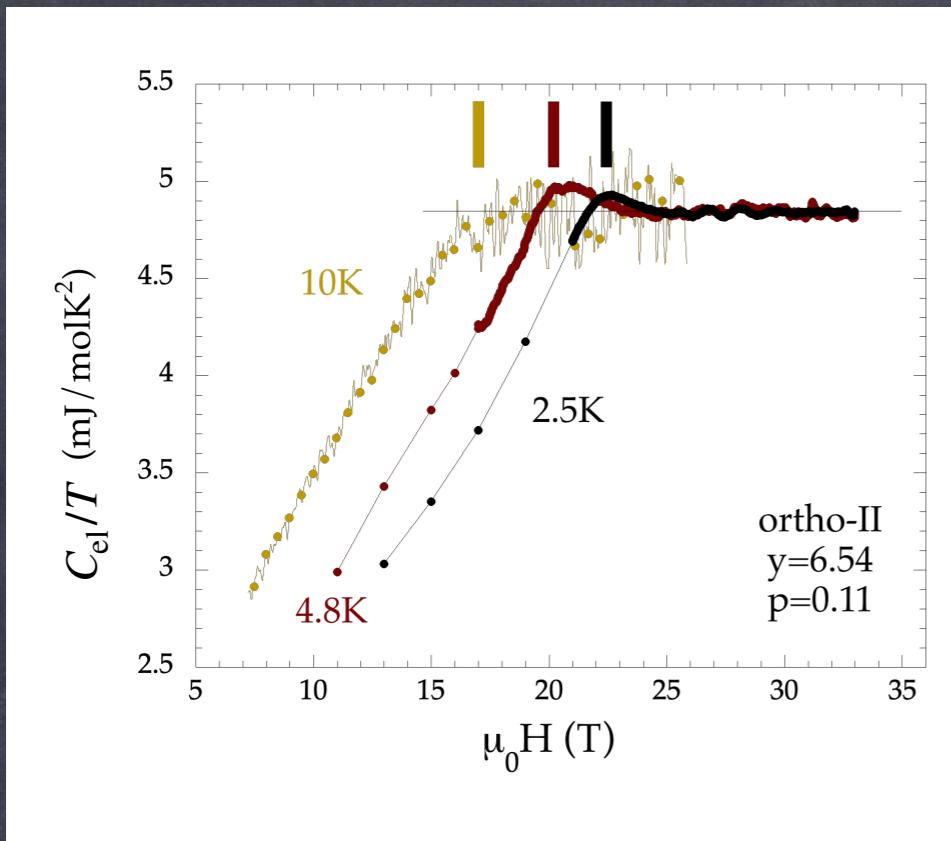


As expected  $H_{\text{DOS}}$  decreases with  $T$

$$\text{but... } \frac{C_{\text{el}}}{T} = \frac{C}{T} - \beta T^2$$

and the phonons contribution  
rapidly increases

⇒ increasing signal/noise ratio



As expected  $H_{\text{DOS}}$  decreases with  $T$

$$\text{but... } \frac{C_{\text{el}}}{T} = \frac{C}{T} - \beta T^2$$

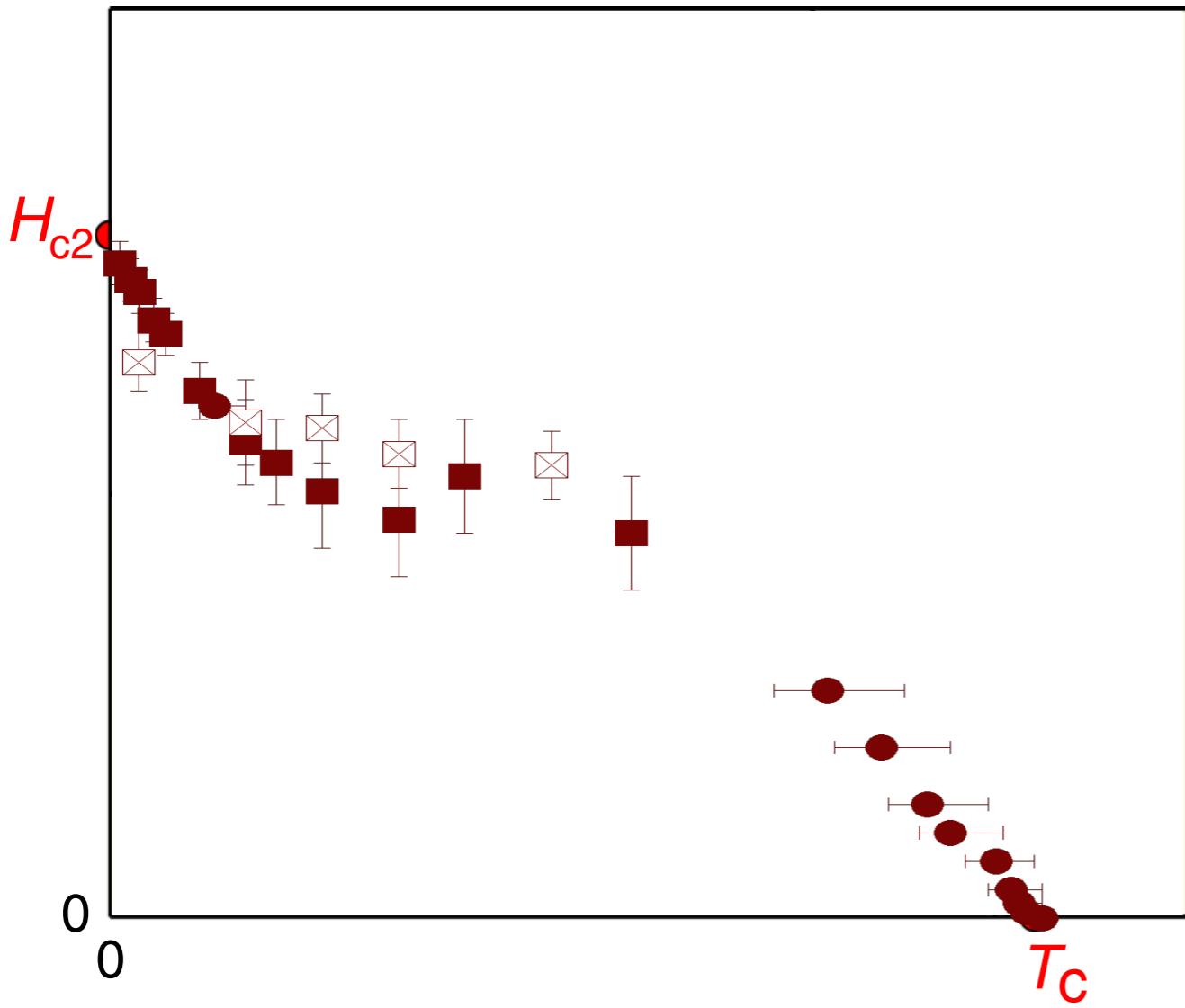
and the phonons contribution rapidly increases

⇒ increasing signal/noise ratio

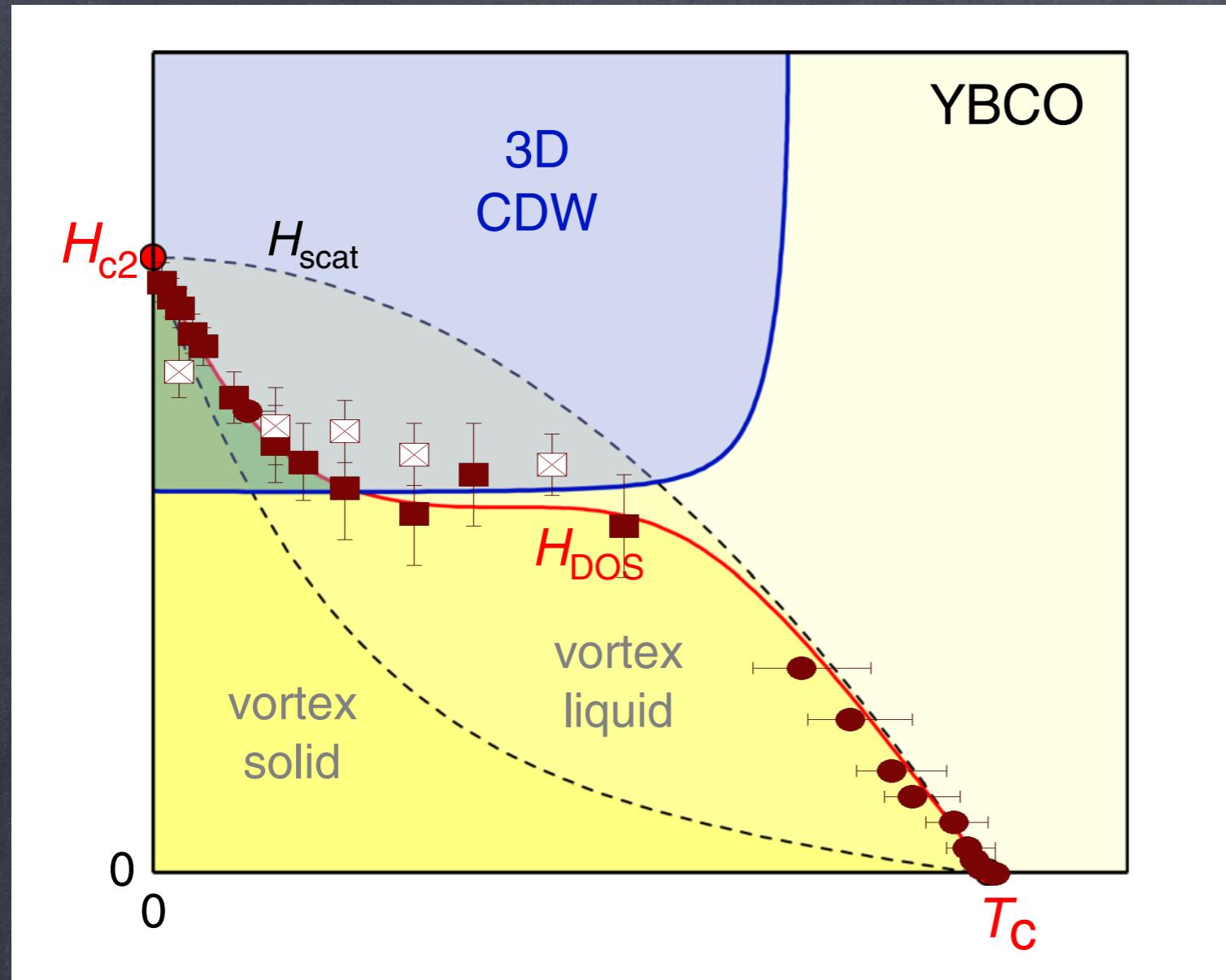
⇒ the variation in  $C_{\text{el}}/T$  becomes smaller than 1% above 20K !

but can still be determined

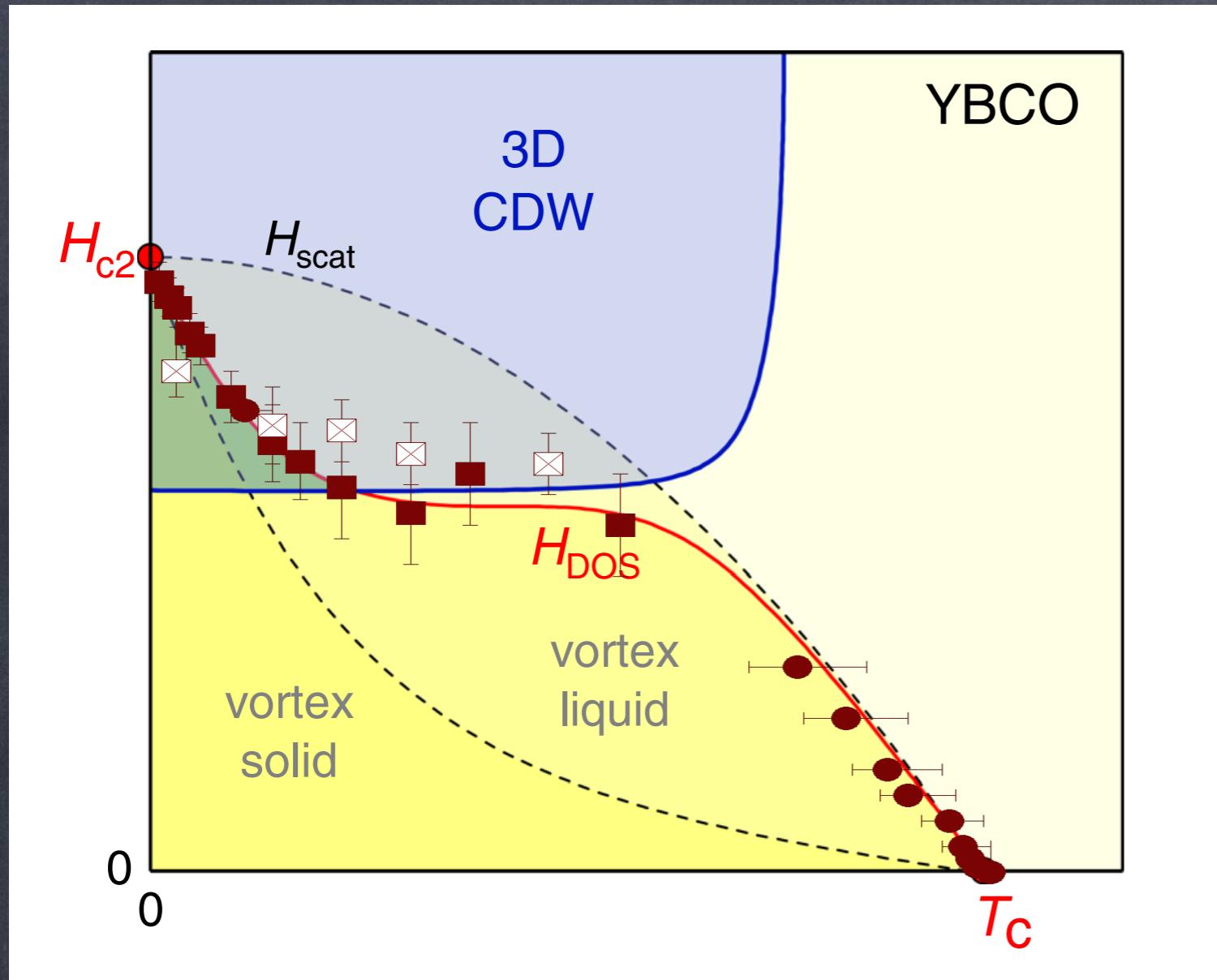
Confirmed by NMR  
(Knight shift) measurements  
Group of M-H. Julien  
see J.Kacmarcik *et al.* PRL 2019



Upturn of  $H_{\text{DOS}}(T)$   
at low T?



**Upturn of  $H_{\text{DOS}}(T)$  at low T?**  
 SC & CDW eventually establish a form of **cooperation** at low T



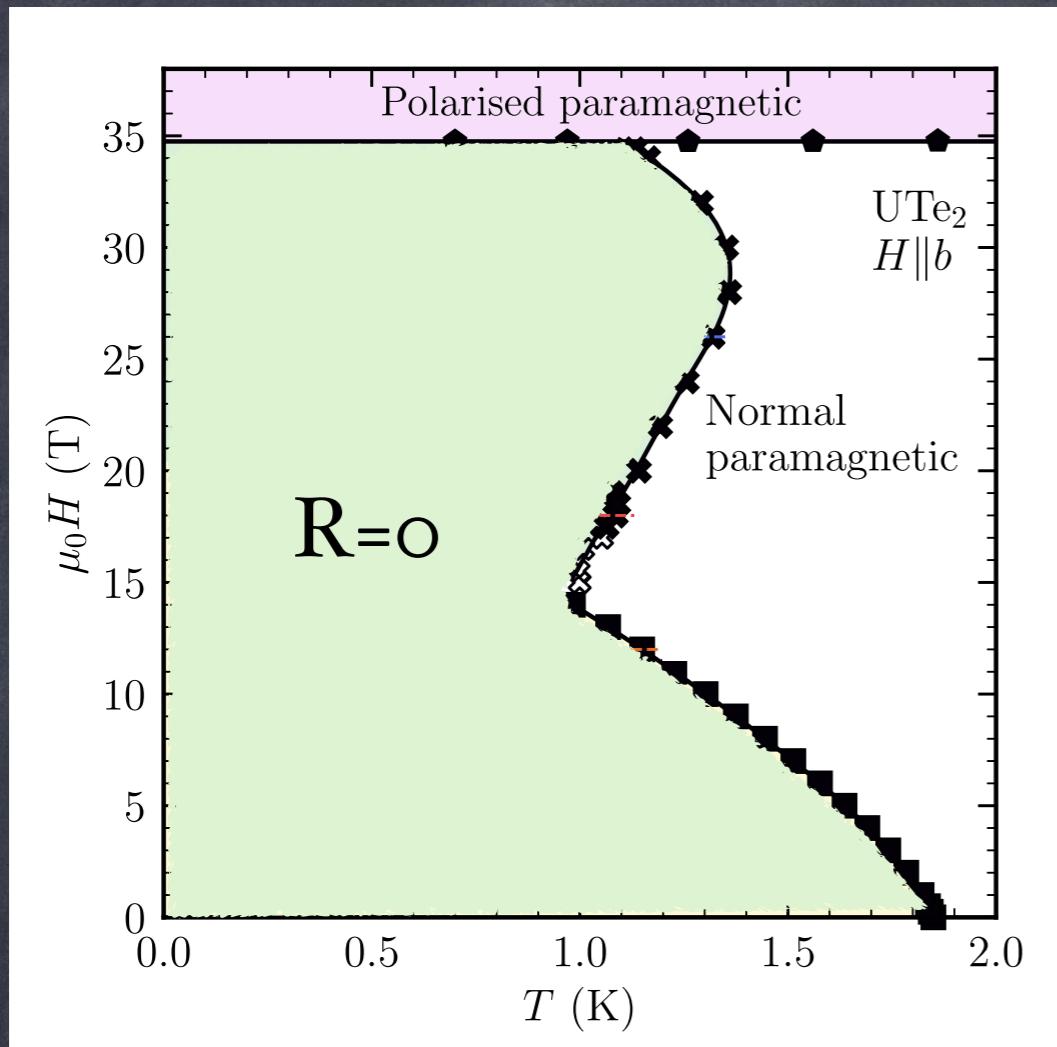
**Upturn of  $H_{\text{DOS}}(T)$  at low T?**  
 SC & CDW eventually establish a form of **cooperation** at low T

giving rise to some kind of **filamentary SC** at the interface of CDW domains ?  
 (or *fragile* SC at CDW dislocations). Yu & Kivelson PRB 2019, Leridon et al. New J.Phys. 2020

or «FFLO-like» upturn, related to the **pair-density wave order** ?

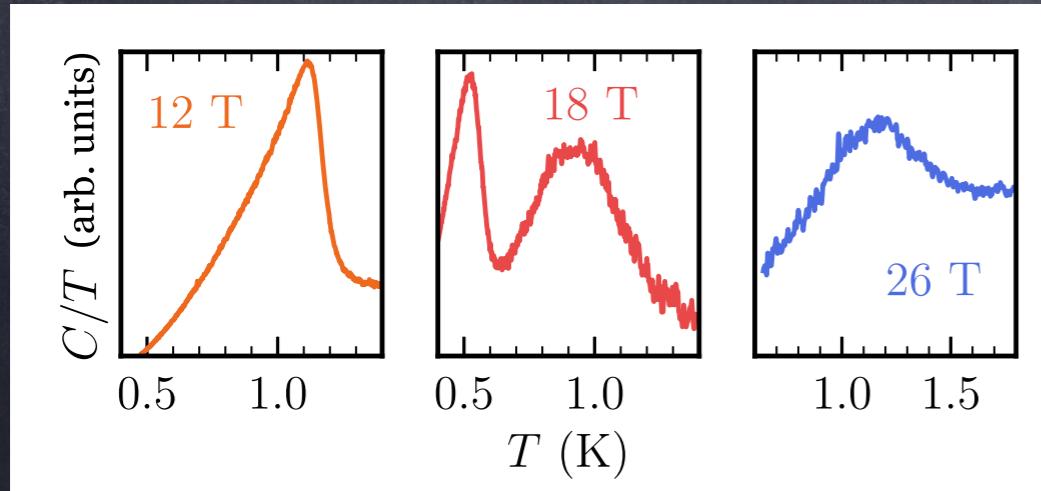
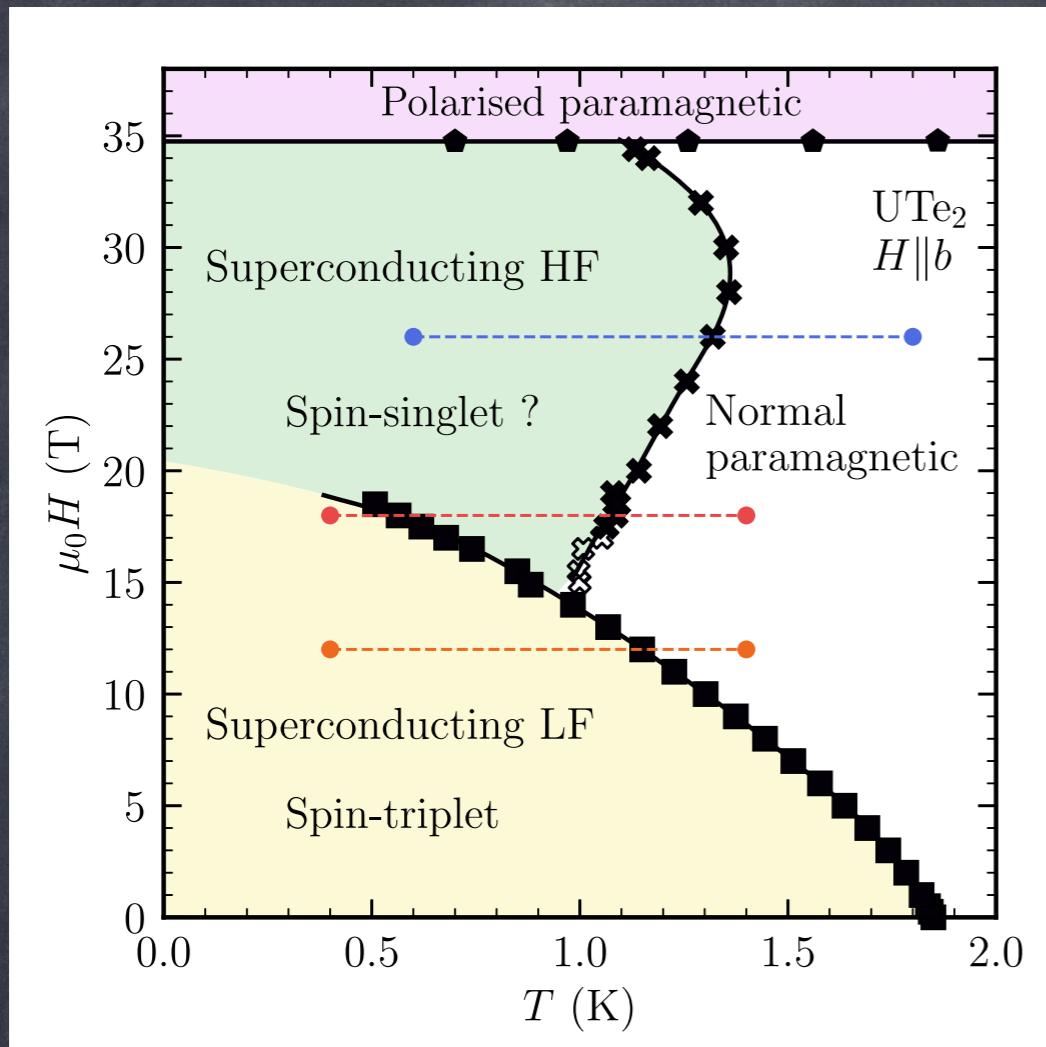
Agterberg et al. PRB 2015, Berg et al. PRL 2007, Dai et al. PRB 2018

A last exemple to flash....



**Re-entrant superconductivity in**  
**UTe<sub>2</sub>**  
(possible spin-triplet and topological SC)

A last exemple to flash....



**Re-entrant superconductivity in  $\text{UTe}_2$  (possible spin-triplet and topological SC)**

C/T measurement  
⇒ phase transition **within** the superconducting state

A Rosuel *et al.* PRX 2023

- A. Demuer<sup>1</sup>, D. Leboeuf<sup>1</sup>, G. Seyfarth<sup>1</sup>, M-H. Julien<sup>1</sup>, H. Mayaffre<sup>1</sup>
- J. Kacmarcik<sup>2</sup>, A. Rydh<sup>3</sup>, Y. Kohama<sup>4</sup>, Z. Yang<sup>4</sup>, B. Fauqué<sup>5</sup>, K. Behnia<sup>5</sup>
- L. Taillefer<sup>6</sup>, S. Badoux<sup>6</sup>, S. Verret<sup>6</sup>, A. Legros<sup>6</sup>, A. Gourgout<sup>6</sup>, N. Doiron-Leyraud<sup>6</sup>
- F. Hardy<sup>7</sup>, C. Meingast<sup>7</sup>
- A. Rosuel<sup>8</sup>, A. Pourret<sup>8</sup>, G. Knebel<sup>8</sup>, J.P. Brison<sup>8</sup>

<sup>1</sup> LNCMI, CNRS-Grenoble

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Thank you for your attention